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NATIONAL BUREAU OF STANDARDS REPORT

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FINAL REPORT

NBS PROJECT WHERE

in support of

USAAMCA PROJECT MNPLS

by
Applied Mathematics Division
and
Computer Services Division



U.S. DEPARTMENT OF COMMERCE NATIONAL BUREAU OF STANDARDS

NATIONAL BUREAU OF STANDARDS

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May 31, 1972

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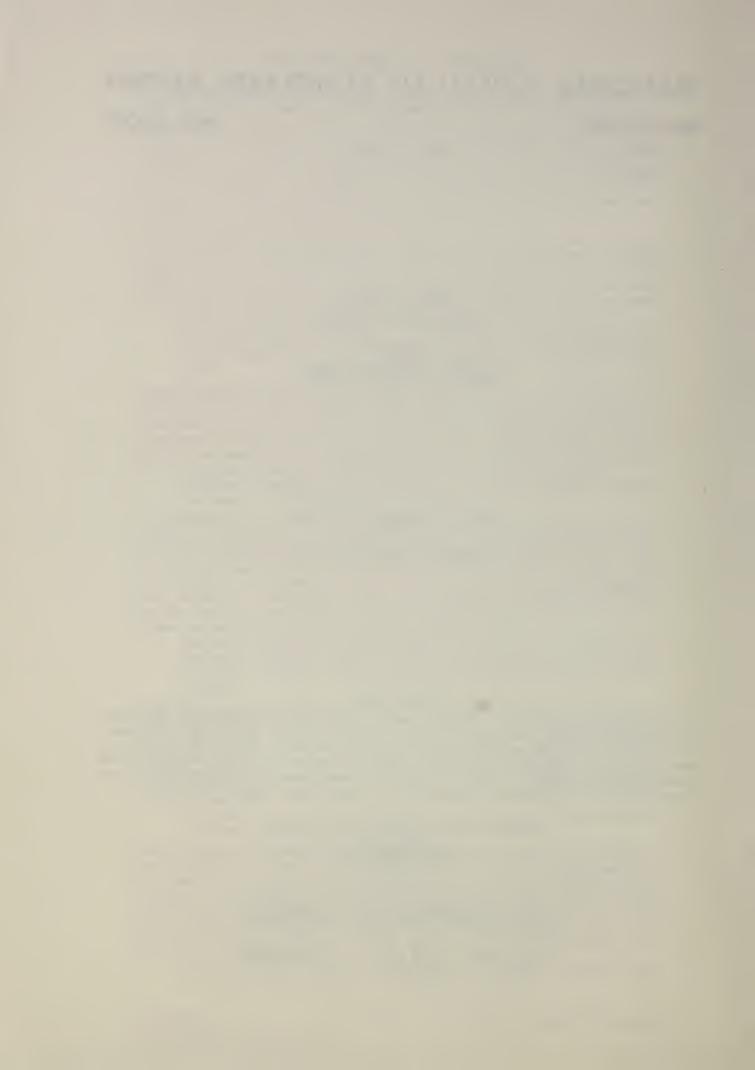
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Approved for public release by the Director of the National Institute of Standards and Technology (NIST) on October 9, 2015.

accounting documents intended ubjected to additional evaluation isting of this Report, either in Office of the Director, National the Government agency for which lies for its own use.



U.S. DEPARTMENT OF COMMERCE NATIONAL BUREAU OF STANDARDS



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 - Working paper no. 9: The MNPLS simulation ("WHERESIM").

 By R.H.F. Jackson



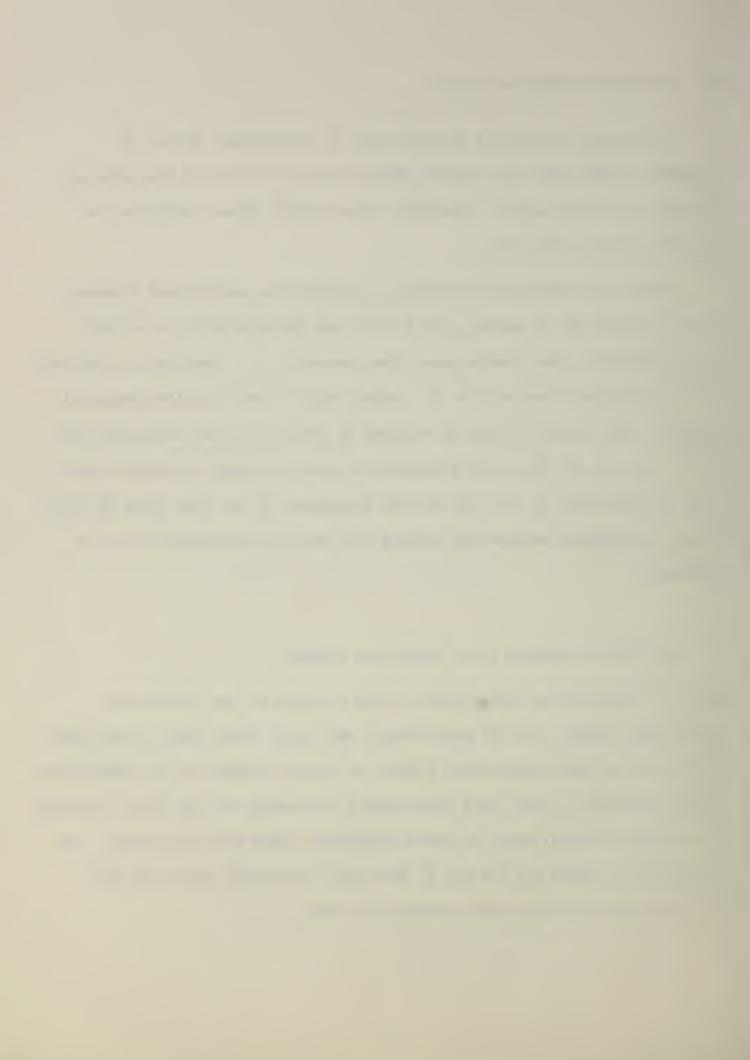
1. Executive summary of report

This report summarizes the work done at the National Bureau of Standards (NBS) under its project WHERE in support of the US Army Advanced Materiel Concepts Agency's (USAAMCA) project MNPLS (Micro Navigation and Position Location System).

MNPLS is a system that utilizes a time-division multiplexed frequency that is shared by n units, all of which are synchronized by a suitable electromagnetic signal during each time interval ΔT . Each unit is assigned one or more time slots within ΔT during which it emits an electromagnetic signal. This signal in turn is received by several but not necessarily all other units in the field which measure the time of flight of the EM signal; from the knowledge of the time and the assignment of the time slots for each unit, the distance between the sending unit and the receiving unit can be inferred.

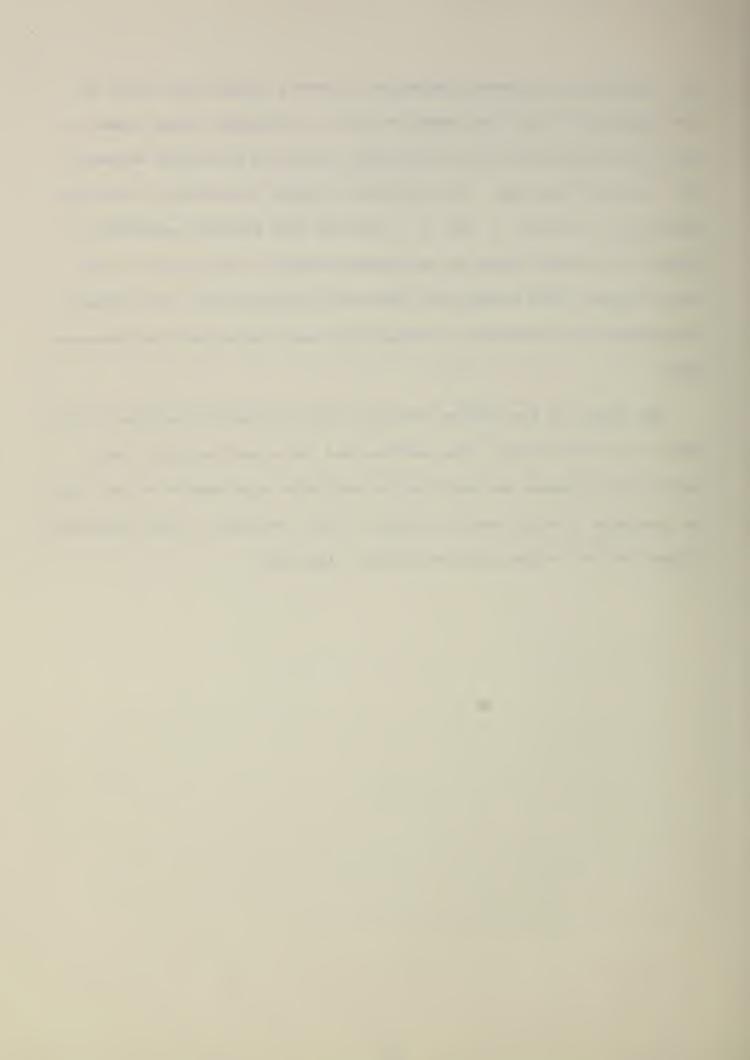
For NBS the problem to be solved was twofold:

(1) To determine the feasibility of such a system in the presence of measurement errors. If all measurements were exact three units in the plane or 4 units in three-space would suffice to locate another (or all other)units. In the presence of error more measurements are needed and the "best" solution that minimizes total error in some mathematical sense has to be found. The fundamental problem for NBS was to show that the overall error does not increase unduly as the system develops in time.



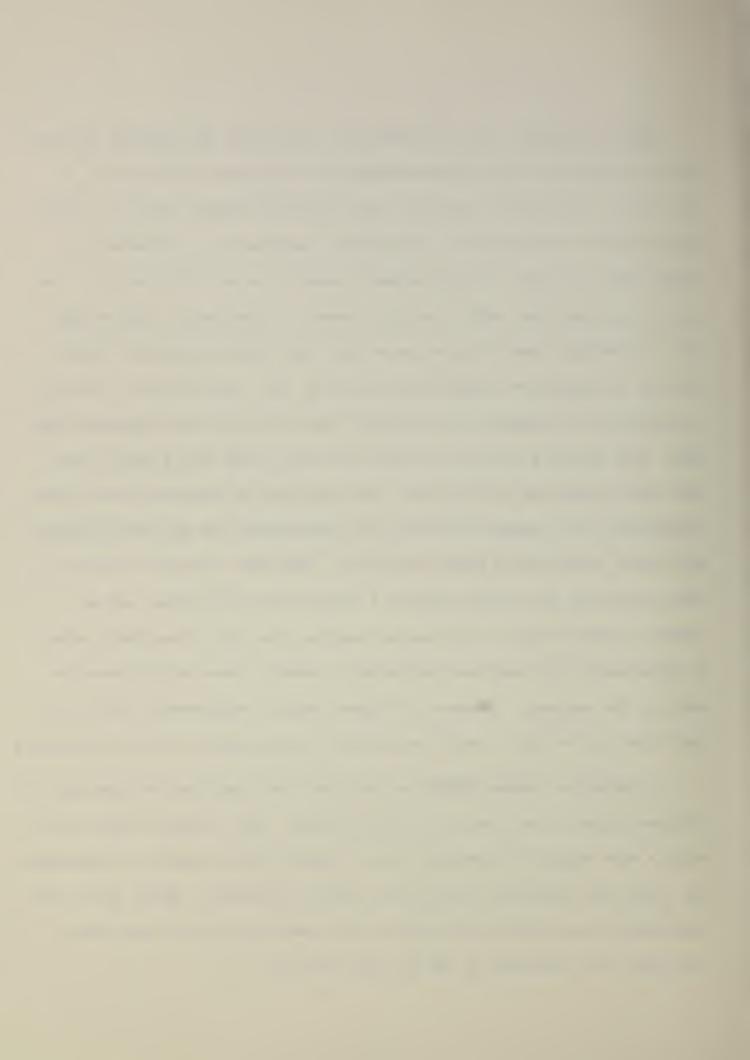
(2) To develop a computer simulation for such a system that allows the investigation of real-time scenarios with a sufficiently large number of units undergoing battle-field manoeuvres, each with prescribed movements over suitably long times. The simulation program determines the distance between any two units i and j , perturbs that distance according to suitable assumptions about the measurement errors, and supplies to the master computer (the program that determines positions from the distance measurements) the distances as though they came from actual field measurements.

The output of the program consists of the successive locations of all units, the errors between true position and calculated position, and a measure of confidence derived from the available measurements but not from the knowledge of exact position (which is only available to the simulation program but not to the position location algorithm).



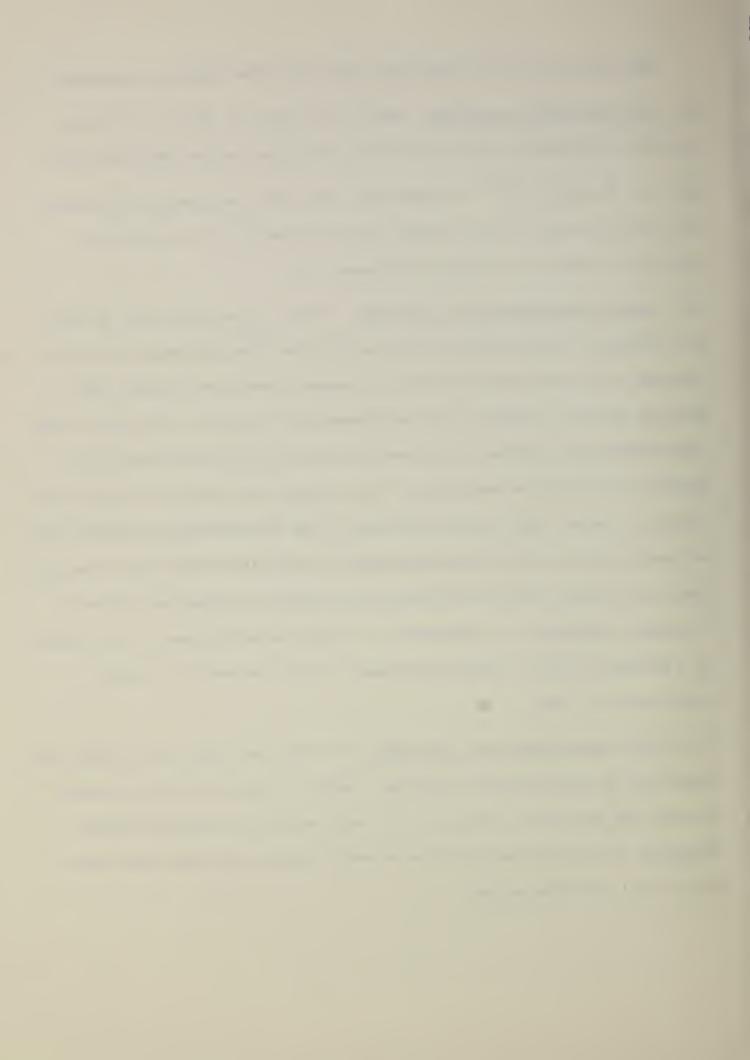
NBS has designed a set of mathematical algorithms for position location determination that allow the determination of successive positions of n field units, from inputs containing only distances between units, or perhaps those distances accompanied by independent measurements of differences in height above sea level. The experiments based on actual deployments in the Boston area show that, with a suitable number of fixed units, the average error of position over all units can be kept well within acceptable limits. Based on a range-error standard derivation of 6m , and using all 83 units as reporters, the maximum error during 2 hours of actual time remained under The average error was 4.5m over all units, with only 3 units "lost" more than 8 times out of 240 tries. When only the 39 fixed units were used as reporters, the average error was 4.7m, the maximum was 40m, but 15 units were "lost" more than 50 times out of 240. (The term "locators" refers to those users that do actually receive a signal from the locatee, and do report a time-of-flight to the master computer; the term "reporters" refers to those users that have been instructed to report time-of-flight measurements to the computer. Because of "line-of-sight" requirements, not all of the latter may be able to serve as locators for any given location-operation.)

A simulation package WHERSM was designed that simulates the operation of a Micro-Navigation and Position Location System. This program allows one to stage a wide variety of movements for any battle-field scenario; it generates the inter-unit distances, perturbs the ranges according to agreed upon error distributions and provides the links to the position location algorithms which were also developed at NBS for this purpose.



The position location algorithms fall into three distinct categories:

- (1) <u>Two-dimensional algorithms</u>. Where the terrain is flat, no altitude reference is necessary and the resulting algorithms become two-dimensional. The sum $\sum w_i(r_i^2-d_i^2)^2$ is minimized, where the sum extends over some or all reporting units and the weights are determined by the estimates of variance of each of the reported distances d_i .
- (2) <u>Pseudo three-dimensional algorithms</u>. Where the altitudes are so small in relation to the horizontal distances that the slant distances are nearly the same as the horizontal distances it becomes necessary to reduce the position location problem to the two-dimensional one above. Not only is the three-dimensional problem ill defined mathematically, but we have also a genuine multiplicity of solutions if all locators are nearly in a plane and trying to locate a unit outside the plane. The determination of heights that are small against the horizontal distance is impossible within any reasonable limits of accuracy and the altitude must therefore be determined either by barometric reference or a reference to a digitized terrain map. For example, at a distance of 1km, a range uncertainty of only 6m leads to a height uncertainity of 110m.
- (3) <u>Fully three-dimensional algorithms</u> are being used when the altitudes are comparable to the horizontal distances. Again, a penalty-function approach is used that minimizes $\sum w_i (d_i^2 r_i^2)^2$ with suitably determined weights depending on the variance of the measurement and the sum being taken over some or all reporting units.



The following results were obtained:

- o The test runs conducted on the Boston deployment show that stability of the position-location process is indeed achievable as long as some units remain fixed.
- o Computer size for position location:

Runs were all carried out on the UNIVAC 1108 at NBS. For this machine, the formula for computing the number of computer words required by the position-location algorithms as they are currently programmed is as follows:

$$26N + 7R + 3874$$
,

where N = number of units in the field, and R = the maximum number of ranges being reported.

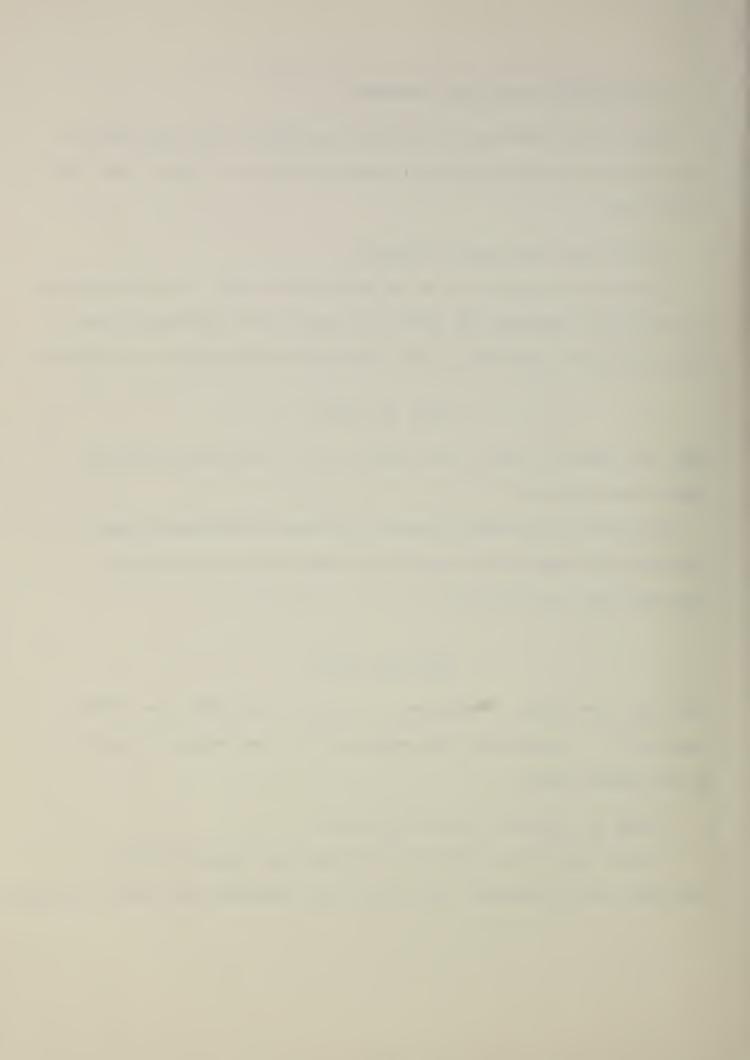
As a matter of possible interest, the number of additional words required by the simulation program (into which the position-location algorithms were inserted) is:

$$91N + N_S + 4002$$
,

where N_S = the number of subcycles in a cycle of the MNPLS (see Working Paper No. 9). Furthermore, the preprocessor to the simulation requires 39,714 computer words.

o Timing for position location operation:

Several runs are available from which the time required by the algorithms can be estimated. One run was done using LSS(3d), with 20 locators;



it required approximately 16.5ms per location operation. A run with 15 locators using slant range reduction took 8-12ms; with 20 locators, the computation took 14 to 18ms. For the Boston deployment, using 39 reporters (but probably less than 15 locators on the average because of intervisibility restrictions), 8 to 14ms were required; using 83 reporters, 17 to 25ms were required. Since the algorithms are not optimized for running time, it is reasonable to expect some decrease in these times for the operational system.

2. Description of general approach used in this report.

(1) Simulation.

The simulation of the battlefield scenario is done in our NBS-developed computer program WHERSM. This program provides for a "real life" framework for MNPLS through its capability for moving all field units along prescribed paths, or subjecting these to random changes in their direction of movement. WHERSM generates all the inter-unit distances(ranges); checks, if necessary, for intervisibility (by look up in an intervisibility matrix); disturbs the exact ranges according to known error distribution laws; and transmitts these "measurements" to the position location algorithms that we developed here at NBS and which are described below.

The simulation package also provides a facility for monitoring the operation of such a system under a variety of movement scenarios; and ultimately it provides for a variety of outputs that are desired for both checking out the feasibility of the entire system and what might be called the ultimate output that would be useful to the field commander who is interested in the whereabouts of his units. For details of WHERSM, the reader is referred to working paper No. 9 in the appendix of this report.



(2) Algorithms.

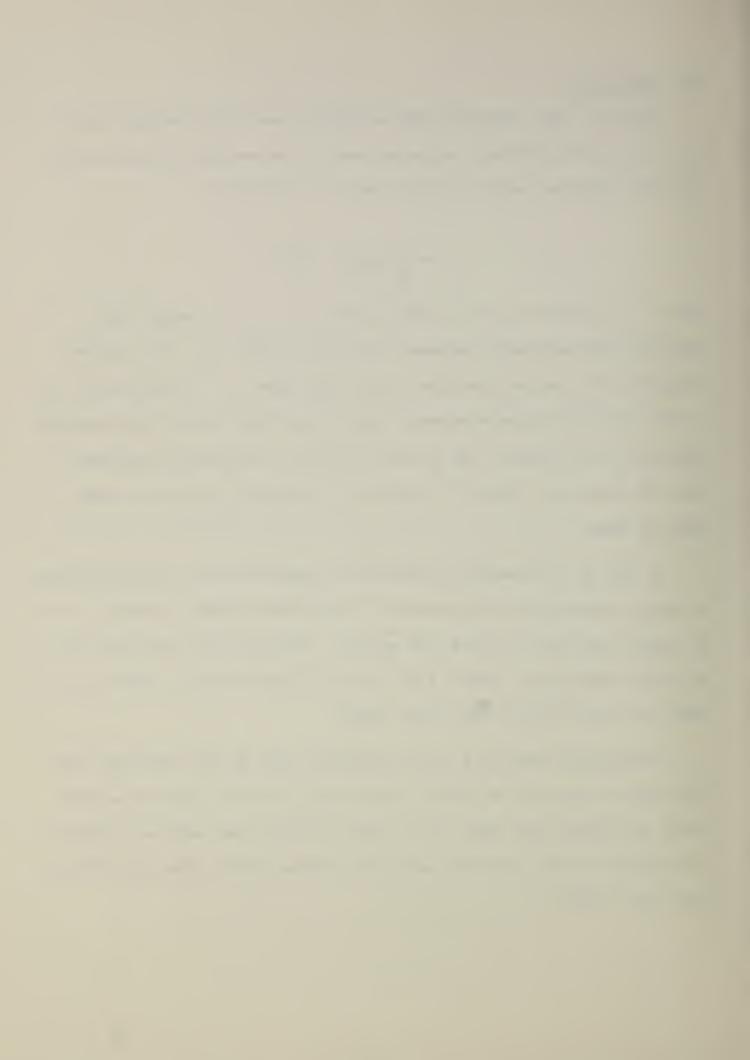
The basic LSS algorithm that we finally used after numerous experiments designed to eliminate competing ones is the so-called "least-squares squared" algorithm, which minimizes the penalty function

$$E = \sum_{i} w_{i} (d_{i}^{2} - r_{i}^{2})^{2}$$

where i is taken over all of the locators and w_i is a weight that increases with decreasing variance of the observation r_i , the reported distance of the locatee from the locator with index i . The quantity d_i is the calculated distance between (x_i, y_i, z_i) and (x,y,z) the estimated position of the locatee. The solution (x,y,z) is obtained iteratively from the equations $\partial E/\partial x = 0$, $\partial E/\partial y = 0$, $\partial E/\partial z = 0$ once a starting point is known.

As long as a trajectory is known for a given locatee, the initial guess is simply obtained from extrapolation. If the unit is lost, however, a set of linear equations is solved (LSL method). Details of the LSL method can be found in NBS report 10663: First Interim Progress Report on NBS Project WHERE in support of USA AMCA Project MNPLS.

The appendix contains a list of variables used in the simulation code. Since this is the part of the NBS system that interfaces with the outside world, we believe that those are the only variables that have to be listed. The variables in the algorithm parts are internal and are thus not reference able from outside.



3. Review of analyses to date.

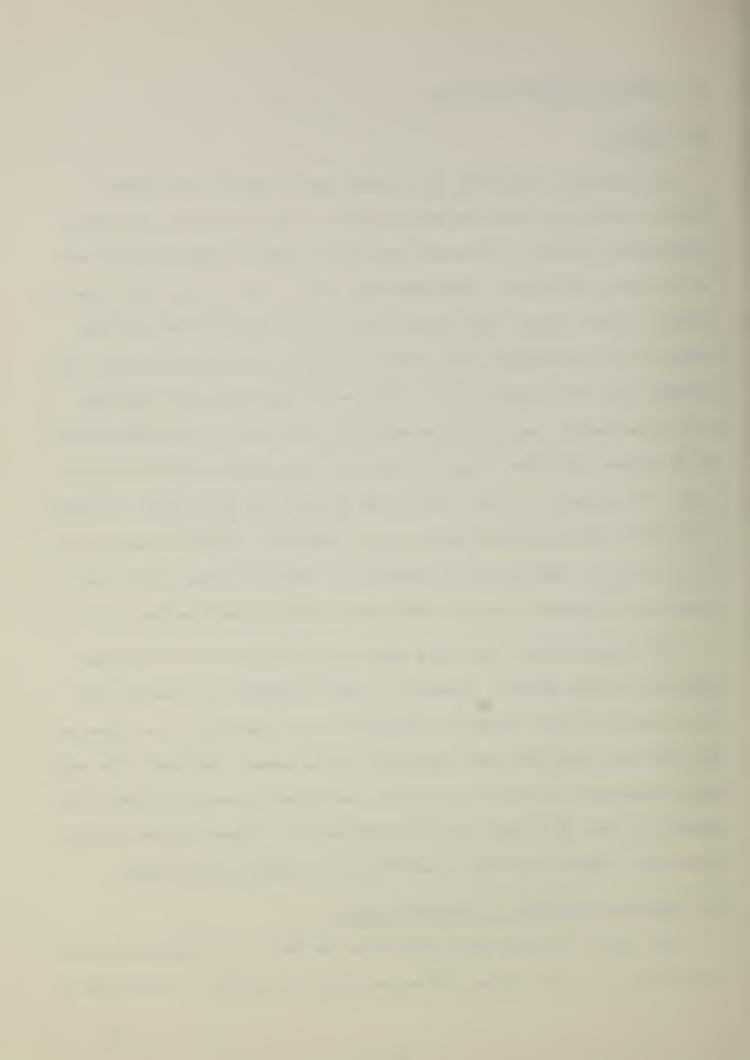
3.1. General.

As originally conveived, the testing was to comprise two phases: initial testing to choose the best position-location algorithm, and final verification testing to determine how well the chosen algorithm would work on the Boston deployment. This neat plan did not fit the real-life flow of events, however: every stone turned over revealed two more yet unturned. The process of developing a new system is bound to contain such loops. For example, one does not know how to optimize the algorithm until one knows the system design, but the system design is sensitive to the effectiveness of the chosen algorithm. Thus the two phases gradually blurred into each other. Furthermore, in the limited time allotted for this study, it seemed that effort would be better spent getting reasonable answers to more of the real questions, rather than "optimizing" on a smaller subset of the questions while assuming particular (and questionable) answers to the others.

For these reasons, a strictly chronological account of our analyses would not be very helpful. Instead, it seems reasonable to describe the test results by first building a framework of the questions to be answered, and then describing the tests performed and the answers obtained. The next section consists of a set of questions; the following section presents the answers to date, as gleaned from the experimental program and from certain theoretical studies undertaken specifically to support that program.

3.2. Questions pertinent to the MNPL system.

The general question that constitutes the focus of a feasibility study is: Will the proposed system perform satisfactorily under the conditions of



its intended use? This question is however a very broad one; it asks essentially whether the final outcome of the feasibility study is "yes", "no" or "maybe", and thus does not give much guidance in conducting the study. Thus one is led to pose narrower queries:

a. General Questions

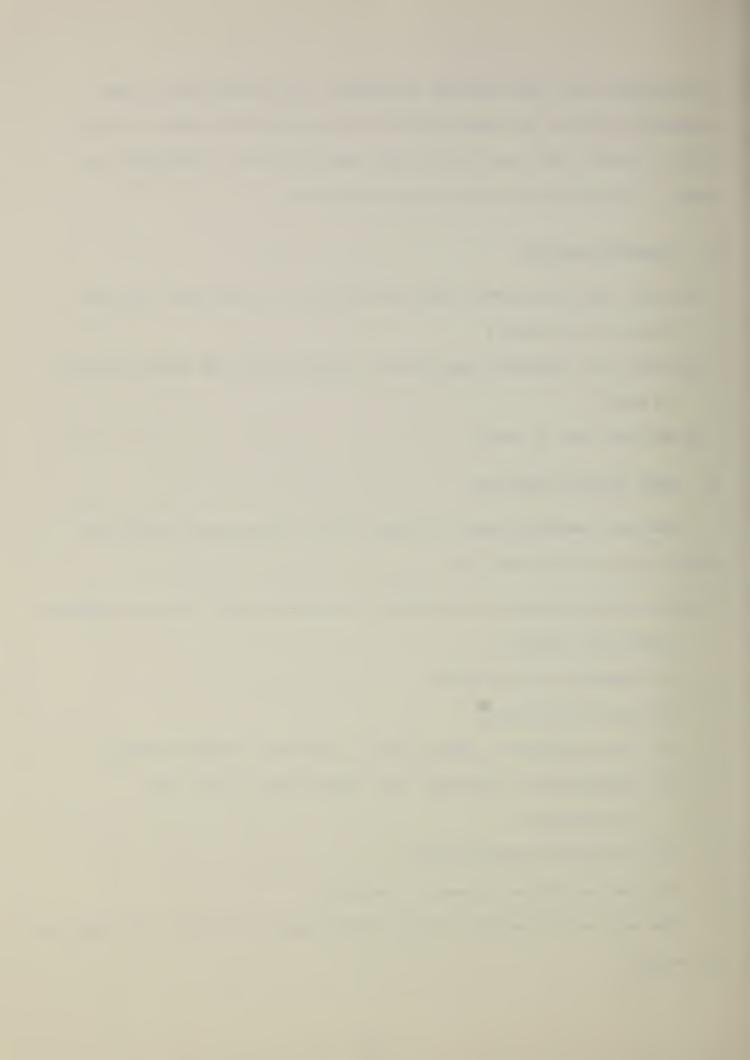
- (1) Under highly optimistic conditions, will the system work? (If not, terminate the study.)
- (2) Under what reasonable near-minimum conditions can the system be made to work?
- (3) How well does it work?

b. More Specific Questions

The next question leads to a whole set of sub-questions, which are listed along with the main one.

- (4) What position-location algorithm(s) should be used? For each candidate algorithm, consider:
 - (a) Computer time required?
 - (b) One-step accuracy?
 - (c) Error propagation (sensitivity to locators' position errors)?
 - (d) Sensitivity to occasional very large errors in the range measurements?
 - (e) Affected by dimensionality?
 - (f) Need an initial estimate of position?

The next set of questions refers to restrictions placed on the units in the system.



- (5) How many (if any) units must remain fixed?
- (6) Must they be permanently fixed in known positions?
- (7) How many reporters are required, to keep the errors small?
- (8) Will ground units have to carry altimeters? Instead, will a digitized map, stored in the computer, suffice?
- (9) How accurate must altimeters be (both ground and airborne)?

 Questions (10) (19) refer to design of the algorithm.
- (10) How often should units report?
- (11) How many aircraft are required, in order to use a three-dimensional algorithm on ground units?
- (12) How should one handle near-planarity (when any aircraft present are flying very low)?
- (13) When should the algorithm:
 - (a) ignore height differences?
 - (b) reduce slant ranges to horizontal distances?
 - (c) use a 3-dimensional method?
 - (d) use 3d for aircraft, slant range reduction for ground units?
- (14) How should the locators be chosen?
- (15) How weight the locators?
 - (a) What is the distribution of range errors?
 - (b) How handle the occasional occurrence of range measurements with extremely large errors?
 - (c) How estimate the accuracy of an estimated position?
- (16) Should the locators be "relocated" ? (i.e., should the locators' positions be adjusted, based on discrepancies between measured ranges and calculated ranges to the best estimate of locatee's position?)



- (17) Use only fixed units as reporters? How soon after they become fixed?
- (18) Can the algorithm determine (satisfactorily) which units are fixed?

 If not, could a moving/stopped indicator bit be included in the transmission?
- (19) After the system has been running for a while, and errors have accumulated, is it possible to "restart" the system ---i.e. to treat the set of (currently) fixed units in toto, simultaneously, allowing all position coordinates to vary, in order to converge to good estimates for their positions?

3.3. Conduct, progress, and results of the test program.

The first few questions, above, suggest a beginning emphasis on favorable conditions. The rationale is that, when very little is known about a system, more is learned faster by starting with conditions where the system works tolerably well, and then investigating the effects of departures from these conditions. Accordingly, the first major project was to devise, develop, program, and test several candidate algorithms for determining the position of a locatee, using the (perturbed) ranges to a set of locators, and assuming the locators' positions to be known exactly. That is, attention was focussed first on questions(4). Some of these algorithms were suitable for 2 or 3 dimensions, others were usable in 2 dimensions only. Methods considered were: Linear Method (LM), Smallest Tangent Circle (STC), Least Squares Linear (LSL), Minmax, Least Squares(LS), and Least Squares Squared (LSS). The first two methods use exactly 3 locators in 2 dimensions, or 4 locators in 3 dimensions. The next two are generalizations of the first two,



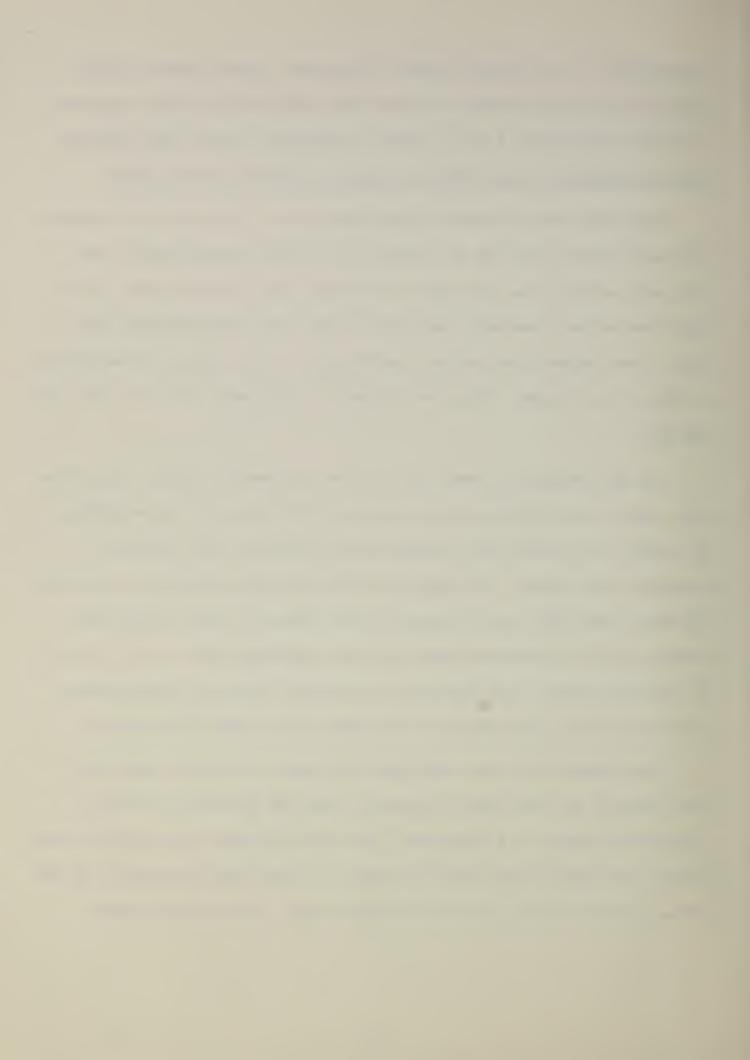
respectively, to an arbitrary number of locators. Least squares and LSS are penalty-function methods. All are fully described in earlier sections, in Working Papers Nos. 7 and 8, and/or in NBS Report 10663, First Interim

Progress Report on Project WHERE in support of USAAMCA Project MNPLS.

Tests were first conducted in two dimensions. STC turned out considerably more accurate than LM, but slower; LS and LSS agreed closely, and were more accurate than any others, but slower than all but Minmax, Since Minmax was no more accurate, and several times more time-consuming, than LSS, it was dropped from further consideration. Also, since LM was inferior to STC, it was dropped. Thus the survivors at this point were: STC, LSL, LS, and LSS.

The next sequence of tests was directed to question (4)(c). For these runs, errors were applied to the positions of the locators, corresponding to a point in time after the system has been operating long enough to accumulate such errors. In these runs, STC fell down markedly. LS and LSS did better than LSL, but the latter was kept since it alone (of the three methods still in contention) does not need a starting value — i.e., is not an iterative method — and therefore can provide a position estimate when the locatee first joins the net or has been out of touch for some time.

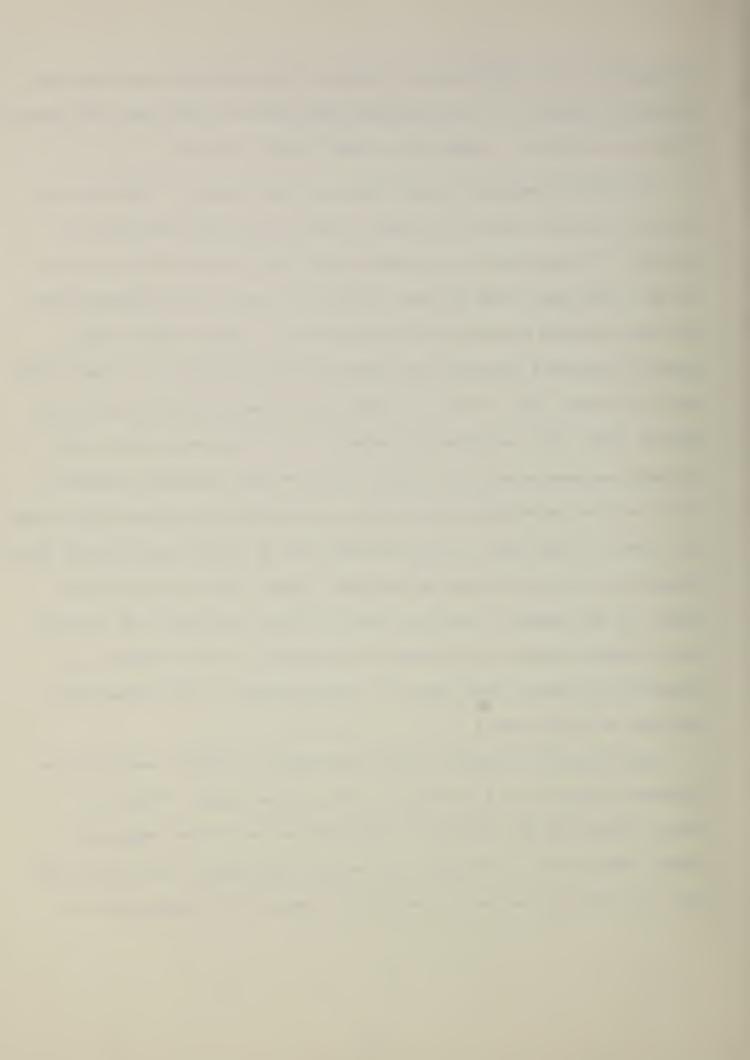
Three-dimensional tests confirmed the pattern of results above, and also accented the importance of geometry: when the locators are nearly coplanar (collinear in 2 dimensions), LSL often produces a very poor estimate, because the planes (lines) that it tries to fit are nearly parallel. LS and LSS also have problems, but not as severe as LSL. These problems were



accentuated in 3d, simply because locators on the surface of the earth are relatively coplanar; the corresponding situation in 2d would have the locators strung out nearly on a single line, a less likely situation.

In terms of computer time LSL was best, with LSS next. Since LSS was devised to perform like LS but faster, these two were then compared for accuracy. 72 trials were run on each method, with 18 users scattered over an 8km by 16km area, with altitudes to 9km, for each of two different values of σ (the standard deviation of the range error). Each of the 18 units served as locatee 4 times for each method and each value of σ . The results were as follows: For $\sigma = 1m$, the position estimates were in error by as much as 3.32m, but the difference between the LS estimate and the LSS estimate was never more than 0.0004m . For $\sigma = 10m$, the errors reached 31.9m, but the two methods gave estimates that differed by no more than 0.045m. As a result of this test, it was concluded that LS and LSS could be used interchangeably so far as accuracy is concerned. Since LSS was considerably faster, LS was dropped. The final result thus was: Use LSS; if no starting value (initial estimate of position) is available, use LSL to obtain one. (Complications develop when there is a choice between 2- and 3-dimensional versions, as we will see.)

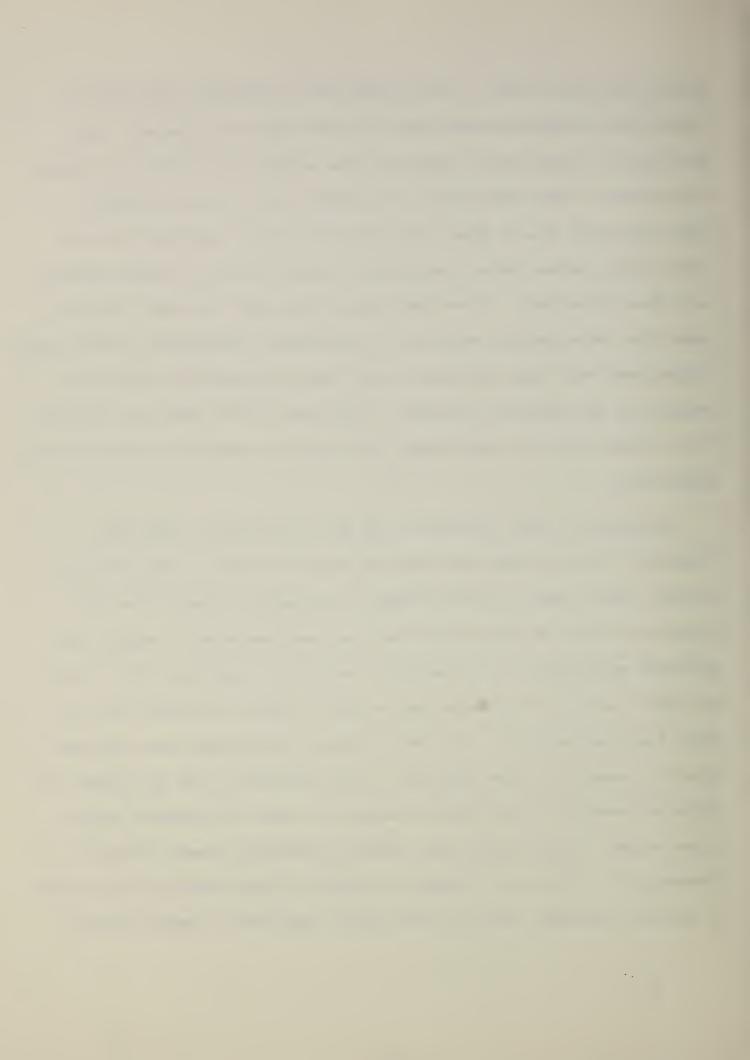
The only part of Question (4) yet unanswered is (4)(d): sensitivity to occasional large errors (outliers) in the measured ranges. This is a severe problem for STC and Minmax, since STC uses only three ranges and Minmax concentrates on minimizing the maximum discrepancy. For LSL, LS, and LSS, the matter is treated in a statistical sense, as is commonly done in



fitting regression curves. The true position is estimated, and then the discrepancies between measured and calculated ranges are examined. Any discrepancies significantly larger than the average are attributed to faulty measurements. These measurements are ignored, and the cycle repeated.

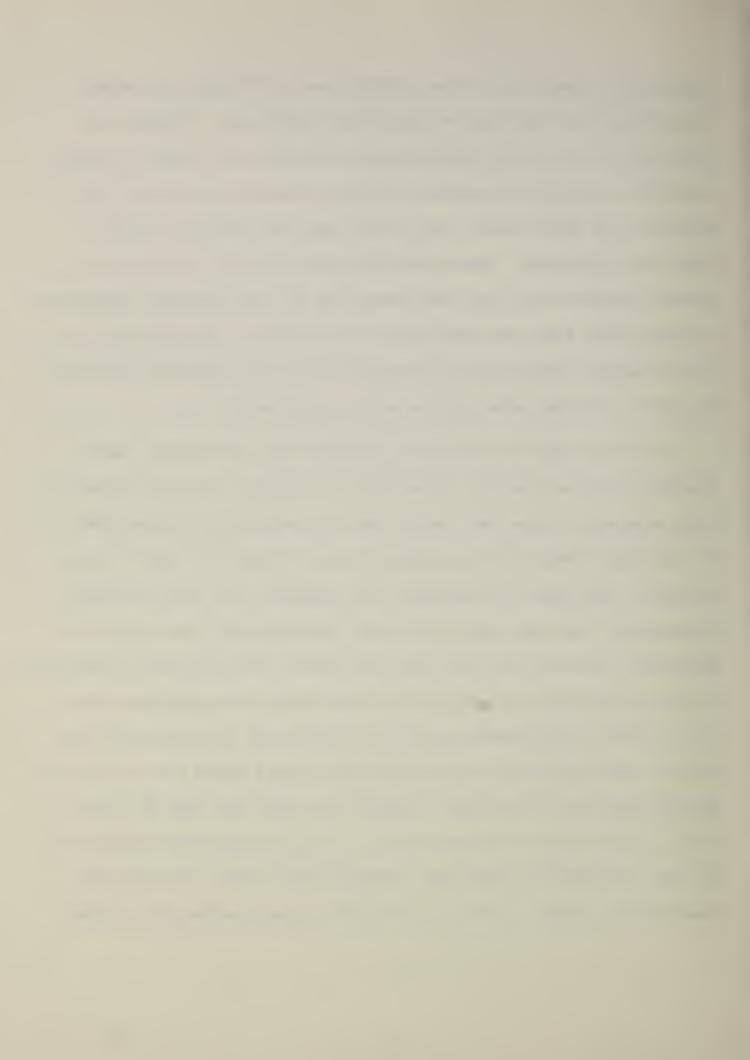
This approach is sure to detect all really bad errors, provided they occur infrequently, unless there is exactly the minimum number of ranges necessary to produce an estimate. It was been shown to be quite efficient, in the sense that the occasional rejection of measurements "apparently" but not really contaminated with large extraneous errors does not appreciably degrade the accuracy of the estimation procedure. The actual cutoff point for rejection is a variable that will need further investigation as part of a system development effort.

Questions 5,6, and 7 pertain to the set of reporters. (The term "locators" refers to those users that do actually recieve a signal from the locatee, and do report a time-of-flight to the master computer; the term "reporters" refers to those users that have been instructed to report time-of-flight measurements to the computer. Due to the requirement for a "line-of-sight", not all of the latter may be able to serve as locators for any given location-operation.) In order to obtain broad(rather than situation-specific) answers to these questions, it was necessary to set up a number of different scenarios, with different numbers of users and different proportions stopped. This diversity was created by employing several kinds of "randomness". Users were assigned to randomly chosen starting points within a specified rectangle, with aircraft heights specified or randomly chosen;



sequences of azimuths were chosen randomly over a 90° range, and azimuth change times were drawn from an exponential distribution. Stopping and starting times were drawn from exponential distributions, chosen to achieve specified values for the expected (long-term average) proportion of users stopped at any given instant, and for the mean times spent in "fixed" status and in "moving". Intervisibilities were similarly randomized, to achieve specified values for the average time two users maintain communication and the average time they remain out of communication. These features were used in various combinations to investigate most of the remaining questions. The results of those investigations are presented below.

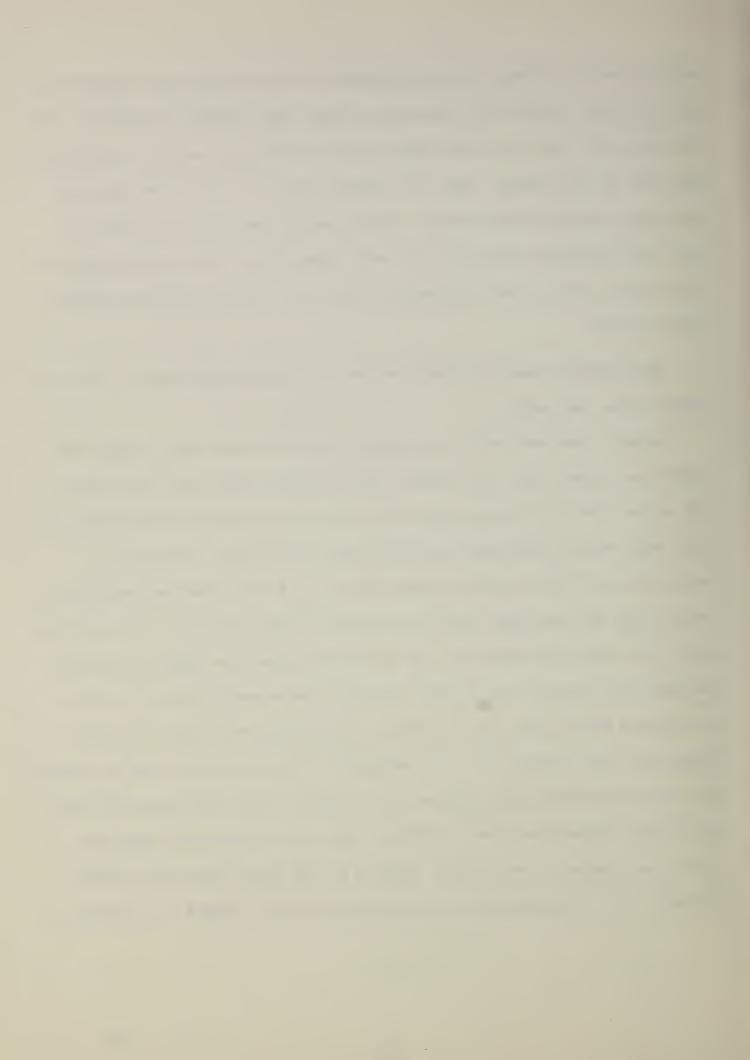
If all the reporters are moving, strange things can happen. Small (random) errors in locating a given reporter propagate into the location of other reporters, so that each remains well-located relative to the others but the whole cluster is displaced(and perhaps rotated) far from its true position. This effect is reasonably well understood, and has been clearly demonstrated. One case involved 30 users, moving more or less in the same direction. 12 users were reporting, with perfect intervisibility (2 dimensions). By the time 100 location operations had been done on each, they had moved 0.9 to 4.1km. The estimated position of the cluster as a whole was 3.3km from its true location, but each element was located within 150m of its true position relative to the others. (Range errors were less than 2m in this case.) The problem can be seen clearly in the following simple example: If all of a collection of fixed users suddenly begin to move, each with the same velocity vector, or all of a collection of users moving with a common



velocity vector suddenly stop, no algorithm based on inter-unit ranges can see the change, because the inter-unit ranges don't change. Therefore, the algorithm will leave the users fixed in the first case, and will continue to move them in the second. This is a special case, of course, but the same principle applies to the average velocity vector when the units begin to move with different velocities - or more generally, to the average change in the velocity vector when they (more or less) all change direction at about the same time.

These results made it plain that one needs some users fixed. The next question was, how many?

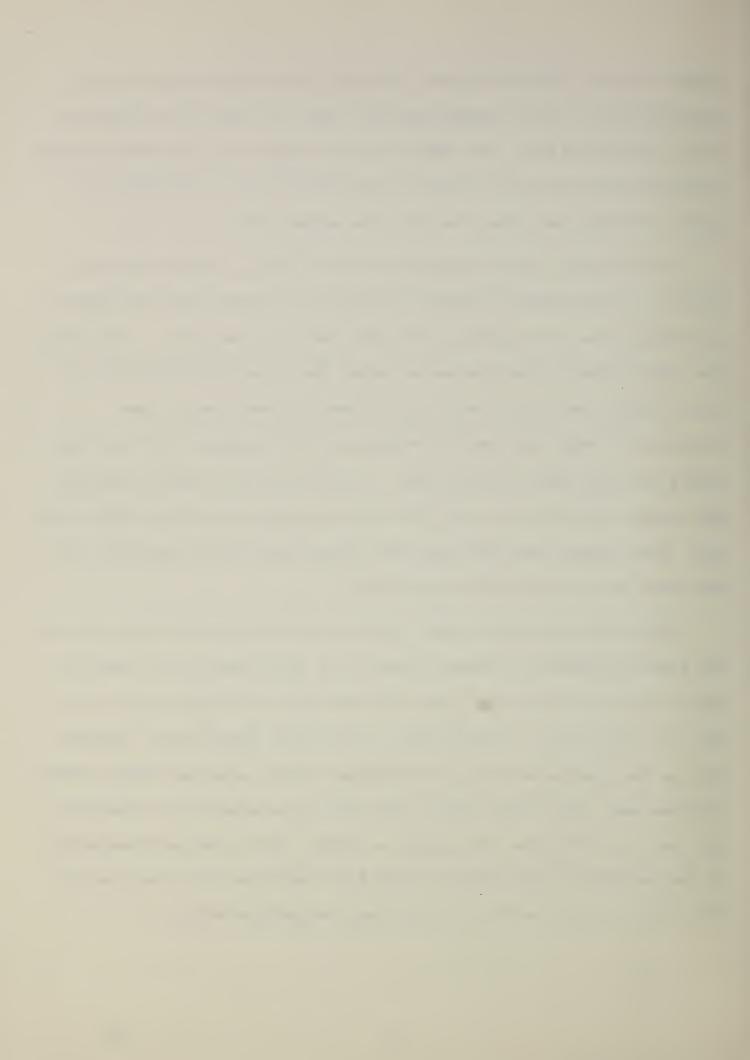
Several runs were made with different sets of fixed users, under two conditions: first, that the computer does not know which users are fixed, and second, that it does know(and can use) this information. The first run, with range errors distributed uniformly from -3m to +3m, involved 15 motorized and 15 foot units; in each set of 15, 5 were fixed and reporting, 5 were moving and reporting, and the remaining 5 were moving but not reporting. After 220 cycles (109 minutes), the xy errors ranged from 500m to 10,240m, and were distributed into all four quadrants (more specifically, 14 users were placed NW of their true locations, 5 SW,10 SE, and 1 NE). For the second run, the subcycle Δt was reduced by a factor of 5, to see if locating the users more often would improve the accuracy. After 613 cycles (60 min), the errors ranged from 570m to 22000m. (The errors grew more slowly per cycle, but faster in real time.) Next, 4 of the fixed users were assumed "known" - i.e., no estimation of their positions was allowed - to provide an



anchor of sorts. After 239 cycles (116 min.), the average error over all users was 9.4m, and the maximum was 23m; over all cycles, the average was 7.2m, the maximum 82m. But there is some evidence that the errors fluctuate considerably with time: in the set of ten cycles prior to the above (i.e., cycles 221-230), the average was 23m; the maximum 69m!

At this point, relocation (Question 16)was tried. (Refer to Working Paper No. 8 for technical details.) Tentative conclusions from the dozen or so runs are: In the beginning, relocation increases the errors. Eventually, the errors without relocation become larger than those with relocation; however, this did not show up until about 2 hours of real time had been simulated, by which time the fast-moving users had separated from the slow-moving and fixed users by about 20km. (At this time, the overall average and maximum errors were 19m and 557m with relocation, and 34m and 1036m with-out. Least Squares was also tried; the average errors were comparable, but the maxima were 570 and 1695 respectively.)

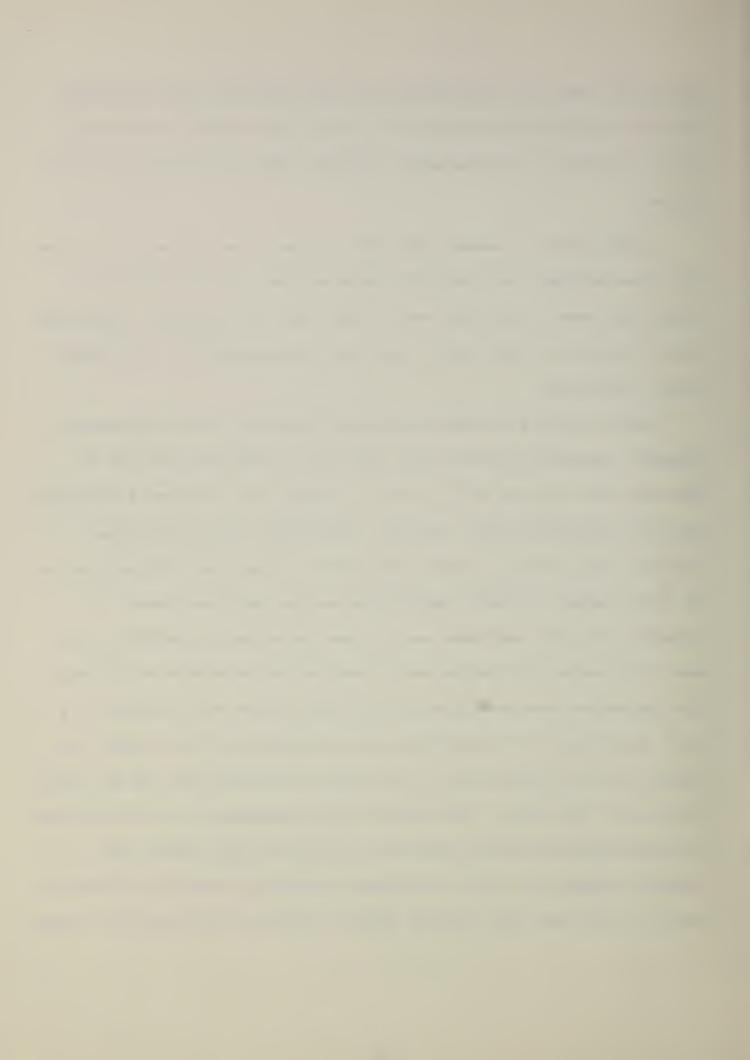
Perhaps more instructive were the shorter runs with differing values of the fraction mentioned in Working Paper No. 8, which measures the extent to which relocation is carried. Runs were done with this fraction set at 0.5, 0.2, 0.1, and 0 (i.e., no relocation). The results showed steady improvement as the fraction went down, with smallest errors occurring when no relocation was done. This shows clearly that there is no advantage to relocation for the first 100 cycles (50 minutes) at least. Still open (and reasonable) is the possibility that relocation should be instituted for a time, now and then, with a small fraction, to help remove accumulated errors.



However, if there are sufficiently many fixed reporters, one can probably do better by periodically going into a survey mode wherein all the fixed units' positions are simultaneously adjusted, effectively "restarting" the system.

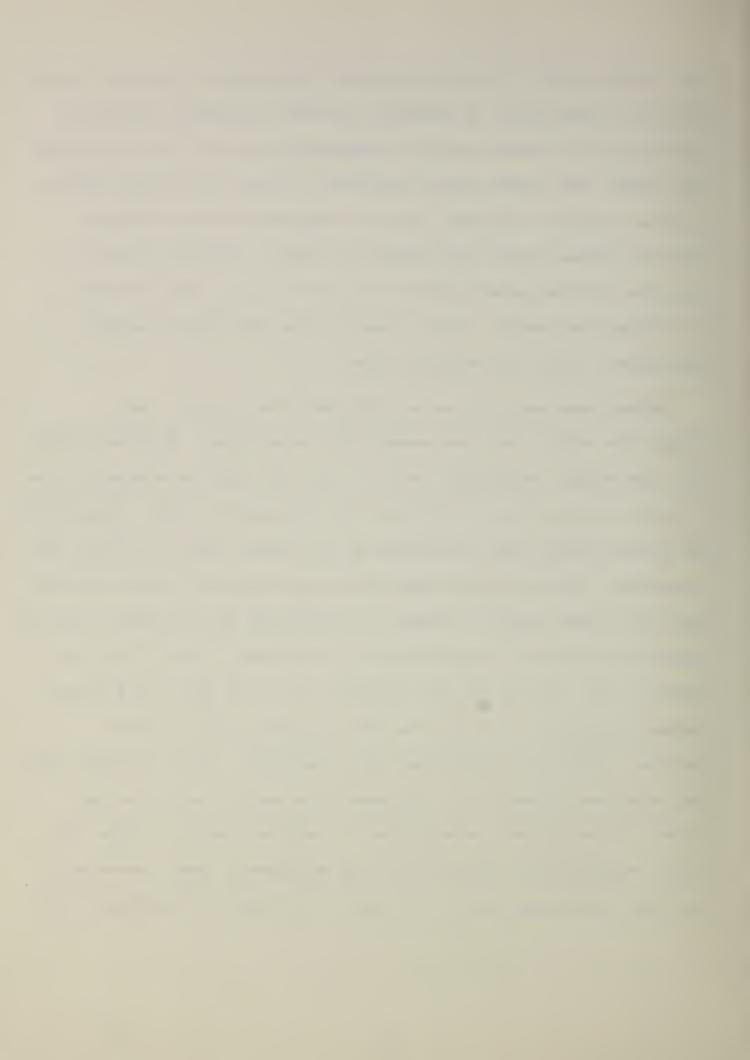
At this point, it seemed clear that relocation was not worth its price (more than doubling the algorithm's computer time). This conclusion was checked once more, in the next set of runs, under more realistic conditions, and was supported by the results: the errors were smaller (at 100 cycles) without relocation.

Parallel efforts by ECOM had meanwhile produced a "best engineering judgment" range-error distribution, which can be adequately modeled as "Gaussian with variance 36 m²; mean 0, except that a random 1% of measurements are inflated by about 7 meters." There will also be occasional extremely large errors; a simple preprocessor can weed most of these out in the field system, by simply checking whether the range measurement is compatible with the last known position and the velocity potential of the user. This error distribution was implemented in the balance of our tests. Also implemented were moving boundaries, which can be set to advance at a speed appropriate for foot-soldiers; any motorized unit which reaches the boundary will be reflected off it, so that the motorized units do not stray far from the foot units. Additional features implemented at this time were: a moving/stopped indicator; calculation of weights which reflect the estimated accuracy of a user's estimated position; the ability to choose as locators those users with greatest weights, or those which have been stopped



for a certain number of location-operations; improvement of estimates for the positions of fixed users, by combining successive estimates; a functional representation of terrain; use of an independent measure of the z-coordinate (the height), with random errors; algorithms to reduce slant-range distances to planar (xy-plane) distances, using the independent measure of height difference between locator and locatee; and tests to determine whether a particular location-operation should be treated by slant-range reduction or by a 3-dimensional method. Again, these features were used in various combinations for the runs recounted below.

Before these remaining runs are described, the rational used to "weight" the various range measurements will be explained. No claim is made that these weights are optimal, but it is felt that they are reasonably close to the best values, which is sufficient for a feasibility study. Suppose half the locators had the same x-coordinate as the locatee, and half had the same y-coordinate. Then (assuming ranges to be large relative to range errors)the first half of the locators is useless in determining the x-coordinate, and the second half is useless in determining the y-coordinate. Thus if there are n locators, n/2 are used for each coordinate, and so we have n/2 estimates (assumed independent) of each of the two coordinates of the locatee's position. Consider for definiteness the x-coordinate. If the locators' position errors are unbiased (i.e., have mean value equal to zero), the best estimate of the locatee's x-coordinate is a weighted average of these n/2 values: weighted by the reciprocals of the variances of these observations. Since the observational error is the sum of the locator's x-coordinate error



and the range measurement error, its variance is the sum of the position error variance (determined when the locator was last located) and the measurement error variance ($=36~\text{m}^2$). Thus one can calculate an estimate of the x-coordinate error variance, which in turn is used to calculate the weight for this user when he serves as a locator.

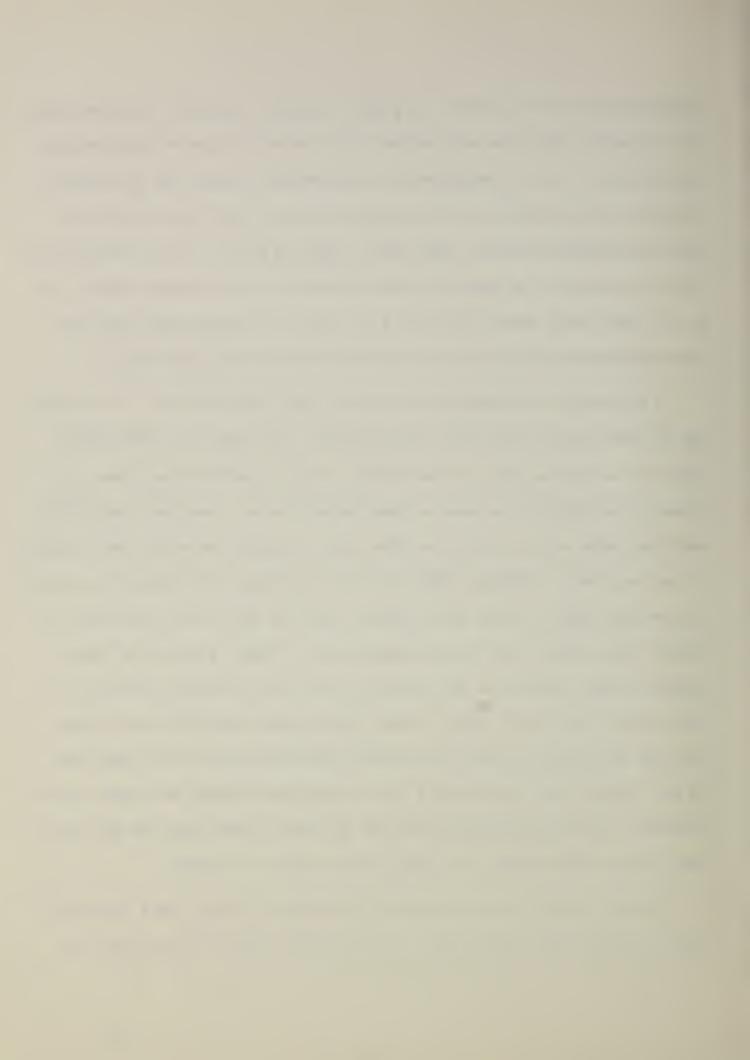
[There are two considerations which should be mentioned here. First, locators are not in general split so nicely along perpendicular lines. Does this matter? Of course it does, in the following sense: if more locators serve to estimate x than y, then x is likely to be better known - i.e., to have smaller variance - and y will be less well known. On the average, however, things even out: if azimuths (from locatee to locators) are uniformly distributed from 0 to 360°, the average (or expected) variance in a given direction turns out to be the value derived above. The second consideration is: What if the estimated variances for the locators are wrong? consequences follow: (a) To the extent that the variances are different multiples of the assumed values, the estimate of position is less than optimum (because the true relative variances should be used to get the estimate); and to the extent that the variances are (as a group) larger (or smaller) than assumed, the estimated variance of the locatee's position will be too small (or large, respectively). Point (a) is not likely to be important, since it would take very large discrepancies to affect the estimate noticeably. Point (b), on the other hand, should at least be investigated. One technique is to act as though the true variances are proportional to the estimated values, with an unknown constant of proportionality (say c) . Then $\, c \,$ can be estimated, and used to produce a fair variance estimate. Specifically, if each



range observation has variance $c\sigma_{\bf i}^2$ ($\sigma_{\bf i}^2$ = location variance + range measurement variance), then the best estimate for the locatee can be found without considering c. If $d_{\bf i}$ represents the discrepancy between the calculated range from this position to the assumed position of the i-th locator and the corresponding measured range, then $\left[\frac{1}{n-2}\sum d_{\bf i}^2/\sigma_{\bf i}^2\right]$ is the (multiplicative) correction to be applied to the variance estimate already given. (If $c \sim 1$, this value should also be ~ 1 .) This is a recent result and the corresponding modification has not yet been made to the algorithms.]

A new series of 2-dimensional runs was done, with 30 users. An initial set of fixed users (reporters) was specified. From then on, units became reporters as soon as they had been fixed for ten location—operations, and ceased to be reporters as soon as they began to move. Average times moving and fixed were set at 15 min., so that about 15 (half the units) were stopped at any one time. A 2½-hour (300 cycle) run was done, and resulted in an overall average error of 3.2m, and a maximum error of 35m; in the last set of 5 cycles, the average was 3.5m, the maximum 11m. Next, a run using longer cycles (90 sec. instead of 30) produced errors of 3.8 and 50.5 overall, 5.7 and 33.8 for the last 5 cycles. Next, the average times fixed and moving were set at 45 min. and this run repeated (because with 15 min. times and 1½ min. cycles, many units didn't stay stopped long enough to be much use as locators). The error figures then came back down toward those of the first run: 3.4 and 33.3 overall, 5.9 and 22.5 for the last 5 cycles.

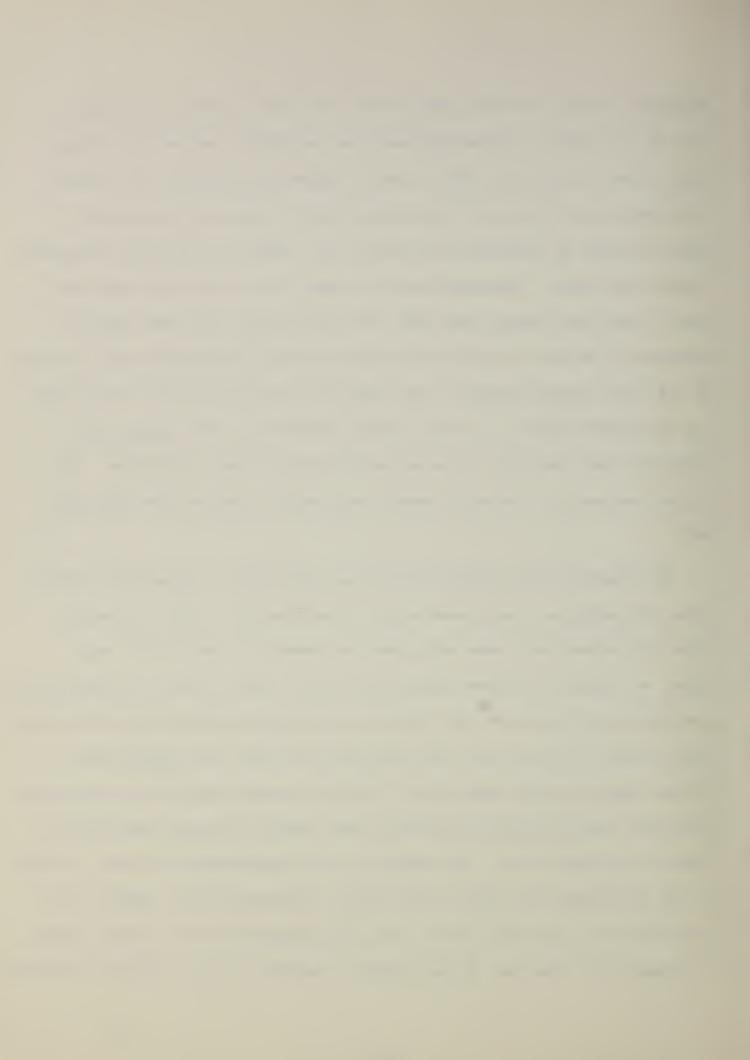
At this point, the cycle time was returned to 30 sec., and a relocation run was tried, with fraction 0.2. It did poorly: errors 5.8 average and



35 maximum overall, with 8.4 and 17.5 for the last 5 cycles. All errors were in one quadrant, indicating that some instability had been introduced.

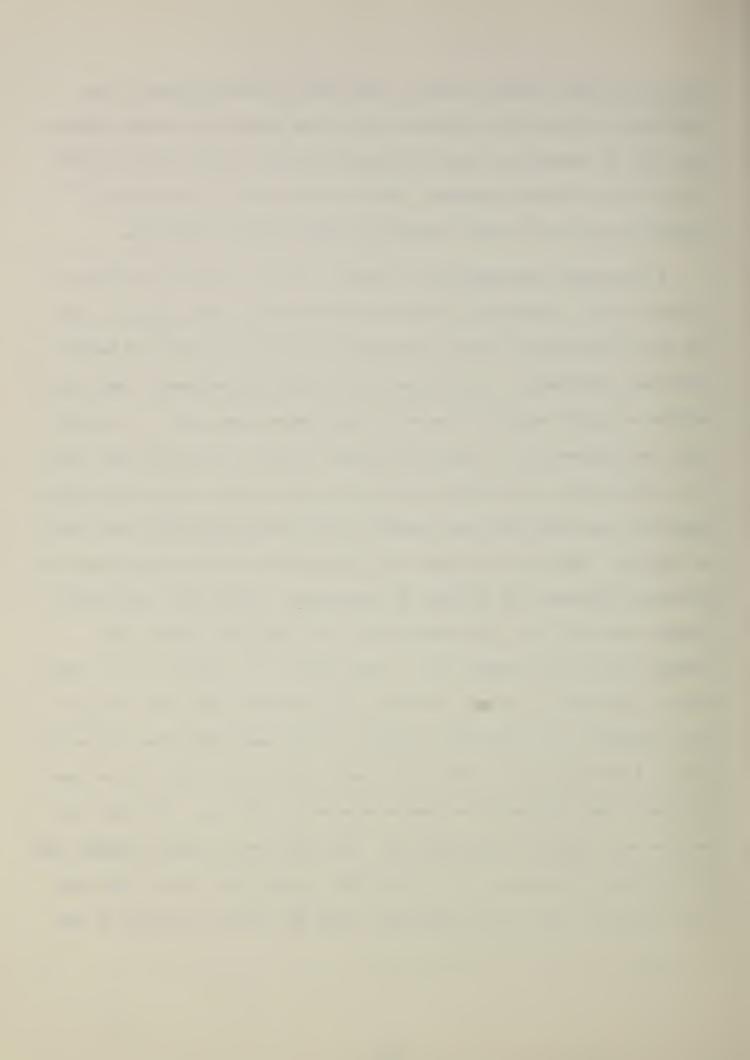
Next, a run with fraction .001 was done. Since this fraction is so small, the magnitudes of the actual relocations will be essentially negligible; thus the effect of relocation in this run is simply to allow more iterations for the algorithms. (Remember that the number of iterations has been kept small to keep the running time down, with the thought that range errors of the order of 6m don't justify too much precision in locating the true solution of the least squares problem.) Only 100 cycles were done, with results equal (up to roundoff effects) to those without relocation. This supports the conclusion that generally, it is not worth doing too many iterations. (Of course, how many is "too many" depends very much on how good the algorithm is!)

The algorithm was modified to treat aircraft with a 3-dimensional method, while continuing to treat ground units 2-dimensionally. (This is possible since only ground units were being used as locators.) Ten aircraft were added, at (random) altitudes ranging from 128 to 2220m. That low-flying aircraft presented a problem became very obvious, since the algorithm located them where they belonged at some times, near the ground at others, and below ground (mirror image) at still other times. One more attempt was made in this series, using only ranges that were at most 10 times height, to ensure that not all lines of sight were flat. This helped for the second-lowest aircraft, at 339m: it had an average (x,y) error of 19m, with a maximum of 113m. However, the lowest aircraft generally did not have enough acceptable(short enough) ranges to estimate its location. It was decided, therefore, to do a separate systematic



study of aircraft location errors. This will be discussed below. The conclusion is already clear, however, that some independent height information will be required to locate low-flying aircraft, unless other aircraft are serving as locators: however, the use of aircraft as locators will probably require very stable aircraft and good tracking techniques.

A functional representation of terrain - i.e., z = f(x,y), with f(x,y)chosen to give a reasonable surface-was implemented at this stage, to test the use of independent pressure references (p.r.'s) as a source of heightdifference information. After consultation with AMCA personnel, these were modeled as giving height with an error that had zero mean and $\sigma = 14m$ (so that the difference of 2 heights will have $\sigma = 20m$). 40 units were used, on a terrain that varied 200m in elevation, with 15 units stopped initially; again only units that had been stopped for 10 location-operations were used as locators. The x,y coordinates were obtained by reducing slant ranges to horizontal distances and applying 2d algorithms. In 2½ hours, the overall average error was 3.5m, the maximum 29.2; for the last 5 cycles, the average was 4.8, the maximum 13.7. Next the p.r. σ was set to 0, with results identical to another run where the terrain was flat and no heights were considered. For extraneous reasons, it only went 260 cycles instead of 300; it had errors of 3.2 (avg), 28.2 (max) overall; 3.3, 14.6 for the last 5 cycles. Next, the height estimates were set at 0: i.e., the hills and valleys were ignored by the algorithm. The errors were slightly smaller than the ordinary run using p.r.'s: 3.35 and 28.2 overall, 4.4 and 14.3 for the last 5 cycles. This is not surprising, since the errors introduced by the

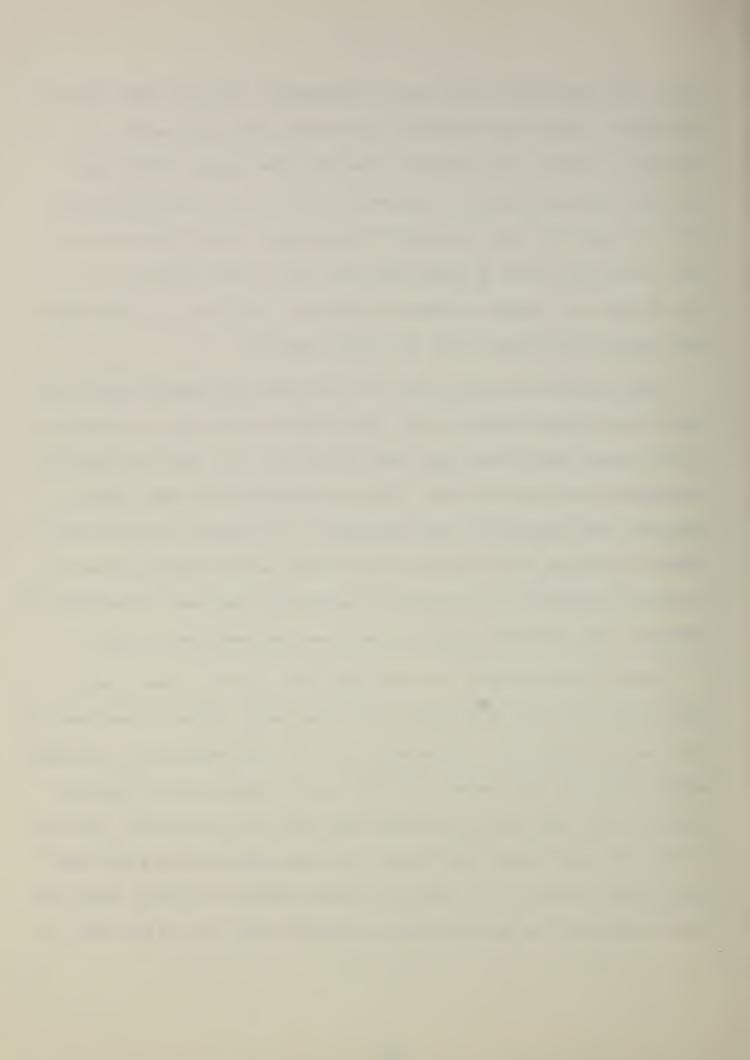


p.r.'s are comparable to the terrain differences. If p.r.'s don't perform any better, perhaps they should be ignored when only ground units are concerned. However, in particular situations, the terrain heights may introduce systematic errors if ignored, which may then propagate; the p.r. errors at least have the advantage of being random. More investigation of this possibility should be undertaken when more is known about p.r.'s.

For the next run, terrain roughness was tripled: with the p.r.'s the errors were essentially the same as on the flatter terrain.

Only two sets of runs are yet to be described: the aircraft error study and the runs on the Boston terrain. The Boston scenario had no aircraft, so it was treated using slant-range reduction with p.r.'s. Two runs using the 1st Brigade constitute the final trials: one with only the fixed users reporting, and one with all units reporting. In preliminary trials, the effect of dropping those reporters which are in another brigade was seen to be minimal, except for a few front-line users which had severe intervisibility problems. The errors for the two primary runs are summarized in Table 1.

Several points deserve to be mentioned with regard to these results. It will be noted that for 30 of the 44 units, the average error is less when all units serve as reporters. Furthermore, in 10 of the remaining 14, the higher average using all units seems to be due to poor estimates where otherwise (with only the fixed units reporting) there would be no estimates. For most of the units with maximum error above 20m, those maxima occurred with less than 2 fixed locators (i.e., where no estimate would be available using only fixed locators). The greatest error occurred for unit 28, and was 108m; it

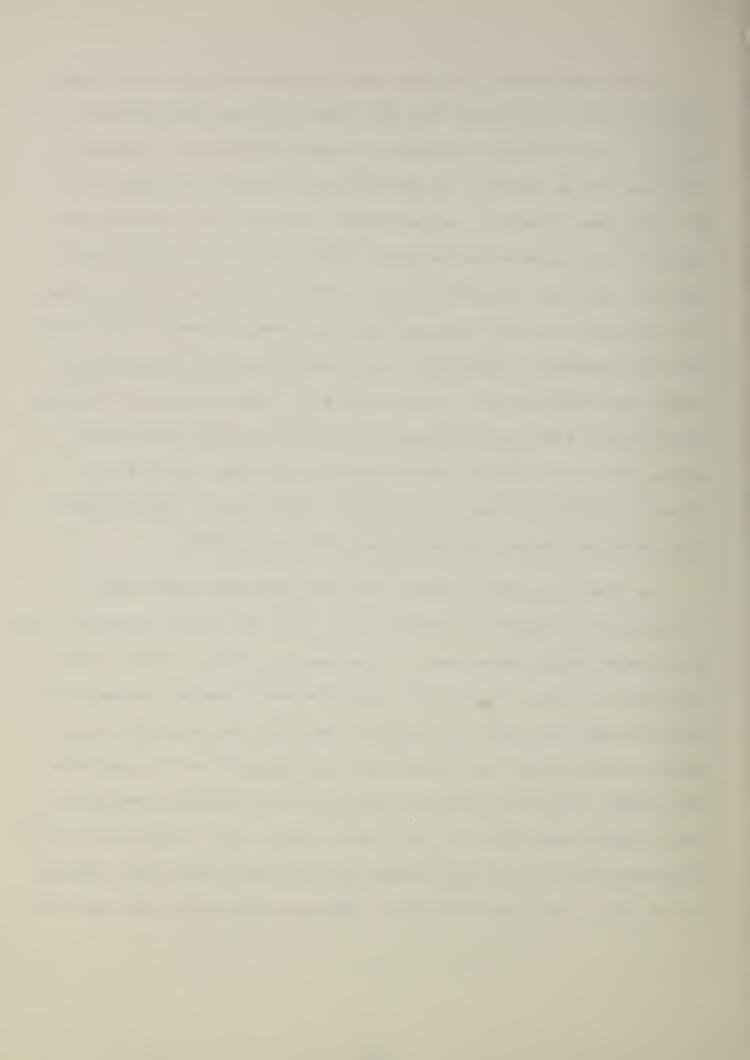


(as well as the two unsuccessful location-operations for this unit) involved 21 locators, including 2 fixed locators. (It is interesting to note that relatively large errors will occasionally occur even with a system " in control.") Using only the fixed locators, that unit never got lost and never had an error greater than 18m. This anomalous behavior suggests that perhaps one should use only the ranges from fixed units, if there are enough, and should use at most a small number of ranges from moving units in any case. Also worthy of note is the fact that apart from this unit, every other maximum error greater than 31m occurred with 4 or fewer locators.



As mentioned earlier, it became obvious very quickly that low-flying aircraft could not be tracked from the ground. To study the effects on accuracy of such variables as number of locators and height, a separate study was done on aircraft. 20 reporters were randomly positioned on a 10 × 10km piece of terrain, and kept fixed. (See Fig. 1.) Ten(simulated) aircraft were started at the southwest corner, at altituted of 100, 250, 400, 550, 700, 1000, 1500,2000, 2500, and 3500m. Each flew a level course, with constant x-velocity; the course reflected several times off both north and south boundaries, terminating at the eastern boundary, systematically covering the entire terrain. (Shown on Fig. 1.) Each aircraft went through either 1230 or 2790 location-operations. The average error and average squared error were tabulated, both in the x,y-directions and in z, by number of locators, for each aircraft (i.e., each height). These tabulations were then studied, and regression techniques applied.

The first run counted locators for which the range was less than 8 × height, 12 × height, 16 × height, etc., up to 80 × height, stopping as soon as 4 or more locators were found. It then used LSS (3d). Table 2 shows the numbers of trials for which the algorithm was and was not successful by aircraft height and number of locators. There are few cases where an aircraft at 700m or higher was not located, but things are not too good below that height. The error statistics bore this out; the maximum z-errors for the 10 aircraft were 1880, 192, 97, 83, 39, 22, 14, 15, 16, 19m (in order of increasing height), while the maximum x,y-errors were 26339, 2373, 337,600, 72, 36, 29, 23, 27, 18m respectively. Since 3d obviously does not work with



low-flying aircraft, an examination was made of the dependence of average error on number of locators and height, for aircraft heights of 550m and above. Regression analyses showed that the average x,y-error could be represented adequately by the expression $\overline{E}_{x,y} = 16 - .9n - \frac{2500}{alt} + .017n^2$, and average z-error by $\overline{E}_z = 31 - 3n + .08 n^2$, where n is the number of locators used. (Note that these expressions were developed for aircraft higher than about 500m.) The values given by these expressions agree with the values obtained in the experiment within an average deviation of 0.5m for x,y-error, and 2m for z-error. (The experiment values for x,y-error ranged from 3 to 10m; for z-error, from 4 to 29m .)

Finally, a similar run was done using slant range reduction, with aircraft at 100, 250, 400, and 550m altitudes, using p.r.'s, and only those reporters with elevation angles < 20°. The average x,y-errors were 3.2, 3.3, 3.4, and 3.7m respectively; the maxima were 15, 15, 15, and 17m respectively. This suggests that one should use slant range reduction up to at least 600m, and use LSS 3-d or slant range reduction above that value depending on whether there are many good ranges at large elevation angles or many at small elevation angles, and on the quality of altitude information available at different heights. (It is understood that p.r.'s of the accuracy contemplated herein are limited in altitute, but will cover at least 0 to 600m.)

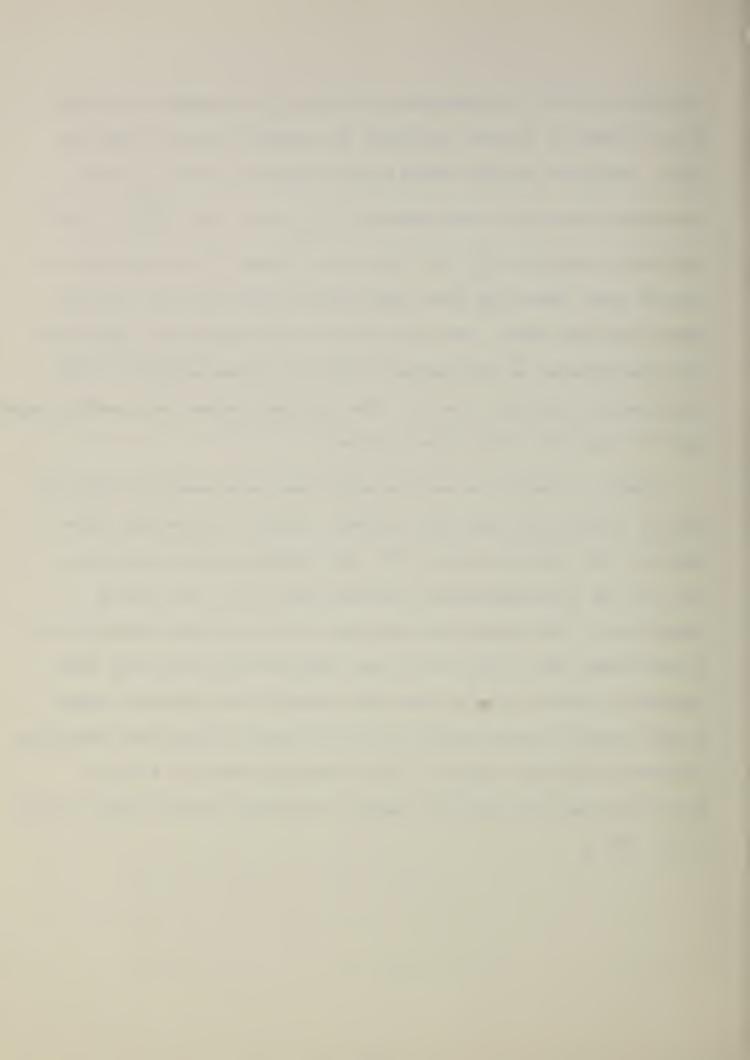


Table 1
Error summaries, Boston runs.

	All reporting		Fixed units reporting				
Unit no.	Errors (m)	No. of times	Errors (m) No. of times				
onit no.	Average Max.	not found	Average Max.	not found			
7	3.8 16.8	19	5.0 21.7				
8	5.9 39.8		7.5 33.4	105			
9	8.6 62.1		7.0 39.6	77			
10	3.7 12.0		. 5.9 20.2				
11	3.4 9.3	20	5.1 22.2				
12	4.2 16.8		4.7 14.2				
13 .	3.7 11.2	104	5.7 21.1	104			
14	3.5 10.0	·	6.8 32.4				
15	3.7 18.7		4.8 18.5				
16	3.7 23.5	1	4.8 16.6				
17	5.1 27.0	. •	5.1 25.4				
18	4.9 20.4		5.3 29.5				
19	5.0 18.0		5.1 23.3				
20	3.9 15.4		5.8 30.7				
24	3.6 24.1		4.3 25.8				
25	4.3 13.3		5.0 16.3	73			
26	2.9 10.0		4.1 11.8	1 '3			
27	3.4 10.1		4.6 21.9				
28	6.3 108.1	2	4.5 17.7				
29	3.4 10.9		3.4 15.0				
30	5.9 51.6		4.3 12.9	79			
31	7.7 79.9	8	4.2 12.3	61			
32	3.7 14.1		5.1 33.9				
33	3.3 12.2		3.6 12.5				
34	3.7 12.5	•	3.5 · 20.4 ·				
35	3.2 11.4	1 .	3.4 10.5				
36	3.6 11.1	1	3.1 12.8				
37	3.6 11.6		3.3 13.4				
38	2.7 10.1		3.4 10.7				
42	3.9 12.8		3.4 8.5	102			
43	3.6 10.9	67	4.5 16.8	67			
. 44							
45	5.7 54.8	3	4.3 12.9 4.7 12.5	57 60			
45	4.9 23.6		l .	69 67			
46	3.5 13.8 9.4 101.3		I .	67 55			
47 48			4.0 11.9 4.4 14.2	55 77			
46		. 3 .	4.4 14.2	77 2			
50	3.9 .12.8 8.3 88.3	2	•	1			
		,		30 <u>.</u> 20			
51				20			
52 . 53	3.7 14.4 3.8 13.5		. 5.2 17.5 4.7 23.1	77			
54 54	3.8 13.1		4.6 25.9	105			
55	3.9 17.2		5.4 25.5	10)			
56	4.2 16.4		5.7 22.0				
All	4.5 108.1		4.7 39.6				
NII.	4.7 100.1		4.1 33.0				
	<u> </u>	l	L	L			



Table 2.

Lost and found summary aircraft study

Aircraft height

Number of Locators	100	250	400	550	700	1000	1500	2000	2500	3500
3	4/0									
. 4	136/640	84/396	44/175	. 18/80 -	7/52					•
5	40/255	48/233	28/189	18/92	3/20					
6	18/98	18/163	8/131 ·	9/103	0/11					
7	7/24	14/98	22/192	16/128	4/32	0/1				
8 .	1/5	6/57	4/122	2/119	0794	0/2				
9	0/2	6/83	3/189	5/159	1/57	0/1				
10		1/22	2/95	1/115	1/7.0	0/3	•			
11		0/1	0/16	0/85	1/98	0/0				
12			0/10	0/94	1/130	1/28				
13				0/90	0/44 ·	0/13				
14				0/70	0/65	0/36				
15				0/16	2/228	0/184				
16				0/10	0/133	0/154				
17					0/44	0/212				
18		•			0/33	0/23i				
19						0/232	0/67			
20						0/132	1/1162	2/1228	0/1230	0/1230
٠.		•								
Total Lost	206	177	111	69	19	1	. 1	2	0	0



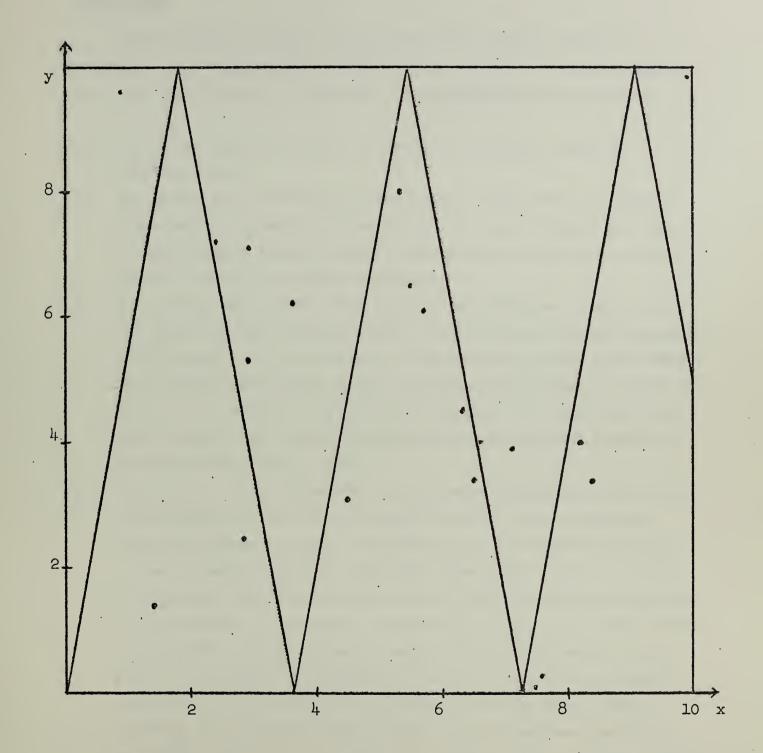


Fig. 1
Locators' positions and aircraft path, Aircraft error study.



4. Conclusions

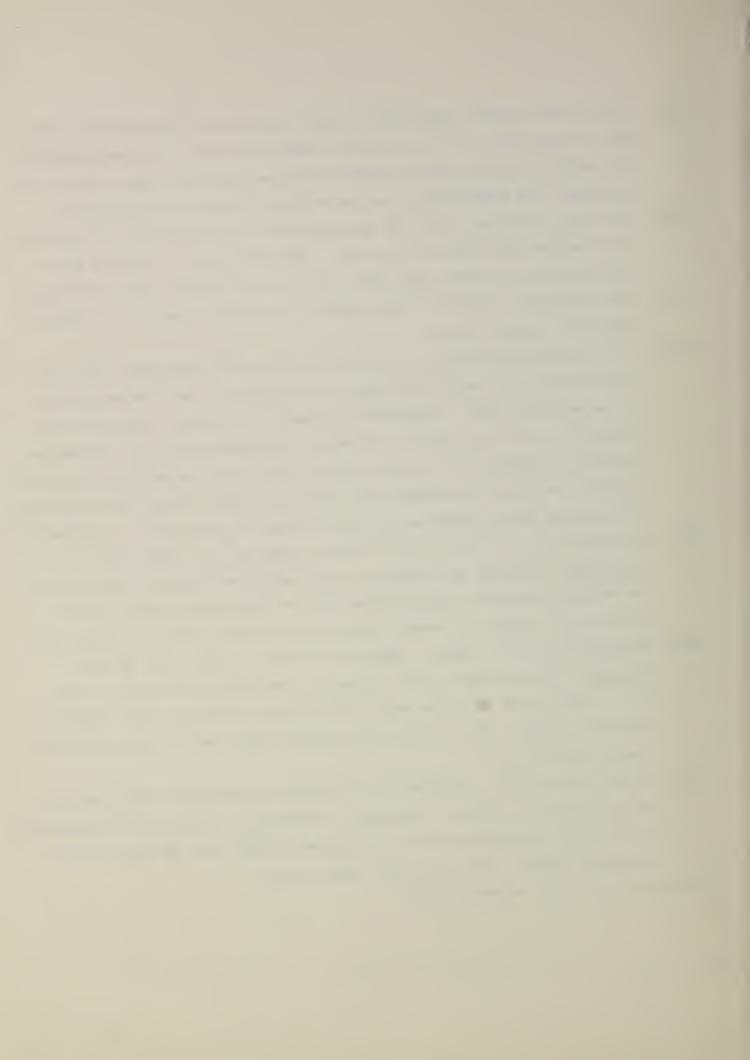
The following represent conclusions with varying degrees of certainty; some only say what might be true, or what should be checked out. They are organized to parallel the earlier list of questions.

- (1) The system will work under reasonable conditions, such as outlined below.
- (2) The system will generally locate ground units within reasonable error bounds whenever such units have at least 4 fixed locators or well-located moving locators (which may be airplanes, as long as they are not too nearly overhead).
- (3) x, y-errors will be the same order of magnitude as range errors, for about 4-6 good locators; the accuracy (error) should improve as $1/\sqrt{n-2}$ where n is the number of locators, up to the point where the computer word length begins to limit the algorithm's accuracy. The z-errors will be comparable for genuine 3-d situations; they will depend solely on the accuracy of the independent pressure reference when that is used.
- Use LSS; to find a starting value when extrapolation from previous estimates is not to be trusted, use LSL. Use an outlier rejection scheme in each, in addition to a preliminary screening of the incoming ranges to eliminate gross (10%) errors. Use the 2-dimensional version on ground units, with slant-range reduction if the terrain is not smooth (unless all but 1 or 2 of the locators are aircraft at high elevation angles, say 60° or more, in which case 3-d treatment is required); also use 2-d with slant-range reduction for aircraft with altitudes less than about 1000m, possibly in conjunction with 3d for aircraft between (say) 600 and 1000m. Use 3d for aircraft over 1000m. (Note: These numbers depend on the spread of ground units; the values given are appropriate for the Boston deployment.)



- (5) Fixed units should constitute a large fraction (at least 1/2) of the set of reporters. The system will work with fewer, but the possibility exists that the set of users' estimated positions will "break its moorings" and wander away, as one entity, from the true position.
- (6) It is <u>not</u> necessary that the same units be fixed throughout the period of time that the system is in use. (In which case it follows that the positions in which they stop will not be "known", only estimated.)
- (7) This question, concerning the number of reporters needed, is answered under (3) and (4) above.
- (8) It is understood that maps will not be generally available, but this is fortunate in a way, since their use extracts a very heavy penalty in computation time. Altimeters (or more accurately, "pressure references", or p.r.'s) will be necessary when aircraft at low elevation angles are working with ground units, either as locatee or as locators, and will be helpful whenever the terrain is rough enough that altitude differences among ground units are as large as the error σ of the p.r.
- (9) An accuracy of 14m (σ) in p.r. values (that is, σ = 20m for the difference between the heights of two units) will enable the system to maintain position errors comparable to range-measurement errors. Better p.r.'s will of course permit more accurate position estimates.
- (10) Reporting once per 30sec. seems reasonable, except: a) Moving

 locators should report more frequently, especially aircraft; and
 b) if the system is to be used for aircraft guidance, close support,
 or fire control, then all aircraft should report more often, say once
 every second or two.
- (11) To use genuine 3d, a minimum of 3 locators is required; only one need be an aircraft. However, at least 5 (including 2 aircraft) is advisable, so that bad measurements may be detected. Note that aircraft at low elevation angles count as ground units here.
- (12) and (13) See answer to (4).



- (14) Use as many locators as possible, but properly weighted.
- (15) Weight fixed, well-known locators considerably higher than others.

 (See discussion of weights earlier in this section.)
- (16) Continual relocation is not advisable. Periodic relocation may be worthwhile; compare with (19) below.
- (17) Do not use only fixed units as reporters, except in situations with unusually good intervisibility. (There are too many times when a unit won't have enough fixed locators.)
- (18) There are indications that relatively large errors will occur when a locator begins to move, if the system continues to treat his position as fixed. Also, whatever time it takes to establish that a unit has stopped becomes a delay in "fixing" that unit's position so that he can become a good locator. Therefore a definite penalty is attached to not having a moving/stopped indicator. The size of this penalty can only be established after the appropriate filtering techniques are implemented. Thus a complete answer awaits a development study.
- (19) Indications are that it is possible to resurvey the set of fixed units. In the course of system development, attention should be paid to developing, implementing, and testing a multivariable least-squares approach, allowing the adjustment of all but a few of the fixed reporters' position estimates simultaneously. This technique would be applied periodically during long battles, when the set of currently-fixed reporters becomes considerably different from the set of initially-fixed reporters. (This technique might be either a supplement to, or a replacement for, the periodic use of relocation; see (16) above.)



Appendix



PROJECT "WHERE" : WORKING PAPER NO. 6

ERROR PROPAGATION FOR ONE-DIMENSIONAL LOCATION OF TWO UNITS

M.H. Pearl

March , 1972

ABSTRACT

The analysis of error propagation for position location in a one-dimensional geometry, assuming Gaussian error distributions and maximum-likelihood estimation (i.e., location by minimizing a particular quadratic penalty function), is mathematically tractable. Although this scenario is unrealistic, "solving" it in closed form may yield insights applicable to more general situations. Working Paper No. 4 developed formulas for the law of error propagation through a single location-operation in such a situation. The present note proceeds to treat a <u>series</u> of location-operations for the (simplest) case where <u>only two units</u> are involved, and shows that in this case the precision of location stabilizes over time. It is planned next to seek to extend this encouraging result to more than two units.

<u>Note</u>: Project working papers are informal documents prepared to facilitate discussion and communication; they may contain tentative or relatively unchecked material.



O. INTRODUCTION

Following the terminology of other papers in this series, we shall use the term <u>location-operation</u> to refer to the process of imputing a position to one unit (the <u>locatee</u>), on the basis of its measured distances from a set of other units (the <u>observers</u>) whose estimated positions are at hand. Both the distance measurements, and the estimates of the observers' locations, are subject to error. The purpose of Project "WHERE" can be roughly described, from a technical viewpoint, as that of determining (for a variety of scenarios) the propagation of location-error over a series of such operations, in which the role of "locatee" varies cyclically among a large set of units, many of which may be in motion during part or all of the series. As a principal tool for this purpose, project staff are developing the various components of a computerized simulation ("WHERESIM").

While such a simulation is needed for the examination of error-propagation in "general" or "unpatterned" situations, it is plausible that valuable insights can be obtained from the study of special situations which are simple enough to admit direct mathematical analysis. Working Paper No. 4⁽¹⁾ initiated one such study, whose key simplifying assumptions are those of

- (a) one-dimensional geometry, and
- (b) Gaussian error distributions.

Specifically, WP4 derived the error-propagation formula under those assumptions for a <u>single</u> location-operation, leaving for a next phase of work the recursive application of this formula to determine error build-up through a <u>sequence</u> of location-operations, with various units serving successively as locatee. The present paper carries out this further analysis for an especially simple situation, that in which <u>only two</u> units are involved. The units thus alternate between the roles of locatee and observer.

Project "WHERE" Working Paper No. 4, Error Propagation for Position Location in One Dimension, M.H. Pearl, December, 1971. To be referred to in what follows as "WP4."

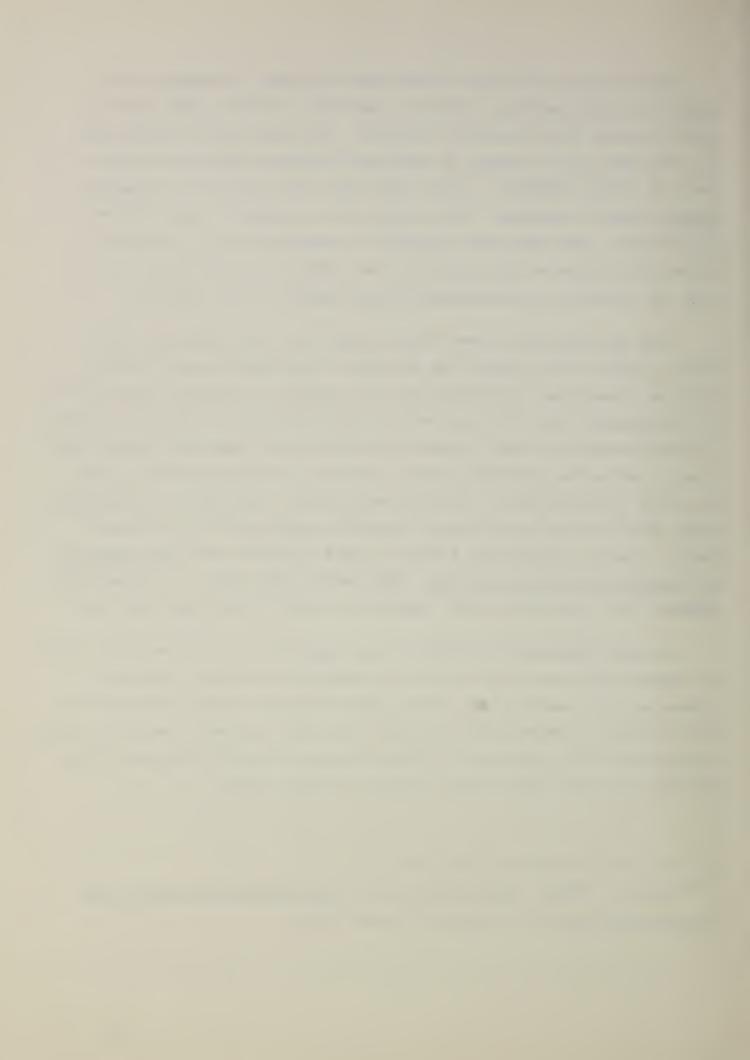


The analysis in WP4 was divided into two cases, according as the single location-operation considered there did or did not make use of a prior estimate of the locatee's position. From the results in WP4 (see its last page) and a variety of additional evidence developed in other parts of Project 'WHERE' , it now seems clear that such prior estimates should indeed be employed, and so their use is assumed in what follows. Specifically, each such prior estimate is obtained from (i) the unit's estimated position at the end of the last previous location-operation and (ii) its velocity of motion(assumed known exactly) in the interim.

With the decision between "prior-using" and "prior-ignoring" thus made in favor of the former, the analysis of the present paper is split into two cases along a different line of cleavage. In Working Paper No.2⁽²⁾, it was suggested that the measurements and calculations taking place during a location-operation might be exploited not only to locate the locatee, but also to revise the currently assumed positions of the observers, so that one would in effect have a "location-and-revision" operation. Accordingly, both "with revision" and "without revision" scenarios will be analyzed below. The most significant finding is that (in both cases) the precision of location stabilizes over time. (The natural next step is to investigate whether this encouraging result combines to hold for more than two units.)

Although familiarity with WP4 is not essential, it will be quite helpful in reading the present text, which is organized as follows. Section 1, appearing next, describes the underlying mathematical models involved and sets up most of the necessary notation. Section 2 presents the error-propagation analysis for a sequence of "location-with-revision" operations, while Section 3 does the same for the "without revision" case.

⁽²⁾ Project "WHERE" Working Paper No. 2, An Iterative Approach to the Location-Operation, A.J. Goldman, October, 1971.



1. MATHEMATICAL FORMULATION

The analysis deals with 2 units located on a line (i.e., the geometry is one-dimensional). The relevant time period begins at time $t_0=0$, and the successive location-operations occur at times t_j (j = 1,2, ...) where

$$0 = t_0 < t_1 < t_2 < \dots$$

For i = 1,2 and j = 0,1,2,..., we set

 $U_{ij} = \text{true position of unit } i \text{ at time } t_{j}$

so that

$$D_{j} = U_{2j} - U_{1j}$$
 (1.1)

= true (signed) distance between

the units at time t .

The U 's are unknown to the location-system, which \underline{is} however "given" at time t quantities,

to be discussed further below. The information on which the j-th location-operation is based consists of u_{1j} , u_{2j} , and

This measurement is assumed unbiased, i.e. $E(D_j) = d_j$, and also normally distributed, so that the random measurement error

$$\delta_{j} = d_{j} - D_{j} \qquad (1.2)$$



is Gaussian and satisfies (for some $\sigma > 0$)

$$E(\delta_{j}) = 0 , E(\delta_{j}^{2}) = \sigma^{2} .$$
 (1.3)

Note that our notation involves σ and not σ_j ; i.e., we assume no systematic change over time in the quality of the distance measurements.

The initial position-estimates, u_{10} and u_{20} , are assumed to be unbiased, i.e. $E(u_{10}) = U_{10}$, and also to be normally distributed; in terms of the vector u_0^T defined by

$$u_0^T = (u_{10}, u_{20})$$
,

we set

$$Q_o = var(u_o) = \begin{bmatrix} var(u_{10}) & cov(u_{10}, u_{20}) \\ cov(u_{10}, u_{20}) & var(u_{20}) \end{bmatrix};$$
 (1.4)

the matrix Q_0 (describing the quality of our starting position-data), as well as σ (which describes the quality of distance measurements), are the basic inputs to our analysis of error propagation.

It is assumed that between t j-1 and t , unit i moves with known velocity $v_{i\,j}$; it therefore covers a known distance

$$\Delta_{ij} = v_{ij}(t_j - t_{j-1})$$
 (1.5)

Thus the prior estimates of the two units' positions, just before the first location-operation, are

$$u_{i1} = u_{i0} + \Delta_{i0}$$
 (i = 1,2);



it follows from (1.4) that

$$Q_{o} = var(u_{1}) , \qquad (1.6)$$

where we have used for j = 1 the notation

$$u_{j}^{T} = (u_{1j}, u_{2j}).$$

Let us define the vector U, by

$$\mathbf{U}_{\mathbf{j}}^{\mathbf{T}} = (\mathbf{U}_{1\mathbf{j}}, \mathbf{U}_{2\mathbf{j}}) .$$

The calculations of the j-th location-operation, in our present model, yield

this estimate is known (cf. WP4) to be unbiased, and we put

$$Q_{j}^{*} = \operatorname{var}(U_{j}^{*}) . \qquad (1.7)$$

It is at this point that the "with revision" and "without revision" cases diverge. In the <u>first</u> case, U_{j}^{*} is accepted as the vector of location estimates after the j-th location-operation; thus Q_{j}^{*} represent the quality of our position locations at time j, so that our aim is to determine these matrices Q_{j}^{*} (and in particular, their behavior as j increases). Moreover, in this case the "next" set of prior estimates is given by

$$u_{j+1} = U_j^* + \Delta_j , \qquad (1.8)$$

where we have defined Δ_{i} by

$$\Delta_{j}^{T} = (\Delta_{1j}, \Delta_{2j}).$$



In the <u>second</u> ("without revision") case, the vector of location estimates after the j-th operation, denoted U_{j}^{**} with components U_{1j}^{**} and U_{2j}^{**} , is taken as

$$U_{1j}^{**} = U_{1j}^{*}$$
, $U_{2j}^{**} = u_{2j}$ if j odd (unit 1 the locatee), (1.9) $U_{1j}^{**} = u_{1j}^{*}$, $U_{2j}^{**} = U_{2j}^{*}$ if j even (unit 2 the locatee),

so that the prior estimate of the observer's position indeed goes unrevised. The "updating" formula (1.8) is of course replaced by

$$u_{j+1} = U_{j}^{**} + \Delta_{j}$$
 (1.10)

And now the matrices

$$Q_{j}^{**} = var(U_{j}^{**})$$
 (1.11)

are the matrices which are to be investigated, and whose limiting behavior (for large j) is to be investigated.

The analyses of the two sequences $\{Q_j^*\}$ and $\{Q_j^{**}\}$ of matrices, are the topics of Section 2 and 3 respectively.



2. ANALYSIS ASSUMING REVISION

It is convenient to define the random error vectors

$$\epsilon_{j} = u_{j} - U_{j}$$
 (2.1)

Then the likelihood function for the first location-operation is

$$L = K \exp\{-\frac{1}{2}(\varepsilon_1^T Q_0^{-1} \varepsilon_1 + \sigma^{-2} \delta_1^2)\}$$

where K is a positive constant, so that maximizing L is equivalent to minimizing

$$L^* = \frac{1}{2} \left(\varepsilon_1^T Q_0^{-1} \varepsilon_1 + \sigma^{-2} \delta_1^2 \right) . \qquad (2.2)$$

From (1.1) and (1.2),

$$\delta_1 = d_1 + [1, -1]U_1$$
,

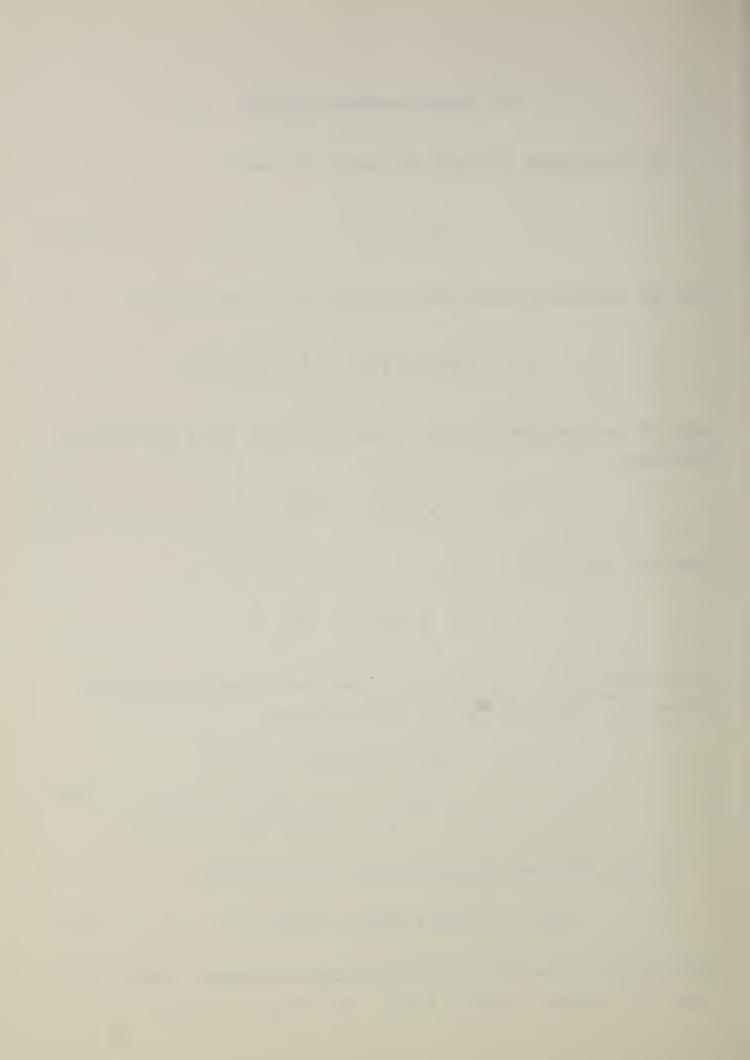
and from this, (2.1), and (2.2), it follows that the maximum-likelihood estimate \mathbf{U}_1^* is the value of \mathbf{U}_1 which minimizes

$$L^* = \frac{1}{2} \{ (u_1 - U_1)^T Q_0^{-1} (u_1 - U_1) + \sigma^{-2} (d_1 + [1,-1] U_1)^T (d_1 + [1,-1] U_1) \}.$$
(2.2a)

We next apply the (straightforwardly verified) formula

$$\partial [(AX + B)^{T} S(AX + B)]/\partial X = 2A^{T}S(AX + B)$$
 (2.3)

where X is a column vector and S is a symmetric matrix. Taking A = I (the 2 X 2 identity matrix), $B = u_1$ and $S = Q_0^{-1}$, we obtain



$$\partial \{u_1 - U_1\}^T Q_0^{-1} (u_1 - U_1)\} / \partial U_1 = 2Q_0^{-1} (U_1 - u_1) ; \qquad (2.4)$$

taking A = [1,-1], $B = d_1$, and S = I, we obtain

$$\partial \{ (d_1 + [1,-1]U_1)^T (d_1 + [1,-1]U_1) \} / \partial U_1 = 2[1,-1]^T (d_1 + [1,-1]U_1)$$

$$= 2\{ [1,-1]^T d_1 + NU_1 \} , \qquad (2.5)$$

where we have put

$$N = \begin{bmatrix} 1,-1 \end{bmatrix}^{T} \begin{bmatrix} 1,-1 \end{bmatrix} = \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix} . \qquad (2.6)$$

Thus the equation $\partial L^*/\partial U_1 = 0$, to be satisfied by $U_1 = U_1^*$, reads

$$Q_0^{-1}(U_1-U_1) + \sigma^{-2}[1,-1] d_1 + \sigma^{-2} NU_1 = 0$$
;

setting

$$H_{o} = \sigma^{-2} Q_{N}$$
 , (2.7)

we see that this is equivalent to

$$(I + H_o)U_1^* = u_1 + \sigma^{-2} Q_o[1,-1] d_1$$

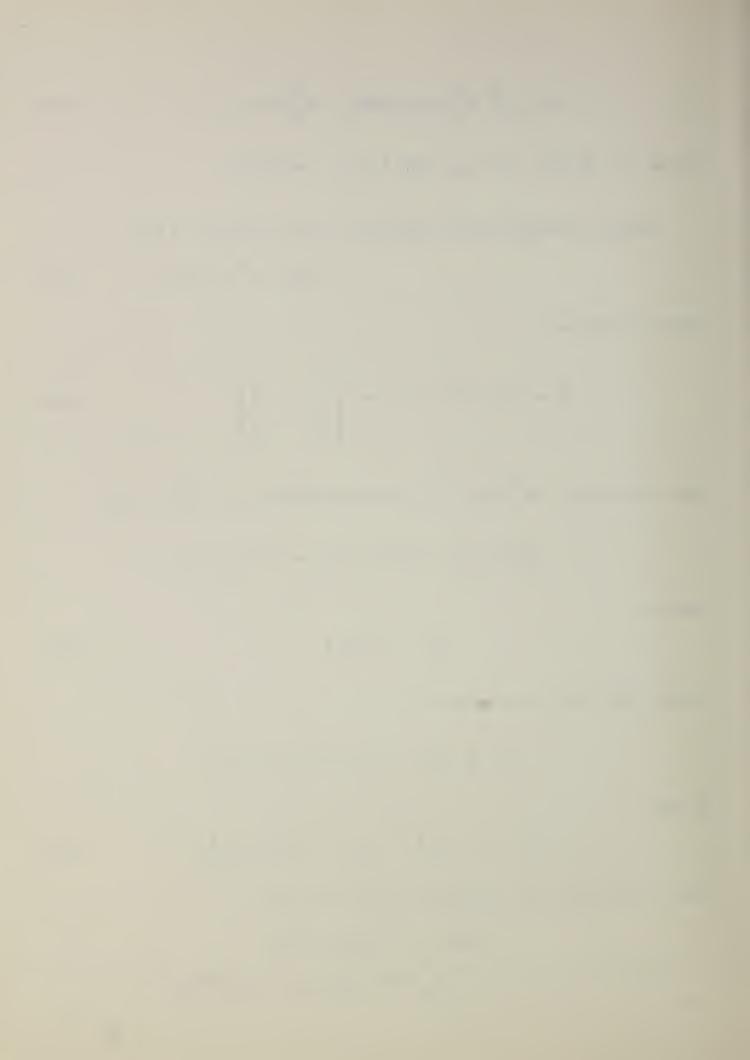
so that

$$U_1^* = (I + H_0)^{-1} (u_1 + \sigma^{-2} Q_0[1,-1] d_1)$$
 (2.8)

Since $cov(u_1, d_1) = 0$, we have by (1.6) and (1.8)

$$var(u_1 + \sigma^{-2} Q_0[1,-1] d_1)$$

$$= Q_0 + \sigma^{-4} Q_0[1,-1] \sigma^2 [1,-1]^T Q_0$$



$$\partial \{u_1 - U_1\}^T Q_0^{-1} (u_1 - U_1)\} / \partial U_1 = 2Q_0^{-1} (U_1 - u_1);$$
 (2.4)

taking A = [1,-1], $B = d_1$, and S = I, we obtain

$$\partial \{ (d_1 + [1,-1]U_1)^T (d_1 + [1,-1]U_1) \} / \partial U_1 = 2[1,-1]^T (d_1 + [1,-1]U_1)$$

$$= 2\{ [1,-1]^T d_1 + NU_1 \} , \qquad (2.5)$$

where we have put

$$N = [1,-1]^{T} [1,-1] = \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix} . \qquad (2.6)$$

Thus the equation $\partial L^*/\partial U_1 = 0$, to be satisfied by $U_1 = U_1^*$, reads

$$Q_0^{-1}(U_1-U_1) + \sigma^{-2}[1,-1] d_1 + \sigma^{-2} NU_1 = 0$$
;

setting

$$H_{o} = \sigma^{-2} Q_{o}N \qquad , \qquad (2.7)$$

we see that this is equivalent to

$$(I + H_0)U_1^* = u_1 + \sigma^{-2} Q_0[1,-1] d_1$$

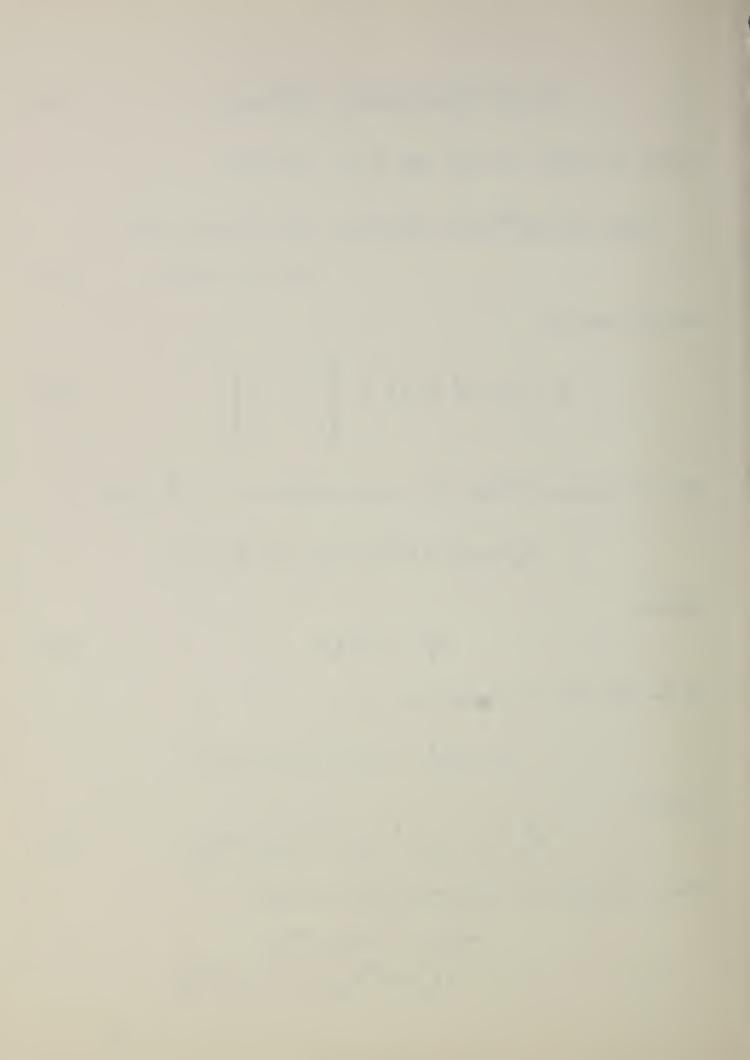
so that

$$U_1^* = (I + H_0)^{-1} (u_1 + \sigma^{-2} Q_0[1,-1] d_1)$$
 (2.8)

Since $cov(u_1, d_1) = 0$, we have by (1.6) and (1.8)

$$var(u_1 + \sigma^{-2} Q_o[1,-1] d_1)$$

$$= Q_o + \sigma^{-4} Q_o[1,-1] \sigma^2 [1,-1]^T Q_o$$



$$= Q_o + \sigma^{-2} Q_o N Q_o = (I + H_o)Q_o. \qquad (2.9)$$

Since (2.8) yields

$$Q_1^* = var(U_1^*)$$

$$= (I + H_0)^{-1} var(u_1 + \sigma^{-2} Q_0[1,-1]d_1)(I + H_0)^{-T},$$

it follows from (2.9) that

$$Q_1^* = Q_0(I + H_0)^{-T}$$
, (2.10)

which is equivalent to

$$Q_1^* = (I + H_0)^{-1}Q_0$$
 (2.11)

We turn now to the second location-operation. By (1.8),

$$var(u_2) = var(U_1^*) = Q_1^*$$
,

i.e. Q_1^* plays the same role now that was played by Q_0 previously. Thus, if by analogy with (2.7) we put

$$H_1^* = \sigma^{-2} Q_1^* N$$
,

then by analogy with (2.10) and (2.11) we will obtain

$$Q_2^* = Q_1^* (I + H_1^*)^{-T} = (I + H_1^*)^{-1} Q_1^*$$
.



More generally, the transition from Q_j^* to Q_{j+1}^{**} is given by the two equations

$$H_{j}^{*} = \sigma^{-2} Q_{j}^{*} N$$
 (2.12)

$$Q_{j+1}^* = Q_j^* (I + H_j^*)^{-T} = (I + H_j^*)^{-1} Q_j^*,$$
 (2.13)

with initial conditions $Q_0^* = Q_0$ and $H_0^* = H_0$.
Using these results, we will prove by induction on j that

$$Q_j^* = (I + jH_0)^{-1} Q_0 = Q_0 (I + jH_0)^{-T}$$
 (2.14)

By (2.11), it is true for j=1. Suppose it is true for some particular value of j; we will prove it correct for j+1. First, by (2.12) and (2.14),

$$H_{i}^{*} = \sigma^{-2}(I + jH_{o})^{-1}Q_{o}N = (I + jH_{o})^{-1}H_{o} = H_{o}(I + jH_{o})^{-1}$$
. (2.15)

If we set

$$z_{i} = (I + H_{i}^{*})^{-1}$$
,

then

$$I = Z_{j}(I + H_{j}^{*}) ,$$

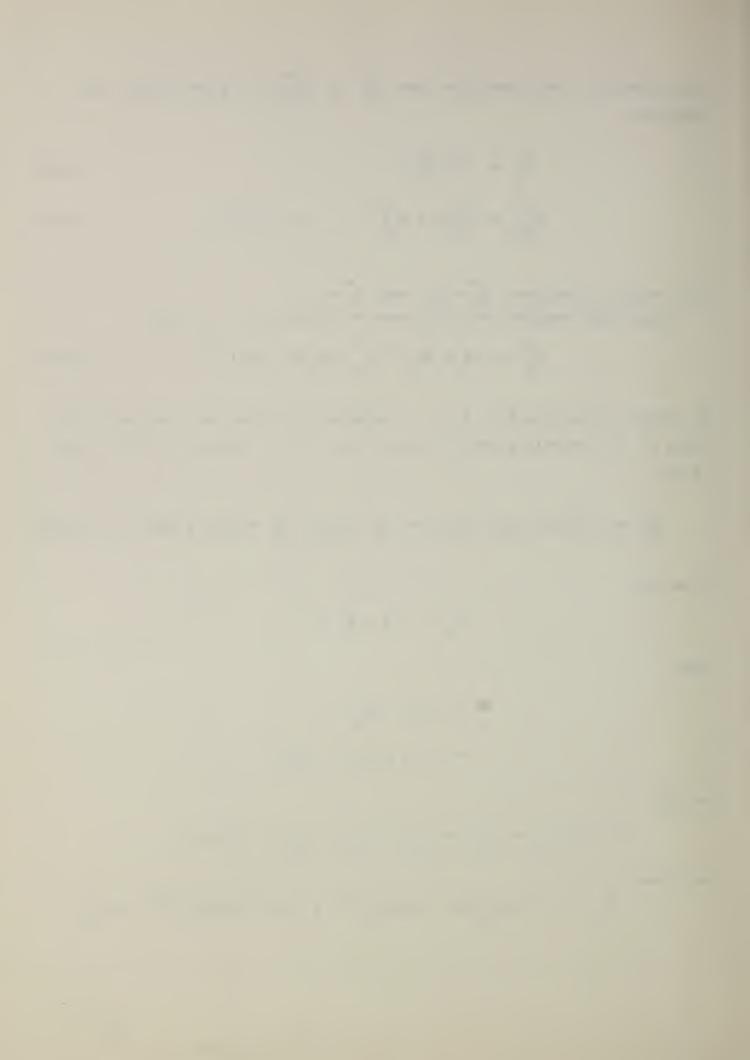
$$= Z_{j} + Z_{j}H_{o}(I + jH_{o})^{-1} ,$$

so that

$$(I + jH_0) = Z_j(I + jH_0) + Z_jH_0 = Z_j[I + (j+1)H_0]$$

and thus

$$Z_{j} = (I + jH_{o})[I + (j+1)H_{o}]^{-1} = [I + (j+1)H_{o}]^{-1}(I + jH_{o});$$



it follows from (2.13 - 15) that

$$Q_{j+1}^{*} = Z_{j}Q_{j}^{*}$$

$$= [I+(j+1)H_{o}]^{-1}[I+jH_{o}][I+jH_{o}]^{-1}Q_{o}$$

$$= [I+(j+1)H_{o}]^{-1}Q_{o},$$

so that (2.14) also applies for j+1. The induction proof is complete.

Note that with (2.6), (2.7) and (2.14), we have succeeded in determining the matrices $Q_{\bm j}^{\bm *}$ explicitly in terms of the basic data Q_o and σ . We now prove that the limit

$$Q_{\infty}^{*} = \lim_{j \to \infty} Q_{j}^{*}$$
 (2.16)

exists, i.e. that the precision of position-location stabilizes over time, and moreover we shall evaluate Q_{∞}^* explicitly.

Let

$$q_0 = \begin{bmatrix} q_1 & q \\ q & q_2 \end{bmatrix}$$
;

then by (2.6 - 7)

$$I + jH_{o} = \begin{bmatrix} 1 + \sigma^{-2}j(q_{1}-q) & \sigma^{-2}j(q-q_{1}) \\ \sigma^{-2}j(q-q_{2}) & 1 + \sigma^{-2}j(q_{2}-q) \end{bmatrix},$$

$$= \sigma^{-2}j \begin{bmatrix} (\sigma^{2}/j) + (q_{1}-q) & q-q_{1} \\ (q-q_{2}) & (\sigma^{2}/j) + (q_{2}-q) \end{bmatrix}. \qquad (2.17)$$



The coefficient of $\sigma^{-2}j$ is a matrix with determinant

$$(\sigma^4/j^2) + (\sigma^2/j)(q_1 + q_2-2q) = (\sigma^2/j)[(\sigma^2/j) + (q_1+q_2-2q)]$$
,

and thus with inverse matrix

$$(\sigma^{2}/j)^{-1} [(\sigma^{2}/j) + (q_{1} + q_{2} - 2q)]^{-1} \begin{bmatrix} (\sigma^{2}/j) + (q_{2} - q) & q_{1} - q \\ q_{2} - q & (\sigma^{2}/j) + (q_{1} - q) \end{bmatrix} .$$

It follows from (2.17) that

$$(\mathbf{I} + \mathbf{j} \mathbf{H}_{o})^{-1} = [(\sigma^{2}/\mathbf{j}) + (\mathbf{q}_{1} + \mathbf{q}_{2} - 2\mathbf{q})]^{-1} \begin{bmatrix} (\sigma^{2}/\mathbf{j}) + (\mathbf{q}_{2} - \mathbf{q}) & \mathbf{q}_{1} - \mathbf{q} \\ \\ \mathbf{q}_{2} - \mathbf{q} & (\sigma^{2}/\mathbf{j}) + (\mathbf{q}_{1} - \mathbf{q}) \end{bmatrix}$$

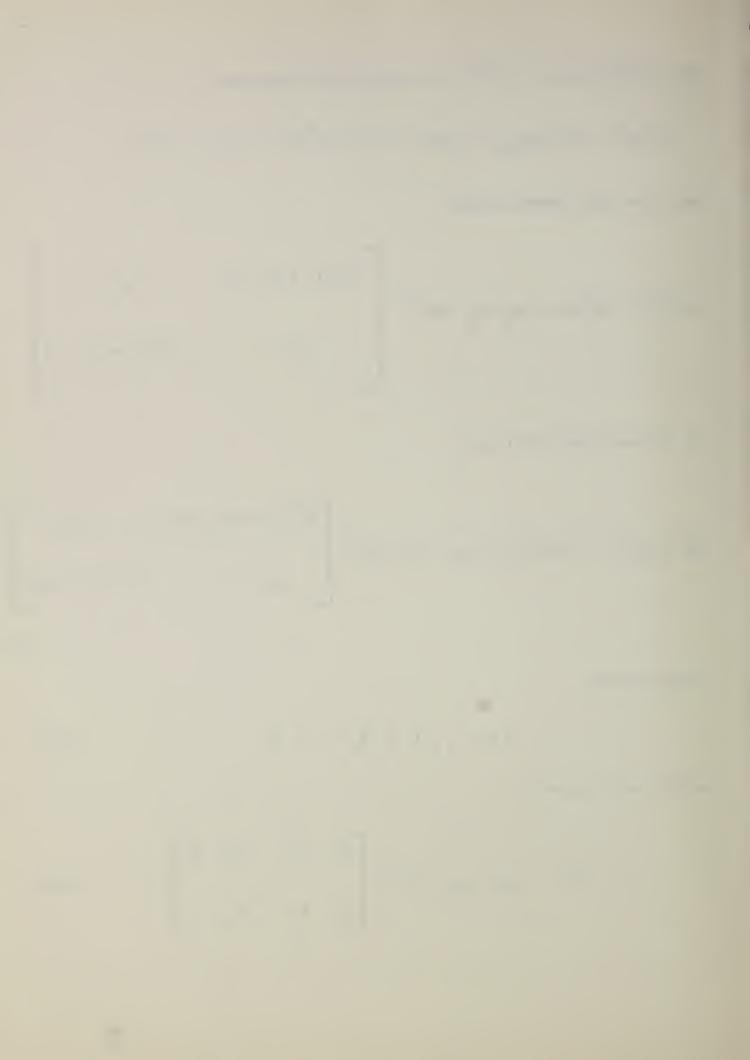
$$(2.18)$$

In particular,

$$\lim_{j \to \infty} (I + jH_0)^{-1} = H^*$$
 (2.19)

exists and is given by

$$H^* = (q_1 + q_2 - 2q)^{-1} \begin{bmatrix} q_2 - q & q_1 - q \\ & & & \\ q_2 - q & q_1 - q \end{bmatrix}; \qquad (2.20)$$



thus by (2.14) the limit Q_{∞}^{*} exists and is given by

$$Q_{\infty}^{*} = H^{*} Q_{O}$$
.
$$= (q_{1}+q_{2}-2q)^{-1} (q_{1}q_{2}-q^{2}) J , \qquad (2.21)$$

where J is a 2 \times 2 matrix of ones. It is somewhat surprising that the limit is independent of σ .

A natural question is whether the position-locations grow increasingly precise over time, i.e. whether the diagonal entries of $Q_j^* = var(U_j^*)$ are decreasing functions of j. By (2.14) and (2.18), the (1,1) entry of Q_j^* is

$$var(U_{1j}^*) = q_1[(\sigma^2/j) + q_1^{-1}(q_1q_2 - q^2)]/[(\sigma^2/j) + (q_1+q_2-2q)]$$
 (2.22)

Now it is readily verified that the function

$$f(x) = (x+a)/(x+b) = 1 - (b-a)/(x+b)$$

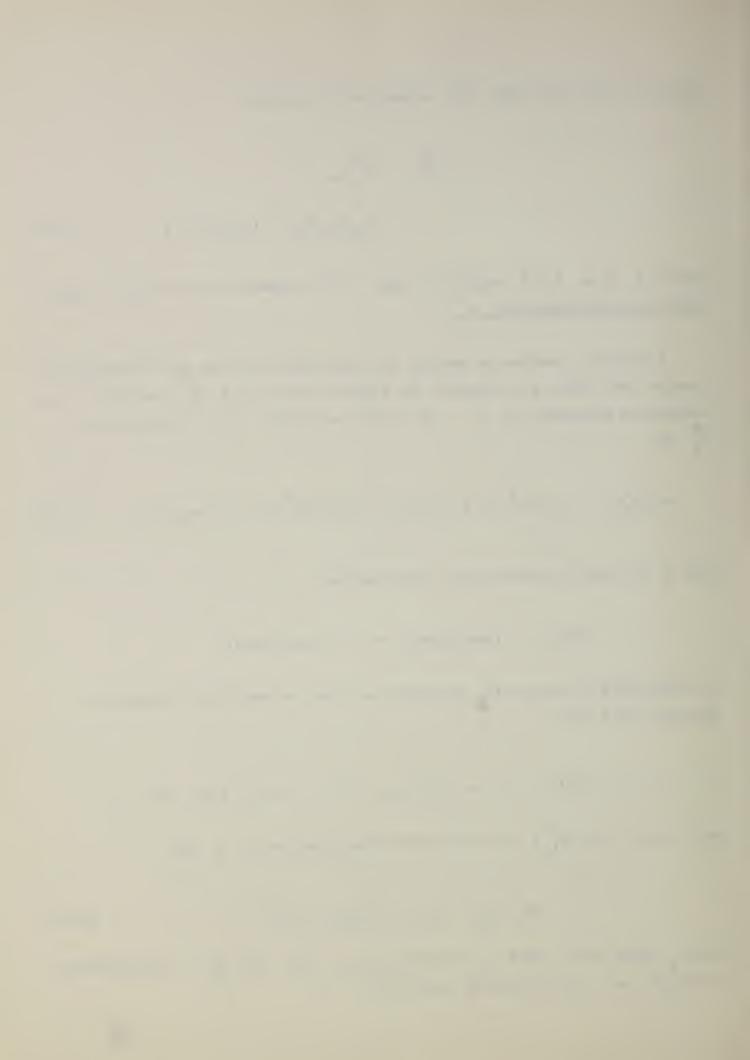
is increasing or decreasing according as (b-a) is positive or negative. Applying this with

$$x = \sigma^2/j$$
, $a = q_1^{-1}(q_1q_2 - q^2)$, $b = q_1 + q_2 - 2q$,

we see that $var(U_{1j}^*)$ is a non-increasing function of j if

$$q_1 + q_2 - 2q \ge q_1^{-1}(q_1q_2 - q^2)$$
, (2.23)

which indeed holds since it is equivalent to $\left(q_1-q\right)^2\geq 0$. Analogously, $\operatorname{var}(U_{2j}^*)$ is a non-increasing function of j.



3. ANALYSIS FOR LOCATION WITHOUT REVISION

We now turn to the matrices

$$Q_{j}^{**} = var(U_{j}^{**})$$
 (3.1)

corresponding to the location-without-revision scenario. The analysis is more complicated here, since the two units no longer figure symmetrically in each location-operation (recall that unit 1 is the locatee in odd-numbered operations, unit 2 the locatee in even-numbered ones).

It is convenient to repeat from Section 2 the definitions

$$N = [1,-1]^{T} [1,-1] = \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix} , \qquad (3.3)$$

$$H_{o} = \sigma^{-2} Q_{o} N$$
, (3.3)

and to introduce the matrices E ; E has entry 1 in the (row i , column k) position, and all other entries zero. Thus, for example, the consequence

$$(\mathbf{U}_{1}^{**})^{\mathrm{T}} = [\mathbf{U}_{11}^{*}, 0]^{\mathrm{T}} + [0,\mathbf{u}_{21}]^{\mathrm{T}}$$

of (1.9) can be written

$$U_1^{**} = E_{11}U_1^* + E_{22}U_1 . (3.4)$$



From this and (3.1) it follows that

$$Q_{1}^{**} = E_{11} \operatorname{var}(U_{1}^{*}) E_{11} + E_{22} \operatorname{var}(u_{1}) E_{22}$$

$$+ E_{11} \operatorname{cov}(U_{1}^{*}, u_{1}) E_{22} + E_{22} \operatorname{cov}(u_{1}, U_{1}^{*}) E_{11} .$$
(3.5)

By (2.8) and (2.11)

$$cov(U_1^*, u_1) = (I + H_0)^{-1}Q_0 = Q_1^*,$$

so that (3.5) yields

$$Q_{1}^{**} = E_{11} Q_{1}^{*} E_{11} + E_{22} Q_{0} E_{22}$$

$$+ E_{11} Q_{1}^{*} E_{22} + E_{22} Q_{1}^{*} E_{11}$$

$$= Q_{1}^{*} + E_{22} (Q_{0} - Q_{1}^{*}) E_{22} .$$

By use of (2.11), this reads

$$Q_1^{**} = (I + H_0)^{-1} Q_0 + E_{22}[I - (I + H_0)^{-1}]Q_0 E_{22}$$
 (3.6)

The second location-operation follows the same logic as the first, except that Q_1^* plays the part of Q_0 and that the roles of the two units are interchanged. Thus, by analogy with (3.3) and (3.6), we have

$$H_1^{**} = \sigma^{-2} Q_1^{**} N , \qquad (3.7)$$

$$Q_2^{**} = (I + H_1^{**})^{-1} Q_1^{**} + E_{11}[I - (I + H_1^{**})^{-1}] Q_1^{**} E_{11} .$$
 (3.8)



More generally, the appropriate recursion equations are

$$H_{j}^{**} = \sigma^{-2} Q_{j}^{**} N$$
 (3.9)

$$Q_{2j+1}^{**} = (I + H_{2j}^{**})^{-1} Q_{2j}^{**} + E_{22}[I - (I + H_{2j}^{**})^{-1}]Q_{2j}^{**} E_{22}$$
, (3.10)

$$Q_{2j+2}^{**} = (I + H_{2j+1}^{**})^{-1} Q_{2j+1}^{**} + E_{11}[I - (I + H_{2j+1}^{**})^{-1}] Q_{2j+1}^{**} E_{11};$$
 (3.11)

these are accompanied by the initial conditions $Q_0^{**} = Q_0$ and $H_0^{**} = H_0$.

In view of the way in which the analysis "alternates" between the two units, it would be unreasonable to expect the type of convergence given by the existence of a single limiting matrix

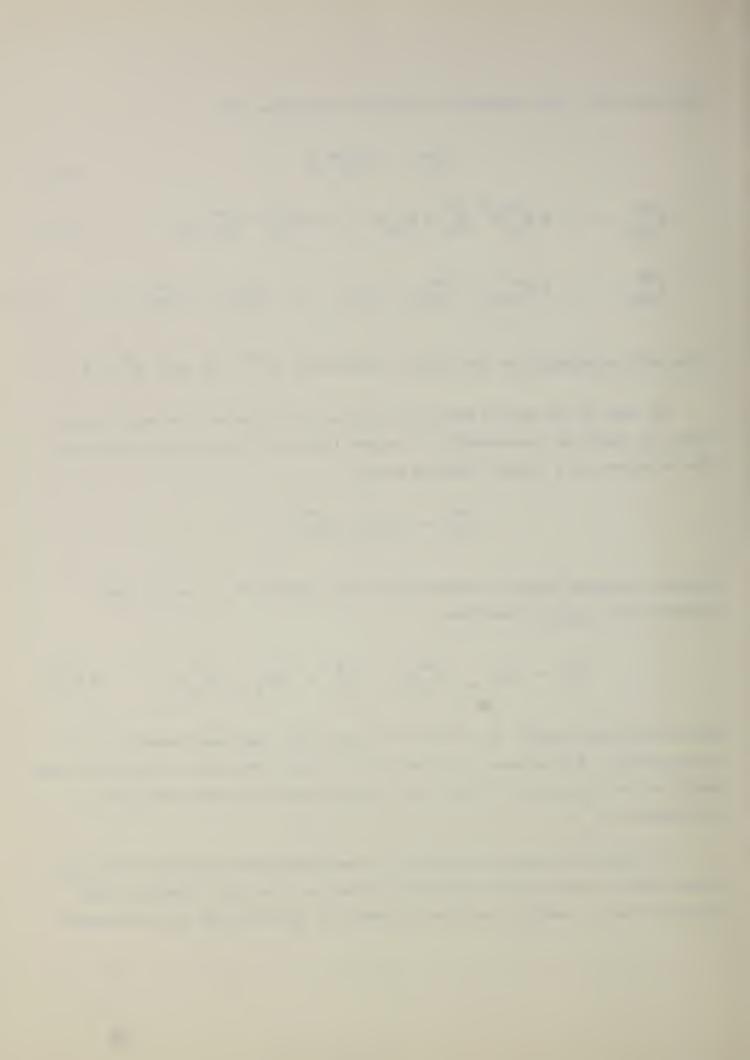
$$Q_{\infty}^{**} = \lim_{j \to \infty} Q_{j}^{**} .$$

Rather, one might hope for "convergence with period 2", i.e. for the existence of a pair of matrices

$$Q_{\infty}^{o} = \lim_{j \to \infty} Q_{2j+1}^{**}, \quad Q_{\infty}^{e} = \lim_{j \to \infty} Q_{2j}^{*}, \quad (3.12)$$

where the superscripts "o" and "e" stand for "odd" and "even" respectively. Furthermore, in view of the results obtained in Section 2, one would not be surprised if these two limiting matrices turned out to be independent of σ .

At present we have <u>not</u> succeeded in analyzing this situation with anything like the completeness achieved in Section 2 for the "location with revision" case. However, we have succeeded in proving that in the present



case, like that of Section 2, the <u>precision of position-location stabilizes</u> over time. To make this precise, let

$$Q_{j}^{**} = \begin{bmatrix} q_{1}^{(j)} & q^{(j)} \\ \vdots & \vdots \\ q^{(j)} & q_{2}^{(j)} \end{bmatrix}$$

then $q^{(0)} = q$ and $q_i^{(0)} = q_i$ (i = 1,2). The precision with which the j-th location-operation estimates the position of the locatee is given by

$$q_2^{(j)} = var(U_{2j}^*)$$
 if j is even,
 $q_1^{(j)} = var(U_{1j}^*)$ if j is odd.

It will be shown below that

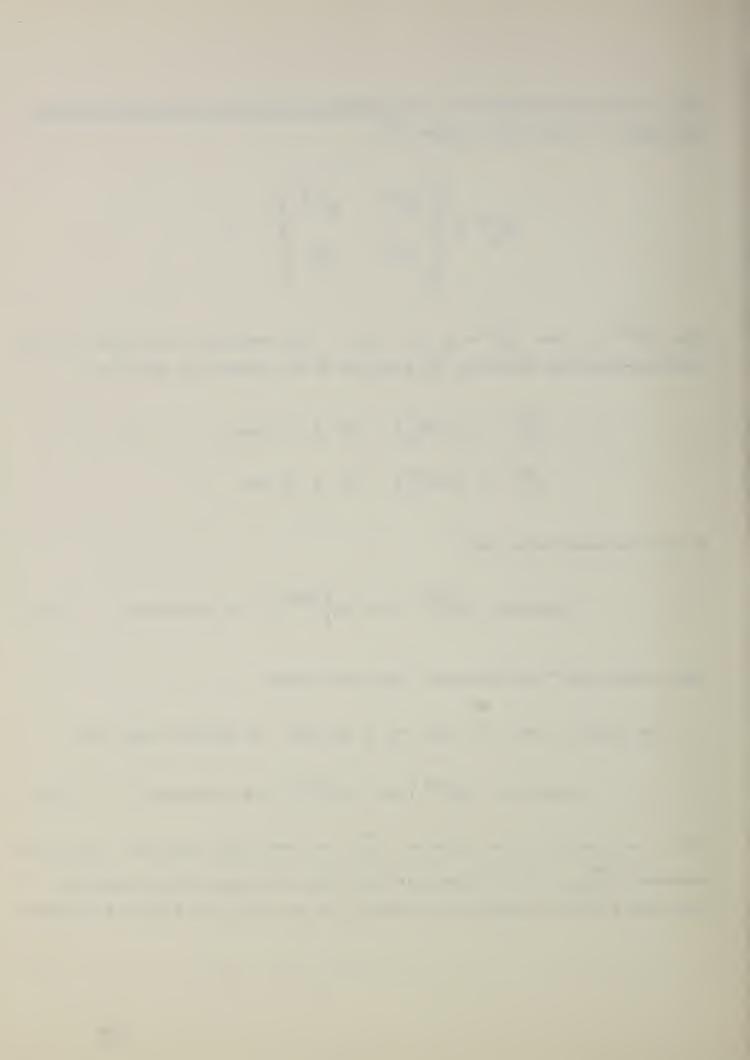
sequences
$$\{q_1^{(2j)}\}$$
 and $\{q_1^{(2j+1)}\}$ are convergent, (3.13)

thus proving the "stabilization" mentioned above.

The logic of the proof will run as follows. It will be shown that

sequences
$$\{q_1^{(2j)}\}$$
 and $\{q_2^{(2j)}\}$ are convergent . (3.14)

This is a property of the sequence $\{Q_{2j}^*\}$ of even-index matrices. Since the sequence $\{Q_{2j+1}^*\}$ of odd-index matrices obeys the same type of recursion, and since (3.14) is symmetric as between the two units, it follows by analogy



that

sequences
$$\{q_1^{(2j+1)}\}$$
 and $\{q_2^{(2j+1)}\}$ are convergent. (3.15)

The desired result (3.13) then follows from (3.14) and (3.15).

Thus it suffices to prove (3.14). Since the variance terms $q_1^{(2j)}$ and $q_2^{(2j)}$ are nonnegative, i.e. bounded below by 0, it suffices to prove that the sequences in (3.14) are non-increasing. These statements,

$$q_1^{(2j+2)} \le q_1^{(2j)}$$
 , $q_2^{(2j+2)} \le q_2^{(2j)}$,

are to be proved by induction on j , but it suffices to establish the prototype induction step, namely

$$q_1^{(2)} \le q_1$$
 , $q_2^{(2)} \le q_2$. (3.16)

The proof of the desired result (3.13) has now been reduced to the demonstration of the two statements (3.16). For proving them, it is convenient to introduce the auxiliary quantities

$$S = (q_1-q) + (q_2-q)$$
 , $\Delta = q_1q_2-q^2$. (3.17)

Since Q_0 is a variance-covariance matrix, its determinant $\Delta \geq 0$, and it follows by (2.23) that $S \geq 0$. The following calculations will make use of the easily-checked identities

$$\Delta - qS = (q_1 - q)(q_2 - q)$$
, (3.18)

$$\Delta - q_i S = -(q_i - q)^2$$
 (3.19)



Direct calculation from (3.6) yields

$$q_{1}^{**} = (\sigma^{2} + s)^{-1} \begin{bmatrix} \sigma^{2}q_{1} + \Delta & \sigma^{2}q + \Delta \\ & & \\ \sigma^{2}q + \Delta & (\sigma^{2} + s)q_{2} \end{bmatrix}$$
 (3.20)

From (3.7), we obtain

$$(I + H_1^{**})^{-1} = [\sigma^4 + 2S\sigma^2 + (q_2 - q)^2]^{-1} \begin{bmatrix} \sigma^4 + (S + q_2 - q)\sigma^2 + (q_2 - q)^2 & \sigma^2(q_1 - q) \\ \\ \sigma^2(q_2 - q) + (q_2 - q)^2 & \sigma^4 + (S + q_1 - q)\sigma^2 \end{bmatrix} .$$

Application of (3.8) and (3.20) yields

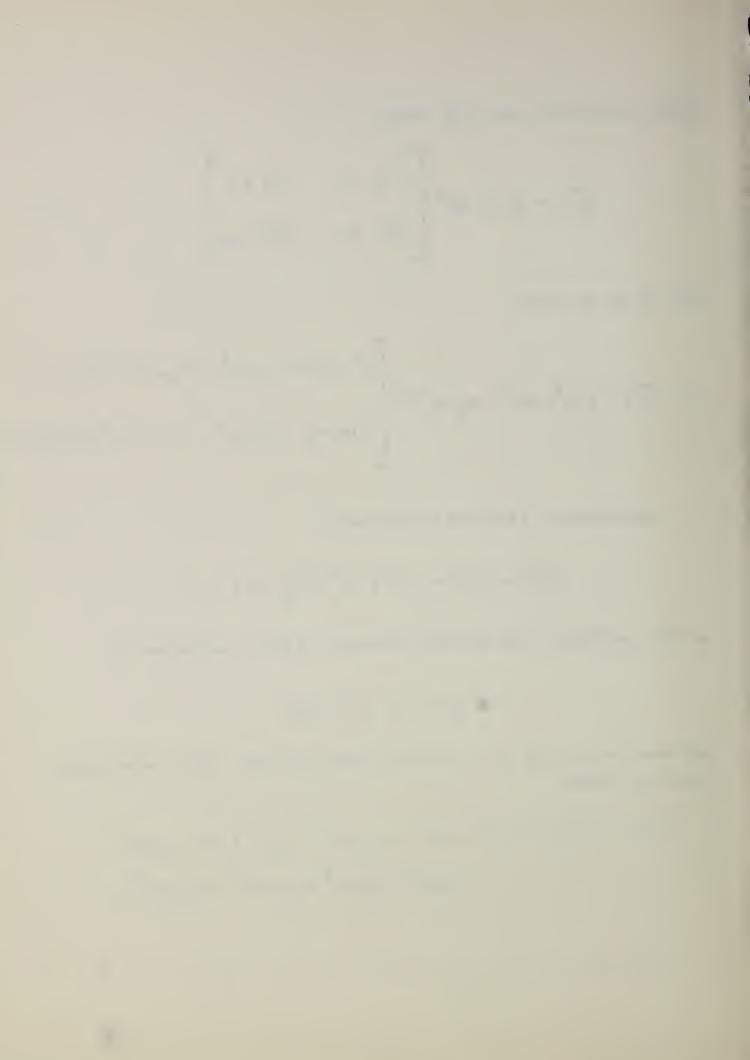
$$q_1^{(2)} = q_1^{(1)} = (\sigma^2 + S)^{-1}(\sigma^2 q_1 + \Delta)$$
,

so that the first of the desired statements (3.16) is equivalent to

$$\sigma^2 q_1 + \Delta \leq (\sigma^2 + S)q_1$$

and hence to Δ - $q_1^S \leq 0$, which is true by (3.19). Next, substitution into (3.8) yields

$$q_{2}^{(2)} = (\sigma^{2} + s)^{-1} [\sigma^{4} + 2s\sigma^{2} + (q_{2} - q)^{2}]^{-1} \{q_{2}\sigma^{6} + [\triangle + 2q_{2}s]\sigma^{4} + [2q_{2}s^{2} - (q_{2} - q)^{2}(q_{2} - 2q)]\sigma^{2} + \triangle(q_{2} - q)^{2}\},$$



so that the second of the desired statements (3.16) is equivalent to

$$q_2 \sigma^6 + [\triangle + 2q_2 S] \sigma^4 + [2q_2 S^2 - (q_2 - q)^2 (q_2 - 2q)] \sigma^2 + \triangle (q_2 - q)^2$$

$$\leq q_2 (\sigma^2 + S) [\sigma^4 + 2S\sigma^2 + (q_2 - q)^2],$$

which is true since it is in turn equivalent to

$$(q_2-q)^2 [\sigma^2 + (q_2-q)]^2 \ge 0$$
.

This completes the proof of (3.13), so that the existence of the "variance terms" in (3.12), i.e. entries q_1^o and q_2^o in Q_∞^o and entries q_1^e and q_2^e in Q_∞^e , is established. We have <u>not</u> as yet succeeded in proving the existence of the covariance limits

$$q^{\circ} = \lim_{j \to \infty} q^{(2j+1)}, \quad q^{e} = \lim_{j \to \infty} q^{(2j)}, \quad (3.21)$$

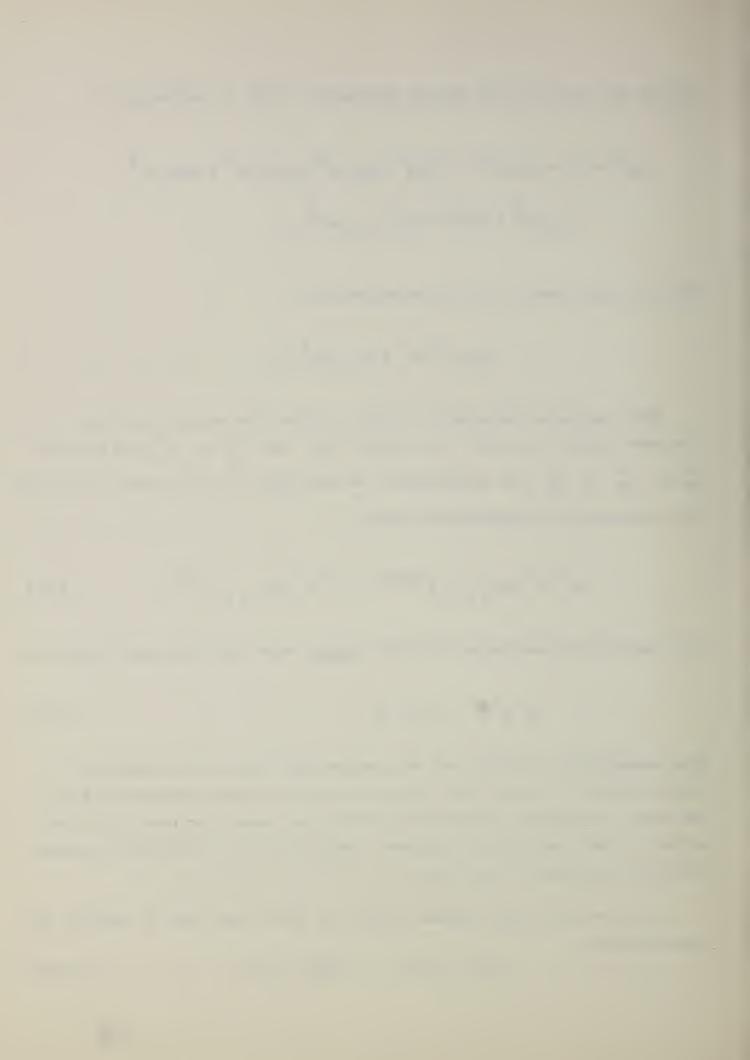
i.e. the off-diagonal terms in (3.12), except under the additional hypotheses

$$q_1 \ge q$$
 , $q_2 \ge q$. (3.22)

This assumption is probably not very restrictive for the situations of interest here; it asserts that the errors in the initial estimates (of the two units' positions), if positively correlated, have covariance less than either of their individual variances. Because $\Delta \geq 0$, (3.22) will automatically be satisfied if $q_1 = q_2$.

To prove that (3.22) implies (3.21), we first prove that it implies the generalization

$$q_1^{(j)} \ge q^{(j)}$$
, $q_2^{(j)} \ge q^{(j)}$ (3.23)



of itself. The proof is by induction on j, and since (3.23) is symmetric as between the two units, it suffices to treat a prototype induction step, i.e. to show that

$$q_1^{(1)} \ge q^{(1)}$$
 , $q_2^{(1)} \ge q^{(1)}$ (3.24)

follows from (3.22). From (3.20), we see that the first part of (3.24) is an immediate consequence of the first part of (3.22). Also from (3.20), we see that the second part of (3.24) is equivalent to

$$(\sigma^2 + S)q_2 \geq \sigma^2q + \Delta$$
,

hence to

$$\sigma^{2}(q_{2}-q) \geq \Delta - q_{2}S - (q_{2}-q)^{2}$$
,

which follows from the second part of (3.22) .

We will show below that (3.22) implies

sequence
$$\{q^{(2j)}\}$$
 is non-decreasing. (3.25)

Because the variance-covariance matrix Q_{2j}^{**} must have a non-negative determinant,

$$[q^{(2j)}]^2 \leq q_1^{(2j)}q_2^{(2j)}$$
,

it follows that the sequence in (3.25) is ultimately bounded above by a quantity $\left[q_1^eq_2^e\right]^{\frac{1}{2}}+\varepsilon$ where $\varepsilon>0$, and so this sequence must have a limit q^e . This pertains to the sequence $\left\{Q_{2j}^{***}\right\}$; since the sequence $\left\{Q_{2j+1}^{***}\right\}$ is generated by the same type of recursion, and since by (3.24) its initial



matrix Q_1 satisfies the analog of (3.22), the same logic proves the existence of the limiting covariance q° .

It only remains to prove that (3.22) implies (3.25). Since (3.22) implies (3.23), it suffices to establish the prototype induction step, namely that (3.22) implies

$$q^{(2)} \ge q$$
 (3.26)

Application of (3.8) yields

$$\begin{split} \mathbf{q}^{(2)} &= (\sigma^2 + \mathbf{S})^{-1} [\sigma^4 + 2\mathbf{S}\sigma^2 + (\mathbf{q}_2 - \mathbf{q})^2]^{-1} \left\{ \mathbf{q}\sigma^6 \right. \\ &+ \left[(\mathbf{q}_2 - \mathbf{q})\mathbf{q}_1 + \triangle + \mathbf{q}(\mathbf{S} + \mathbf{q}_1 - \mathbf{q}) \right] \sigma^4 + \left[(\mathbf{q}_2 - \mathbf{q}) \triangle + \mathbf{q}_1 (\mathbf{q}_2 - \mathbf{q})^2 + (\mathbf{S} + \mathbf{q}_1 - \mathbf{q}) \triangle \right] \sigma^2 \\ &+ (\mathbf{q}_2 - \mathbf{q})^2 \triangle \right\} \\ &= (\sigma^2 + \mathbf{S})^{-1} \left[\sigma^4 + 2\mathbf{S}\sigma^2 + (\mathbf{q}_2 - \mathbf{q})^2 \right]^{-1} \left\{ \mathbf{q}\sigma^6 \right. \\ &+ \left[2\Delta + \mathbf{q}\mathbf{S} \right] \sigma^4 + \left[2\mathbf{S}\Delta + \mathbf{q}_1 (\mathbf{q}_2 - \mathbf{q})^2 \right] \sigma^2 + \left(\mathbf{q}_2 - \mathbf{q} \right)^2 \triangle \right\} . \end{split}$$

Thus (3.26) is equivalent to

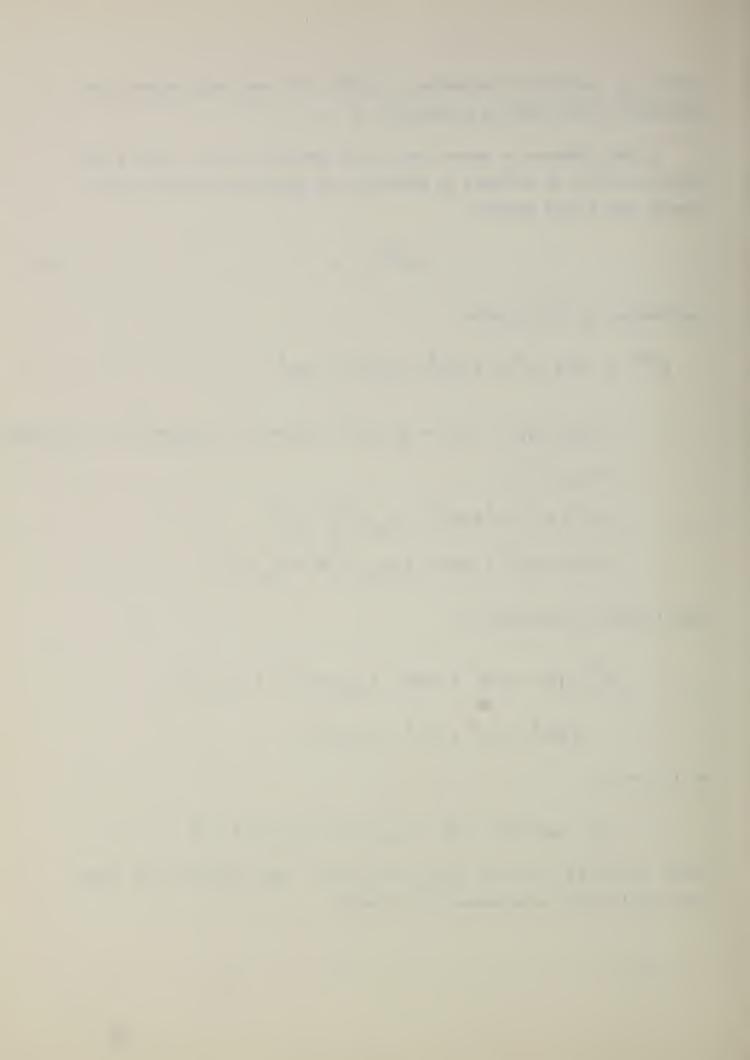
$$q\sigma^{6} + [2\triangle + qS]\sigma^{4} + [2S\triangle + q_{1}(q_{2}-q)^{2}]\sigma^{2} + (q_{2}-q)^{2}\triangle$$

$$\geq q(\sigma^{2} + S)[\sigma^{4} + 2S\sigma^{2} + (q_{2}-q)^{2}],$$

or in turn to

$$(\Delta - qS)\{2\sigma^4 + [2S + (q_2-q)]\sigma^2 + (q_2-q)^2\} \ge 0$$
,

which is true by virtue of (3.18) and (3.22). This completes the proof that the limiting covariances (3.21) exist.



matrix Q_1 satisfies the analog of (3.22), the same logic proves the existence of the limiting covariance q° .

It only remains to prove that (3.22) implies (3.25). Since (3.22) implies (3.23), it suffices to establish the prototype induction step, namely that (3.22) implies

$$q^{(2)} \ge q$$
 (3.26)

Application of (3.8) yields

$$q^{(2)} = (\sigma^{2} + s)^{-1} [\sigma^{4} + 2s\sigma^{2} + (q_{2} - q)^{2}]^{-1} \{q\sigma^{6} + [(q_{2} - q)q_{1} + \triangle + q(s + q_{1} - q)]\sigma^{4} + [(q_{2} - q) \triangle + q_{1}(q_{2} - q)^{2} + (s + q_{1} - q)\triangle]\sigma^{2} + (q_{2} - q)^{2} \triangle \}$$

$$= (\sigma^{2} + s)^{-1} [\sigma^{4} + 2s\sigma^{2} + (q_{2} - q)^{2}]^{-1} \{q\sigma^{6} + [2\triangle + qs]\sigma^{4} + [2s\triangle + q_{1}(q_{2} - q)^{2}]\sigma^{2} + (q_{2} - q)^{2}\triangle\}.$$

Thus (3.26) is equivalent to

$$q\sigma^{6} + [2\Delta + qS]\sigma^{4} + [2S\Delta + q_{1}(q_{2}-q)^{2}]\sigma^{2} + (q_{2}-q)^{2}\Delta$$

$$\geq q(\sigma^{2} + S)[\sigma^{4} + 2S\sigma^{2} + (q_{2}-q)^{2}],$$

or in turn to

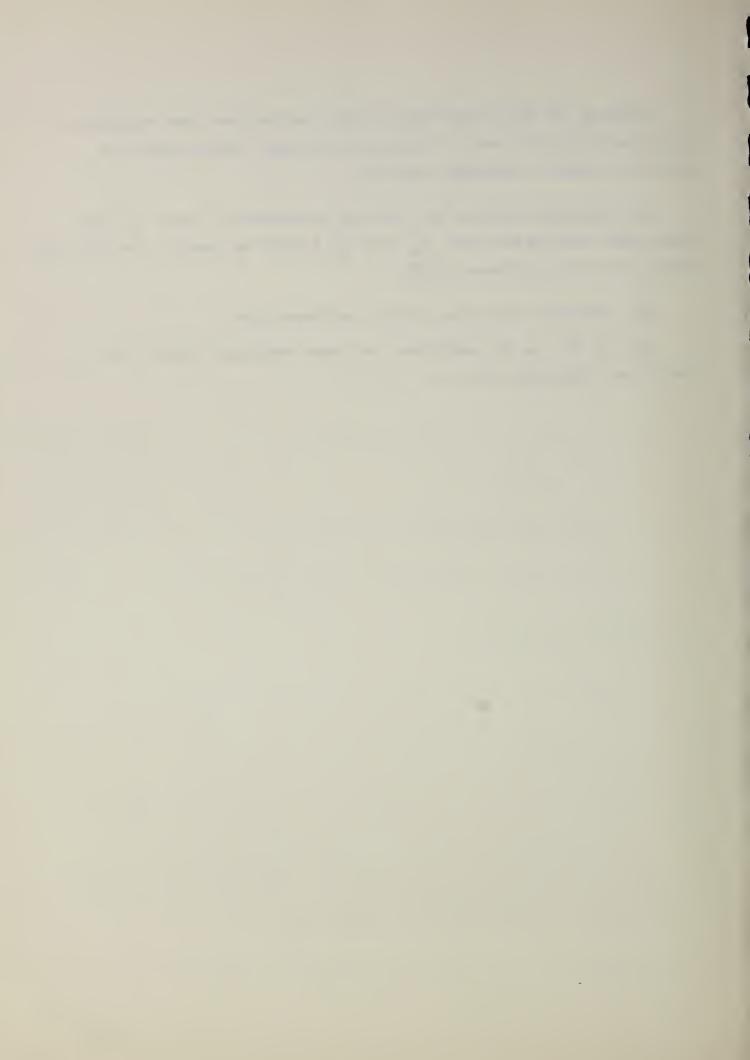
$$(\Delta - qS)\{2\sigma^4 + [2S + (q_2-q)]\sigma^2 + (q_2-q)^2\} \ge 0$$
,

which is true by virtue of (3.18) and (3.22). This completes the proof that the limiting covariances (3.21) exist.



Although the main objectives in this Section have been achieved, we should note several items of "unfinished business" which need to be settled to obtain a thorough analysis:

- (a) Determine whether the limiting covariances q^o and q^e (and hence, the limiting matrices Q^o_{∞} and Q^e_{∞}) exist in general, and not only under the extra hypotheses (3.22).
 - (b) Evaluate the various limits in closed form.
- (c) If (b) is too ambitious, at least determine whether the limits are independent of $\boldsymbol{\sigma}$.



PROJECT "WHERE": WORKING PAPER NO. 7

Algorithms

D. J. Sookne

1. Description of the Algorithms used by WHERSM

The algorithm used to locate each unit is the least squares squared (LSS) algorithm. Both two- and three-dimensional subroutines are included in the WHERSM system. The three-dimensional program is described in detail below.

For each locator i, i = 1, 2, ..., n, let (x_i, y_i, z_i) be its estimated position, r_i its reported distance to the locatee, and w_i the reciprocal of its variance, the calculation of which is described below. The w_i 's act as weights; the smaller the variance of a locator, the more accurately we know its position, and the higher its weight will be. Then LSS minimizes

$$E = \sum_{i=1}^{n} w_{i} E_{i} \quad \text{where} \quad (1)$$

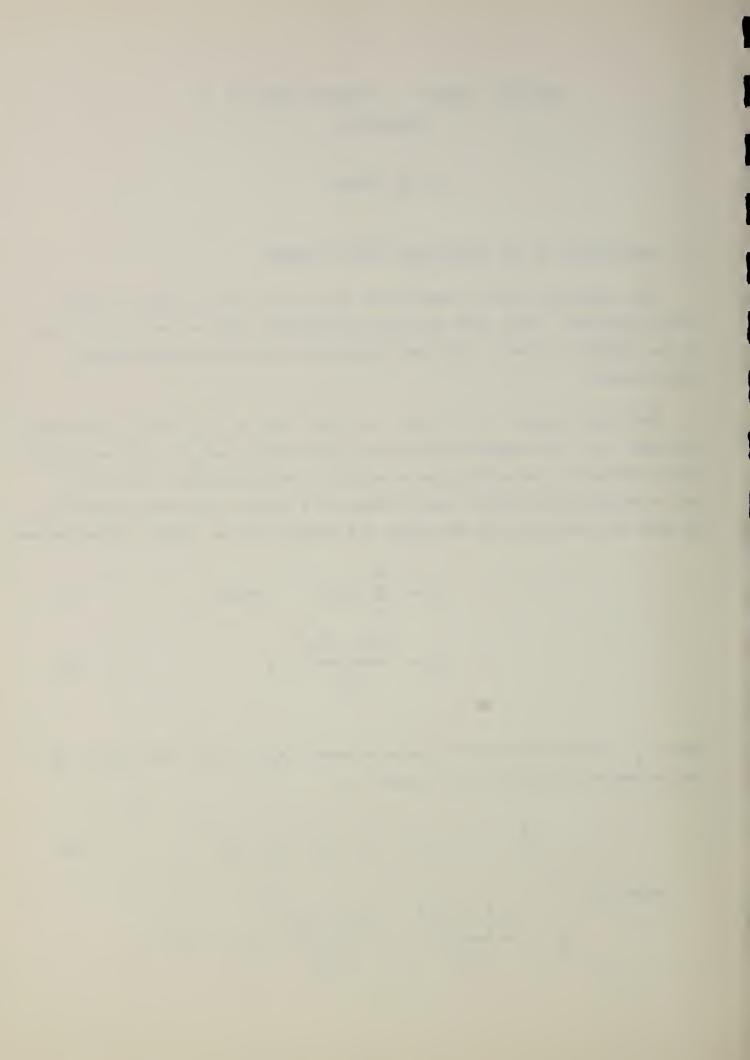
$$E_{i} = \frac{(d_{i}^{2} - r_{i}^{2})^{2}}{4r_{i}^{2}}; \qquad (2)$$

here d_i is the calculated distance between (x_i, y_i, z_i) and (x, y, z), the estimated position of the locatee, so

$$d_i^2 = (x - x_i)^2 + (y - y_i)^2 + (z - z_i)^2$$
. (3)

Note that

$$E_{i} = \frac{(d_{i}^{2} - r_{i}^{2})^{2}}{4r_{i}^{2}} = \frac{(d_{i} + r_{i})^{2}}{4r_{i}^{2}} \cdot (d_{i} - r_{i})^{2}.$$



When the estimated positions of locators and locatee are near their true positions, r_i is very near d_i , so the factor $(d_i + r_i)^2/4r_i^2$ is very near 1, and E_i behaves very much like $(d_i - r_i)^2$. Thus we expect this algorithm to produce answers nearly identical to those produced by the least squares (LS) algorithm, for which $E_i = (d_i - r_i)^2$. Indeed, computer tests indicate that there is no significant difference between the results of these two algorithms. Thus LSS is used because it is more economical, since LS requires the calculation of d_i , which in turn requires a square root to be taken (see (3)). LSS avoids the square root, since only d_i^2 is needed.

Where E is a minimum, its partial derivatives with respect to x, y, and z will be zero. Thus the program calculates

$$F = \frac{\partial E}{\partial x} = \sum_{i=1}^{n} \frac{w_{i}(d_{i}^{2} - r_{i}^{2})}{r_{i}^{2}} (x - x_{i})$$

$$G = \frac{\partial E}{\partial y} = \sum_{i=1}^{n} \frac{w_{i}(d_{i}^{2} - r_{i}^{2})}{r_{i}^{2}} (y - y_{i})$$

$$H = \frac{\partial E}{\partial z} = \sum_{i=1}^{n} \frac{w_{i}(d_{i}^{2} - r_{i}^{2})}{r_{i}^{2}} (z - z_{i}).$$
(4)

Since d_i depends on x, y, and z (see (3)), F, G, and H depend non-linearly on these variables. Then the system (4) cannot be solved directly for x, y, and z. Instead, LSS does successive Newton-Raphson iterations ([1], pp. 201-223), beginning with a starting point p = (x,y,z). The first iteration yields a new point $p' = (x + \Delta x, y + \Delta y, z + \Delta z)$; this point is used as the starting point for the next iteration, and so on. The process begins with the first order approximation



$$F_{p}' = F_{p} + \frac{\partial F}{\partial x} \Delta x + \frac{\partial F}{\partial y} \Delta y + \frac{\partial F}{\partial z} \Delta z$$

$$G_{p}' = G_{p} + \frac{\partial G}{\partial x} \Delta x + \frac{\partial G}{\partial y} \Delta y + \frac{\partial G}{\partial z} \Delta z$$

$$H_{p}' = H_{p} + \frac{\partial H}{\partial x} \Delta x + \frac{\partial H}{\partial y} \Delta y + \frac{\partial H}{\partial z} \Delta z$$

Here F_p denotes the value of F at point p, and all partial derivatives are evaluated at p. Thus this system represents the expansions of the functions F, G, and H about p. Now we want F_p , G_p , and H_p , all to be zero, so the problem reduces to that of finding Δx , Δy , Δz which satisfy the three simultaneous equations

$$\frac{\partial F}{\partial x} \Delta x + \frac{\partial F}{\partial y} \Delta y + \frac{\partial F}{\partial z} \Delta z + F_{p} = 0$$

$$\frac{\partial G}{\partial x} \Delta x + \frac{\partial G}{\partial y} \Delta y + \frac{\partial G}{\partial z} \Delta z + G_{p} = 0$$

$$\frac{\partial H}{\partial x} \Delta x + \frac{\partial H}{\partial y} \Delta y + \frac{\partial H}{\partial z} \Delta z + H_{p} = 0 .$$
(5)

The program calculates F, G, and H (see (4)), and

$$\frac{\partial F}{\partial x} = \sum_{i=1}^{n} \frac{w_{i}(d_{i}^{2} - r_{i}^{2} + 2(x - x_{i})^{2})}{r_{i}^{2}}$$

$$\frac{\partial C}{\partial y} = \sum_{i=1}^{n} \frac{w_{i}(d_{i}^{2} - r_{i}^{2} + 2(y - y_{i})^{2})}{r_{i}^{2}}$$

$$\frac{\partial H}{\partial z} = \sum_{i=1}^{n} \frac{w_{i}(d_{i}^{2} - r_{i}^{2} + 2(z - z_{i})^{2})}{r_{i}^{2}}$$
(6)



$$\frac{\partial G}{\partial x} = \frac{\partial}{\partial x} \frac{\partial E}{\partial y} = \frac{\partial}{\partial y} \frac{\partial E}{\partial x} = \frac{\partial F}{\partial y} = \sum_{i=1}^{n} \frac{2w_{i}(x - x_{i})(y - y_{i})}{r_{i}^{2}}$$

$$\frac{\partial H}{\partial x} = \frac{\partial}{\partial x} \frac{\partial E}{\partial z} = \frac{\partial}{\partial z} \frac{\partial E}{\partial x} = \frac{\partial F}{\partial z} = \sum_{i=1}^{n} \frac{2w_{i}(x - x_{i})(z - z_{i})}{r_{i}^{2}}$$

$$\frac{\partial H}{\partial y} = \frac{\partial}{\partial y} \frac{\partial E}{\partial z} = \frac{\partial}{\partial z} \frac{\partial E}{\partial y} = \frac{\partial G}{\partial z} = \sum_{i=1}^{n} \frac{2w_{i}(y - y_{i})(z - z_{i})}{r_{i}^{2}}$$
,

then solves (5) for Δx , Δy , Δz . This determines $p'=(x+\Delta x, y+\Delta y, z+\Delta z)$, which is used as the starting point for the next iteration. For a given set of locators, the program will do up to 4 iterations, stopping if an iteration converges, namely

$$\max(|F|,|G|,|H|) \leq \sum_{i=1}^{n} w_{i},$$

or if an iteration diverges (which see below) . I.e. convergence occurs when F, G, and H are all small.

Computer tests indicated that for both the two- and three-dimensional versions of LSS, 2 to 4 Newton-Raphson iterations are generally sufficient for convergence, even when the starting point is 100 meters from the true position.

The LSS algorithm allows for easy elimination of outliers. These are locators whose reported distance (r_i) to the locatee contains a greater error than do the reported distances of the other locators. Let

$$\overline{E} = \left(\sum_{i=1}^{n} w_{i} E_{i}\right) / \sum_{i=1}^{n} w_{i} . \tag{7}$$



Now any locator i is eliminated for which

$$E_{i} > 4\overline{E} . \tag{8}$$

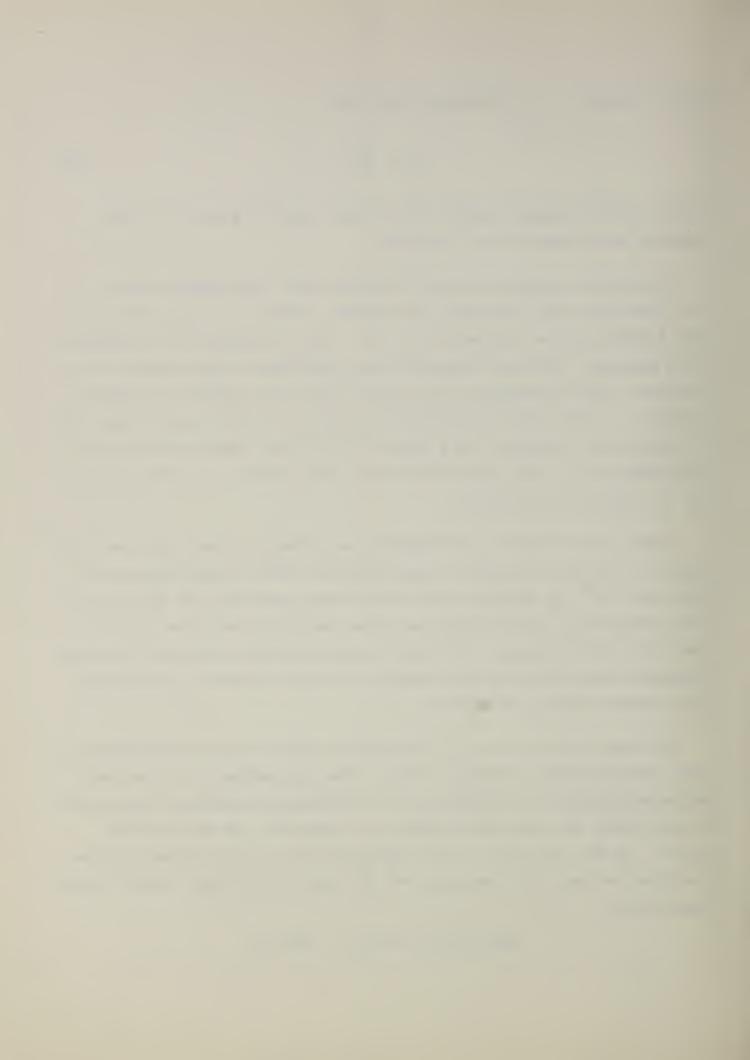
Several other constants greater than 1 were tried in place of 4, but computer tests showed that 4 was best.

The algorithm iterates on all locators until convergence occurs, up to 4 iterations (for divergence, see below). Then \overline{E} is calculated and some locators may be eliminated via (8). (If no locators are eliminated, we're through). Then more iterations are performed on the reduced set of locators. After convergence, (7) and (8) are again applied to eliminate outliers. This iteration-elimination process continues until either (1) no locators are eliminated in a step, (2) 1/4 of the locators have been eliminated, or (3) the algorithm diverges (see below). In cases (1) and (2) the algorithm terminates.

There are two types of divergence; an increase in the objective function, E, from one iteration to the next and a badly scaled determinant less than 10^{-8} in absolute value which makes equations (5) impossible to solve accurately. In each case, we halve the step size of the previous iteration, and try again. This can be done unless the iteration at which divergence occurs is the first iteration for this locatee. Then we must quit without finding a solution.

For any locatee and set of locators, the size of successive iteration steps should decrease rapidly. If not, then the problem is ill-behaved, and perhaps dozens of iterations will be necessary to achieve convergence. To avoid this, the algorithm attempts to "home in" on the solution faster. If the step size in the x-direction (or y or z) is Δx_1 for one iteration and Δx_2 for the next, and if $|\Delta x_2| > \frac{1}{2} |\Delta x_1|$, then Δx_2 is replaced by

$$2\text{min}(\left|\triangle \mathbf{x}_{1}\right|,\left|\triangle \mathbf{x}_{2}\right|)$$
 • $\text{sgn} \triangle \mathbf{x}_{2}$



if Δx_1 and Δx_2 have the same sign, and if they have opposite signs, Δx_2 is replaced by

$$\frac{\Delta x_2 \cdot \Delta x_1}{\Delta x_1 - \Delta x_2} \quad .$$

A further refinement of the algorithm was tried; this involved relocating the locators. More concerning this may be found in sec. 3 and Working Paper No. 8. Once the Newton iterations have converged, there is an error between the reported distance \mathbf{r}_i and the calculated distance \mathbf{d}_i , for each locator \mathbf{r}_i in the set. By changing the estimated position of each locator, i.e. by moving it along the straight line connecting it with the locatee, this error $\mathbf{d}_i - \mathbf{r}_i$ may be reduced, even eliminated. After relocating, more Newton-Raphson iterations may be done. Several runs were made, using different values for the fraction, \mathbf{f} , of the error eliminated by relocation, with $0 < \mathbf{f} < 1$. The best such \mathbf{f} was the smallest, and that was not quite as good as no relocation ($\mathbf{f} = 0$). Relocation remains an option in the LSS routines, but one which is not now used.

The 2-dimensional LSS program is analogous to the 3-dimensional one. It solves the equations

$$\frac{\partial F}{\partial x} \Delta x + \frac{\partial F}{\partial y} \Delta y + F = 0$$

$$\frac{\partial G}{\partial x} \Delta x + \frac{\partial G}{\partial y} \Delta y + G = 0 \quad .$$

Here, F and G and their partial derivatives are as described above, except that all z-components are zero. The 2-dimensional program is less likely to result in divergence of an iteration, so the special steps to handle divergence (see previous page) are omitted.



The weights w_i (see (1)) are again taken as the reciprocals of the variances σ_i^2 . When a unit has been located, the variance of its location is calculated as

$$\frac{\left(\sum_{i=1}^{n} w_{i} E_{i}\right)}{\sum_{i=1}^{n} w_{i}}$$
(9)

when n is the number of locators, m the dimensionality (2 or 3) of the algorithm.

When the locatee is lost, so that no starting point exists for the LSS routine, the least squares linear (LSL) routine is called to provide a starting point. First, a slant-range reduction is done to convert 3-D reported distances to 2-D . Then the 2-D LSL algorithm is called. This is the same basic algorithm which is described in sec. 2 of [2] . The modifications are these: all pairs of circles are used, and outliers are eliminated. Consider the M radical axis lines each formed by a pair of circles; the equation for such a line is found by subtracting the equation of one circle from the equation of the other as in [2] , p. 10. For each such line k, k = 1,2,...M, let d_k be the calculated distance from the locatee to the line. Then LSL minimizes

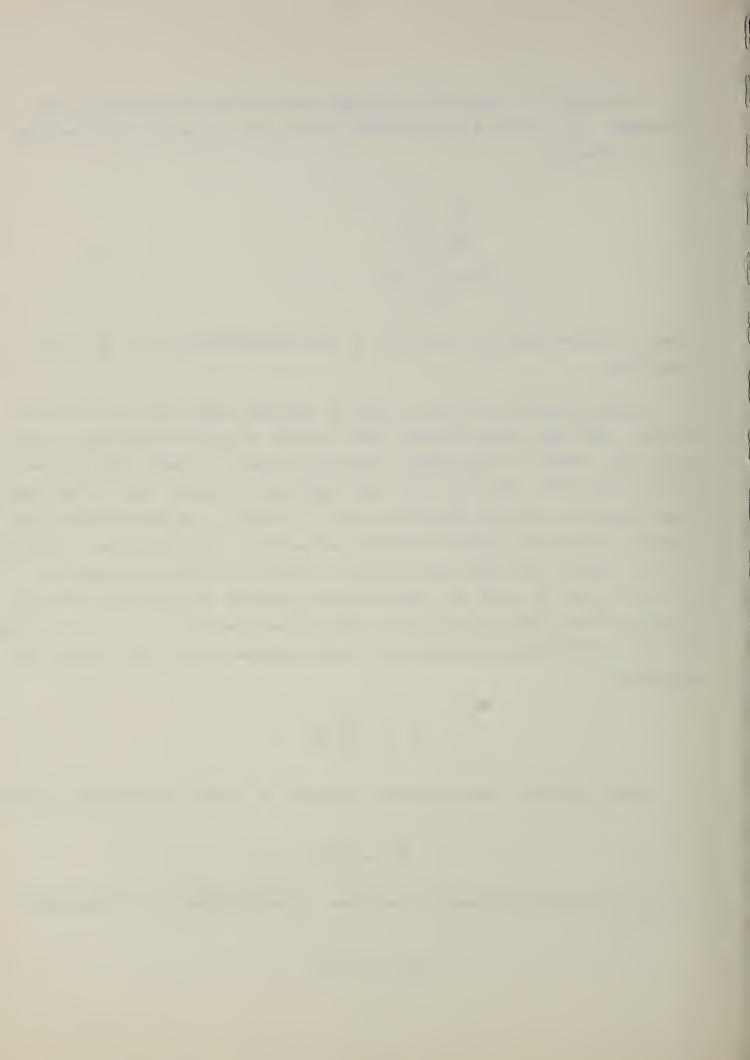
$$D = \sum_{k=1}^{M} d_k^2 .$$

After a locatee has been found using all M lines, the routine calculates

$$\frac{1}{d^2} = D/M ,$$

the average squared distance to the lines. Then any line $\,k\,$ is eliminated for which

$$d_k^2 > 8 \cdot \overline{d^2}$$
.



The reduced set of locators is used to calculate a position, d^2 is recalculated, and a line k is eliminated for which

$$d_k^2 > 4 \cdot \overline{d^2}$$
.

The process is repeated twice more, once with the elimination condition

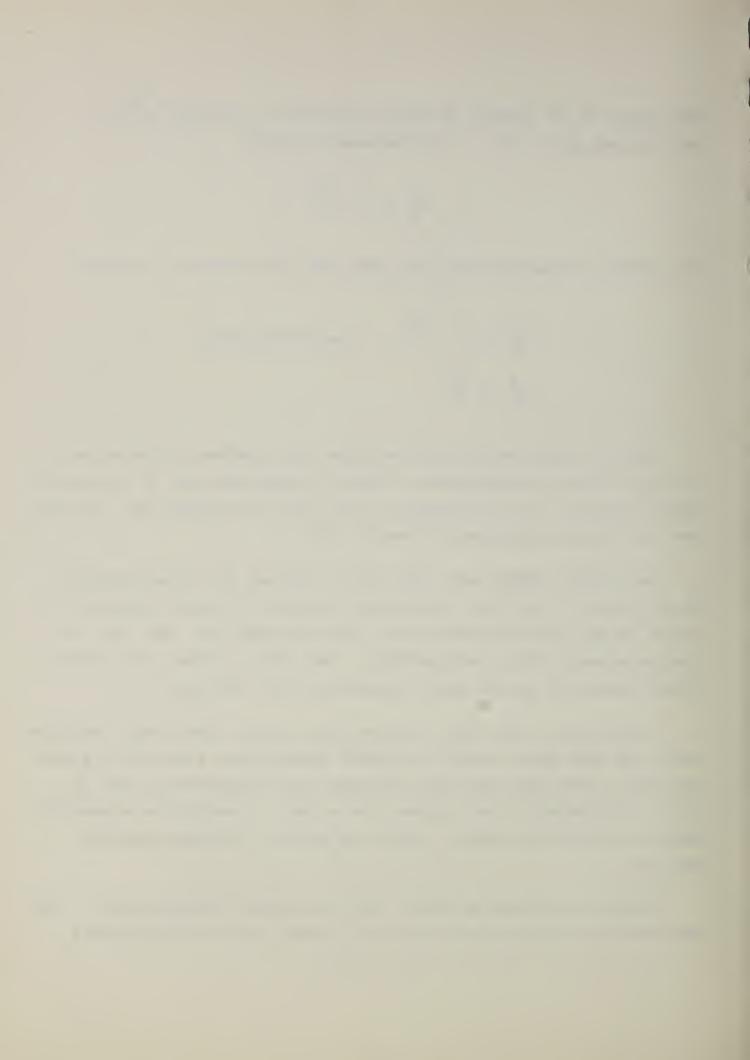
$$d_k^2 > 2 \cdot \overline{d^2}$$
 , and finally with
$$d_k^2 > \overline{d^2}$$
 .

The LSL algorithm will fail only when the equations at the bottom of p. 13 of [2] are ill-conditioned. This will happen when the M lines are nearly parallel, i.e. the locators all lie near one straight line. In this case, no starting point can be found for LSS.

The routine FINDIT calls LSS (2-D or 3-D) and LSL when necessary. If the locatee is not lost, two previous locations are used to extrapolate in the x- and y- directions to get a starting point for LSS. The last z-value is used, with no extrapolation. Then LSS is called; the 2-dimensional routine for ground units, 3-dimensional for airplanes.

If the unit is lost, LSL is called after doing a slant-range reduction (using the last known z-value) to convert 3-dimensional distances to planar distances. Then using the planar distances, the 2-dimensional LSS is called. If the unit is an airplane, the x- and y-coordinates returned by LSS(2-D) plus the last known z-value are used as a starting point for LSS(3-D).

Control is returned to FINDIT with the variance defined by (9). This represents the variance of the position estimate, based on the reported



distances. The total variance is computed by adding RVAR, the variance of the distances. If the locatee is known to be moving, its weight is calculated by inverting the total variance.

If the unit is fixed, the current position estimate is taken to be a weighted average of the old estimate and the just-calculated estimate. Then the weight of the locatee is computed as a weighted average of the old weight and the just-calculated weight. A further description of these calculations may be found in Section three of this report.

2. Description of Algorithms Programmed for WHERSM But Not Now Used

The linear method (LM) and smallest tangent circle (STC) method are described in [2]. They were both found to be less accurate than the LSS and LSL algorithms.

The least squares method mentioned in §1 is the same as LSS, except equations (2), (4), and (6) are replaced by

$$E_{i} = (d_{i} - r_{i})^{2}$$

$$F = \frac{1}{2} \frac{\partial E}{\partial x} = \sum_{i=1}^{n} \frac{(d_{i} - r_{i})(x - x_{i})}{d_{i}}$$

$$G = \frac{1}{2} \frac{\partial E}{\partial y} = \sum_{i=1}^{n} \frac{(d_{i} - r_{i})(y - y_{i})}{d_{i}}$$

$$H = \frac{1}{2} \frac{\partial E}{\partial z} = \sum_{i=1}^{n} \frac{(d_{i} - r_{i})(z - z_{i})}{d_{i}}$$
(4')

and



$$\frac{\partial F}{\partial x} = \sum_{i=1}^{n} \left(\frac{d_{i}^{-r_{i}}}{d_{i}} + \frac{r_{i}(x-x_{i})^{2}}{d_{i}^{3}} \right)$$

$$\frac{\partial G}{\partial y} = \sum_{i=1}^{n} \left(\frac{d_{i}^{-r_{i}}}{d_{i}} + \frac{r_{i}(y-y_{i})^{2}}{d_{i}^{3}} \right)$$

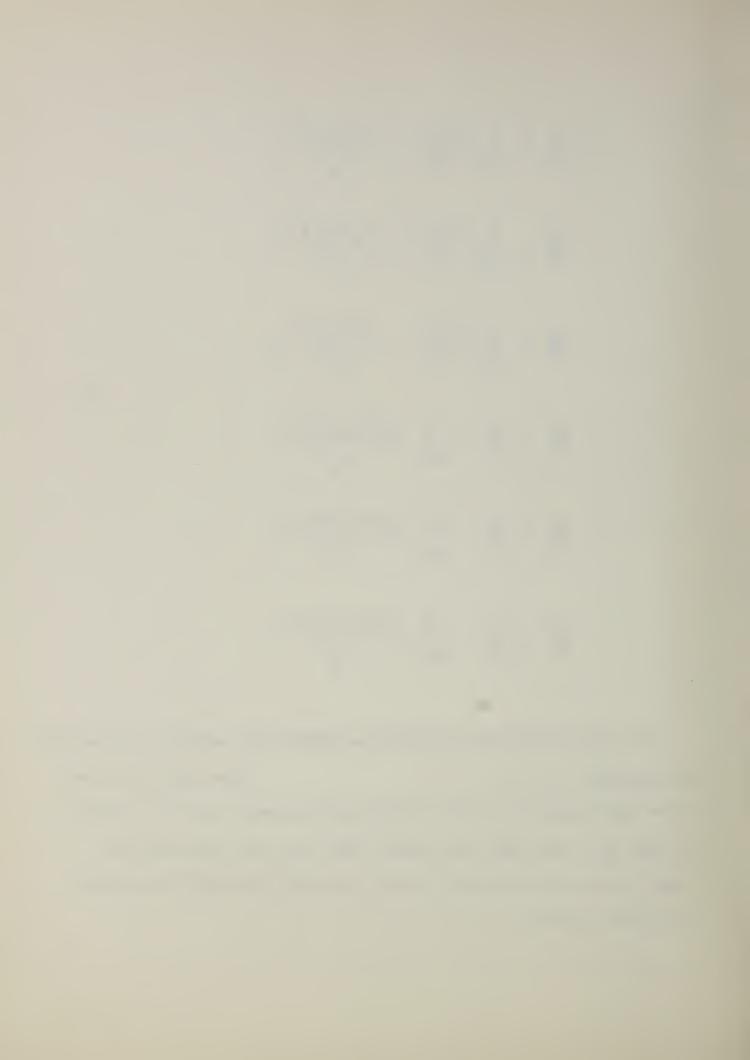
$$\frac{\partial H}{\partial z} = \sum_{i=1}^{n} \left(\frac{d_{i}^{-r_{i}}}{d_{i}} + \frac{r_{i}(z-z_{i})^{2}}{d_{i}^{3}} \right)$$

$$\frac{\partial G}{\partial x} = \frac{\partial F}{\partial y} = \sum_{i=1}^{n} \frac{r_{i}(x-x_{i})(y-y_{i})}{d_{i}^{3}}$$

$$\frac{\partial H}{\partial x} = \frac{\partial F}{\partial z} = \sum_{i=1}^{n} \frac{r_{i}(x-x_{i})(z-z_{i})}{d_{i}^{3}}$$

The other algorithm programmed was MINMAX which minimizes the maximum of the errors $d_i - r_i$. This algorithm proved to be less accurate than STC and much less accurate than LSS. Further, it uses 10 to 100 times the computer time the other algorithms use, since (in the two-dimensional case) it considers all pairs and triples of locator circles.

 $\frac{\partial H}{\partial y} = \frac{\partial G}{\partial z} = \sum_{i=1}^{n} \frac{r_i(y-y_i)(z-z_i)}{d_i^3}.$

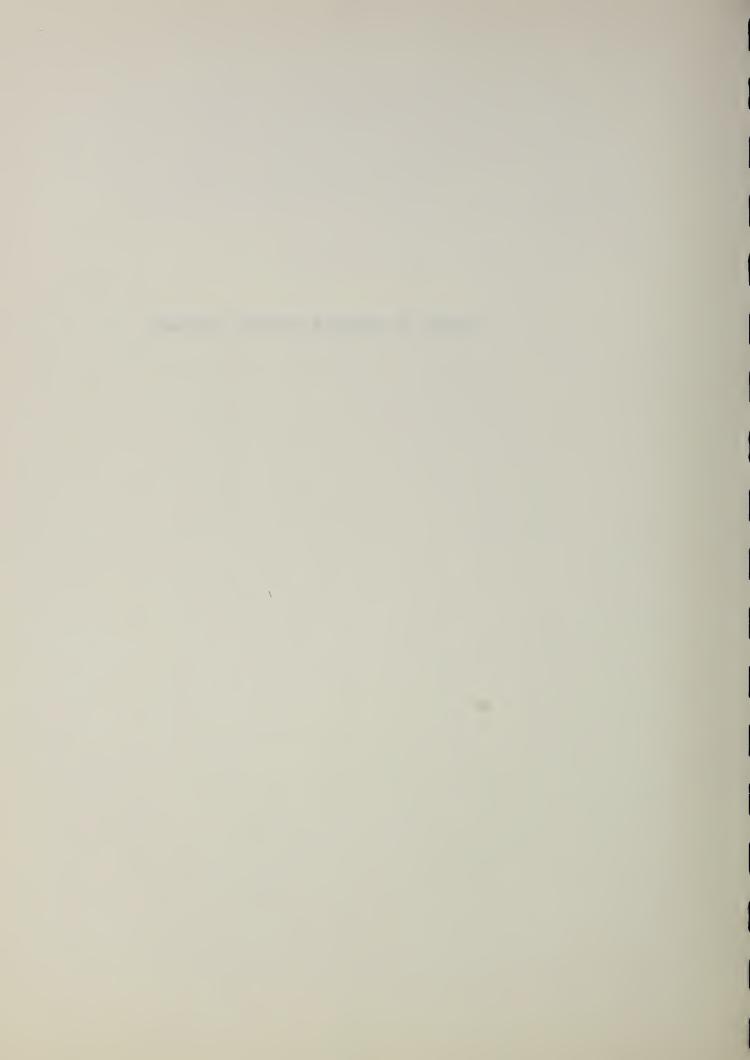


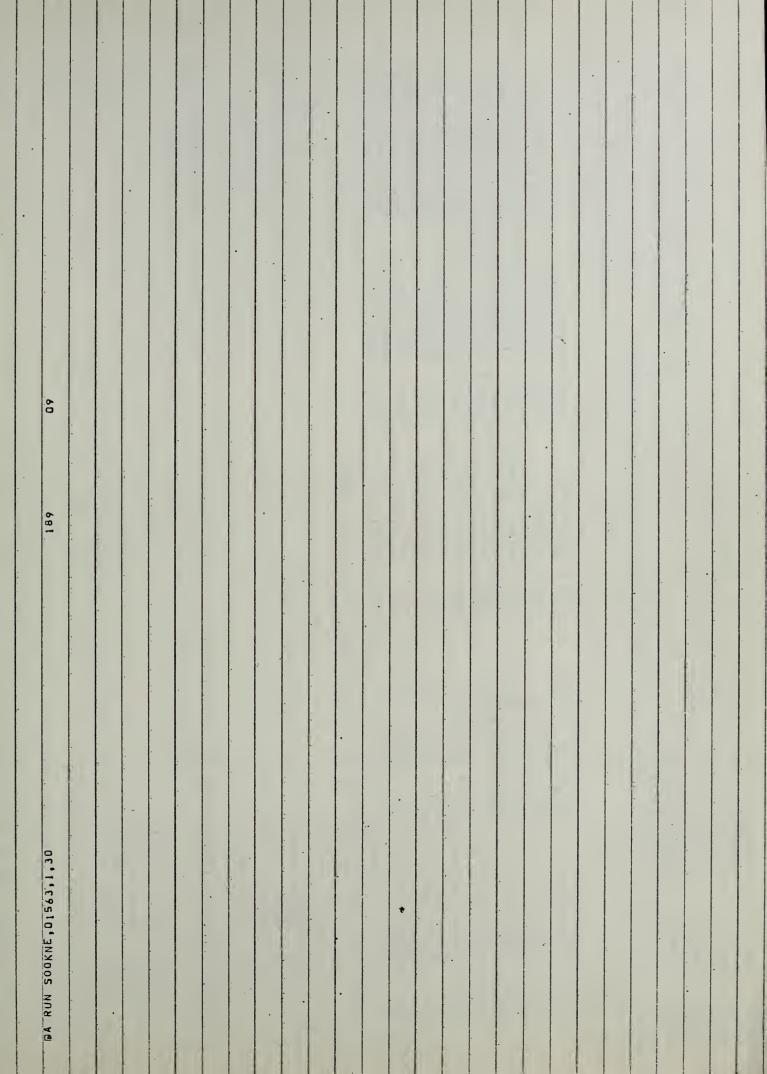
References

- 1. Scarborough, James B., <u>Numerical Mathematical Analysis</u>, John Hopkins Press, Baltimore, 1930.
- 2. First Interim Report on NBS Project WHERE.



LISTING OF POSITION LOCATION PROGRAMS







ENTRY POINT 001120 SUBROUTINE FINDIT

STORAGE USED (BLOCK, NAME, LENGTH)

001135	001121	000000	013000	67,9000
0001 *CODE 001135	*DATA	0002 *BLANK 000000	CB 1	DOD4 MXYZ
1000	0000	0000	0003	4000

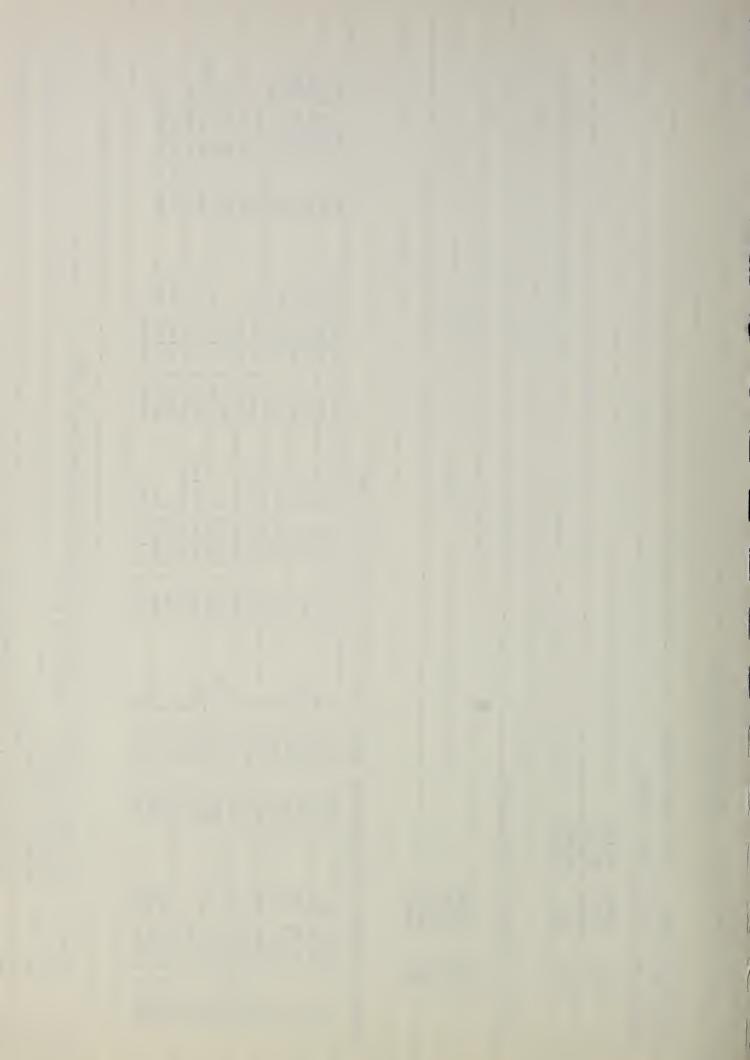
EXTERNAL REFERENCES (BLOCK, NAME)

LOCUSL	Lockss	HEIGHT	LSS30	Sari	NERR35
0000	000¢ LOCL	0007	0000	0011	0012
	-				

STORAGE ASSIGNMENT FOR VARIABLES (BLOCK, TYPE, RELATIVE LOCATION, NAME)

	1000	0001 000152 2L	0001 000403 2416		9225 FEEDUU 1000	0001 000751 4016	DOD B DIIS I CLK	4 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7		0000 1 001032 13	0003 1 006116 LAM		F 7 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	Lead in a contract in a contra	UNATAU A CUUU	0003 R 011167 W	DODGE R DODGE XX		
	361 F/8000 1000	0001 000660 19L	2000 100000	0000 000337 2226	0001 000253 31	000313 4L	3000 730100 0000		0000 R 001047 EPT	0000 1 001042 1	0004 1 000001 L	DODO I DOTOSA MEXO	The state of the s	0003 1 01243/ NITPE	0003_L_012076_RPT	0003 R 007363 TLOC	WANT CERT OF COOL	U003 K 01 + 332 ANE	0004 R 000262 22
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And a final state of the state	0001 000376 12L	17 - 10 - 00 - 10 - 00	1000 1000 1000	0001 000257 2046	192 4 20100 1000		0001 0004°5 35L	0001 000442 56	0003 R 000000 EP	0003 L 011535 FXD		UNIT 0 05110 1 5000	0000 1 001037 LFXD	9000 1 000471 NFXD	0004 R 000E42 R	2 6 2 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	0000 5 00/052 3	0000 R 001051 WORST	0004 R 000132 YY
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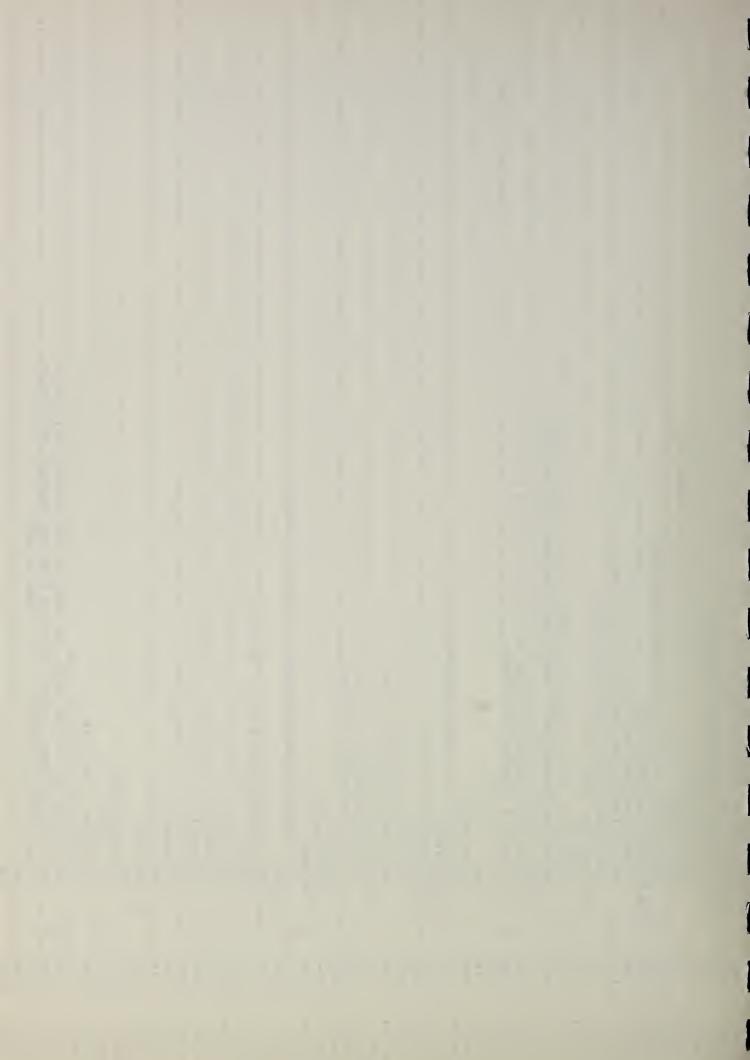
THIS ROUTINE ATTEMPTS TO LOCATE THE LOCATEE BY CALLING LSL OR THE TWO- OR 3-DIMENSIONAL VERSIONS OR LSS. COMMON/CB1/EP(L1,14), LAM(L4), RR(L4), S(L1), TLOC(11,4), W, L1). JEIND, CLK, XNEW, YNEW, ZNEW, EXD(LI), RPI(LI), NTYPE(LI), COMMON/MXYZ/M, L, XX(88), YY(88), ZZ(88), WW(88), R(88), PDIMENSION LAMM(88), NEXD(LI) LOGICAL S.SI (L11) . RPT. FXO. PARAMETER LI=225, Ly=L1+1 SUBROUTINE FINDIT 3.0 * 9 7.8 00101 00103 00105 00105 00106 00100 00100



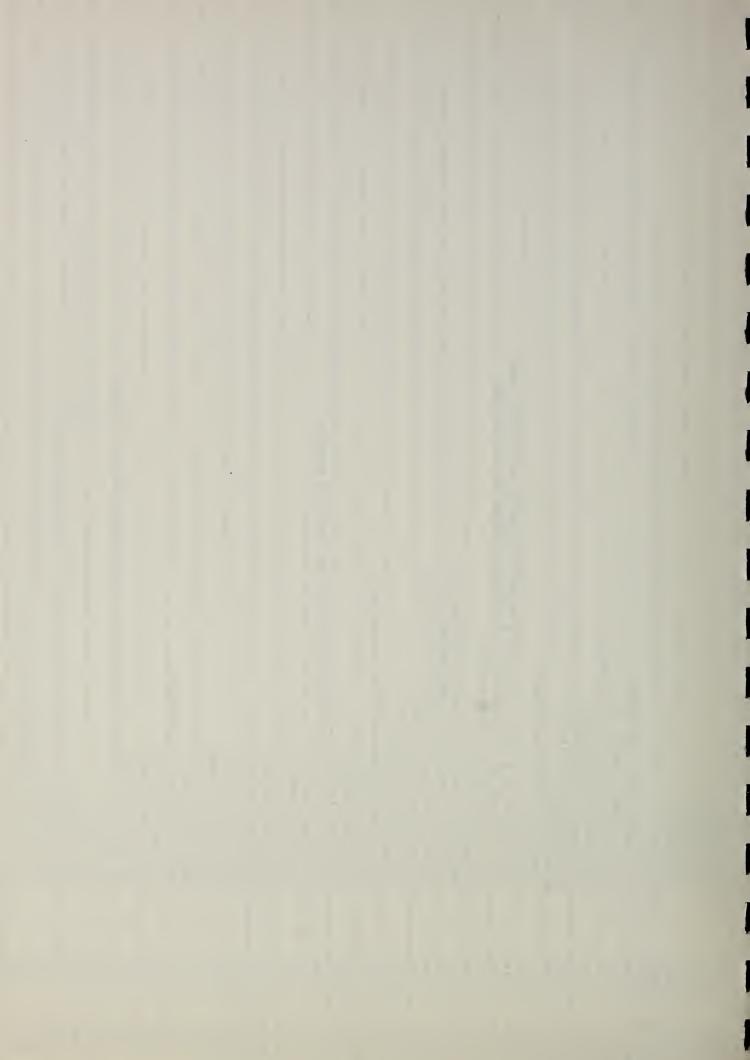
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COUNT THE LOCATORS. KEEPING TRACK OF THEIR POSITIONS. MEIGHTS. AND REPORTED DISTANCES TO THE LOCATEE. EXTRAPOLATE ON TWO PREVIOUS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 THE LOCATEE AND ALL LOCATORS ARE GROUND UNITS, SO LSS-2D IS USED.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    THE LAST ATTEMPT TO LOCATE THE LOCATEE WAS NOT SUCCESSFUL, SO AN ESTIMATE OF THE PRESENT POSITION MUST BE FOUND BY CALLING LSL. FIRST, A SLANT-HEIGHT REDUCTION MUST BE DONE (3-D DISTANCES ARE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         IF (.NOT.S(JFIND)) GO TO 3.
LAST ATTEMPT TO FIND THE LOCATEE WAS SUCCESSFUL. SO AN ESTIMATE
                                                                                                                                                                                                                                                                                                                                                                 IF (TLOCKK, 3) . GT. TLOC (K, 1) . AND . . NOI. F XD (K) ) ... F # ICLK TLOC (K, 3) 1) /
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            IF (TLOC(JFIND, 3), GT.TLOC(JFIND, 1)) F=(CLK-TLOC(JFIND, 3))/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        OF THE PRESENT POSITION MAY BE FOUND BY EXTRAPOLATION.
                                                     IF (FXD (JFIND) . AND . M (JFIND) . GT.O) _WOLD #1 . /W (JFIND) -RVAR
                                                                                                                                                        POSITIONS TO FIND PRESENT_POSITION OF EACH LOCATOR.
                                                                                                                                                                                                                                             IF (RR(1) . GT . RMAX . OR . . NOT . (S(K) . AND . S1(K))) GO TO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 IF (NPLANE. GT. D. OR. NTYPE (JFIND), GT. 2) GO TO 12
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               XHE .. = EP (JF IND , 7) + F . (EP (JF IND , 7) - EP (JF IND , 1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               YNEW=EP(JFIND,8)+F*(EP(JFIND,8)+EP(JFIND,2))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    RR(I) = SQRT (ABS(R(I) ** 2-(ZNEW-ZZ(I)) ** 2))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 IF (RPT(JFIND) . AND . FXD(JFIND)) GO _TO 19
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      IF (RPT (JFIND) . AND . FXD (JFIND)) GO TO 22
DATA SI, RHAX, HMAX, RVAR, FVAR, LFXD, NFXD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    RR(1)= R(1)-.5*(ZNEW-ZZ(1))**2/ R(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    IF (3. + (ZNEA-ZZ(I)) . LT.R(I)) GO TO 4
                  L1**TRUE*,5*E6,200*,36*,40*,L4*1,0/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ZZ(M)=EP(K,9)+F*(EP(K,9)-EP(K,3))
                                                                                                                                                                                                                                                                                                                                                                                                   XX (M) = EP (K, 7) +F+ (Ep (K, 7) -EP (K, 1) 1
                                                                                                                                                                                                                                                                                                                                                                                                                YY (M) = EP (K,8)+F* (EP (K,8)-EP (K,2))
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            1 (TLOC(JFIND, 3)-TLOC(JFIND, 1))
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                                                                                                                                                                                                                                                                                                                                                                               (TLOC(K,3)-TLOC(K,1))
                                                                                                                                                                                                                            IF (RR(11).LT.0) GO TO 2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          IF (M.LT.2) GQ TO 5
                                                                       SI (JFIND) = S(JFIND)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ZNEA=EP (JF IND , 9)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   NPLANE=NPLANE+1
                                                                                                                                                                                                                                                                                                                                                                                                                                    22(4)=EP(K,9).
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                                                                                                                                                                                                                                                                                                                                 (Y)=(K) M(K)
                                                                                                                                                                                                                                                                                                                 R(M)=RR(I)
                                                                                                                                                                                                              LAMM(I)=K
                                      40LU=1.E9
                                                                                                                                                                                             K=LAM(1).
                                                                                                       NPLANE=0
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2 6	73	FROM CANDOO LO MONTH TO THE LANGE OF THE LONG OF THE L
00220	73.	SS 1S CALLED TO HOME
022	74.	TE(6,900) JFIND, S(
23.	75.	900 FORNAT(15,L3,3E14,8,15)
0.2	16.	IF(.NOT.S(JFIND)) GO TO S
023	77.	ALTITUDE OF THE
00233	78.	EIGHT (EPX, EPY, XNEW, YNEW, ZNEW, N
	80.	SO TO IS
0.2	81.0	CCATEE OR A LOCATOR IS AN AIRPLANF, AND LSC2D IS USED TO FIND
23	82.	THE X- AND Y-COORDINATES MORE EXACTLY BEFORE CALLI
00237	83.	13 CALL LOCLSS
23	84.	THE
~	85.	AT LEAST 5 LOCATORS ARE
00240	9 6 6	12 00 33 K=4,10,2
	88	00 32 1#1.M
3	89.	IF (K + (ZNEW-ZZ(I)) + GT + R(I) L=L+1
00251	*06	
06253	414	IF (L.
00255	92.	NUE.
00057	7 70	
00261	92.	SEE CANNOI DE
00262	96*	N (CNITA) OX POLICE OF THE CONTRACT OF THE CON
00264	97.	(, RPT (JFIND)) RETURN
00266	98.	
00267	•66	NWORST = JFIND
00270	100	
00271	102	AS 1 = 0
00272	103.	00 34 1#1.
00275	104.	IF (K*(ZNEW-ZZ(1)) +LT.R(1)) GO TO 34
00277	105.	
00300	106.	RR (L) = R (1)
20500	100	
00303	0 0 0 0	
30	110.	22 (L) ±22 (I)
00305	111.	
90800	112.	34 CONTINUE
00311	7 3	
00312	115.	5530
00313	116.	IF (S (JFIND)) GO TO 15
00315	117.	YPE (JFIND) . GT. 2) GO
00315	118.	THE LOCATEE IS A GROUND UNIT, AND SOME OF THE
00315	119.	AIRPLANES. LSS30 COULD NOT FIND THE LOCATEE. SO
00315	120	THE LOCATORS ARE ELIMINATED, AND LSSZD IS USED
00317		X 1
00320	122.	٥.
00324	124*	1.5
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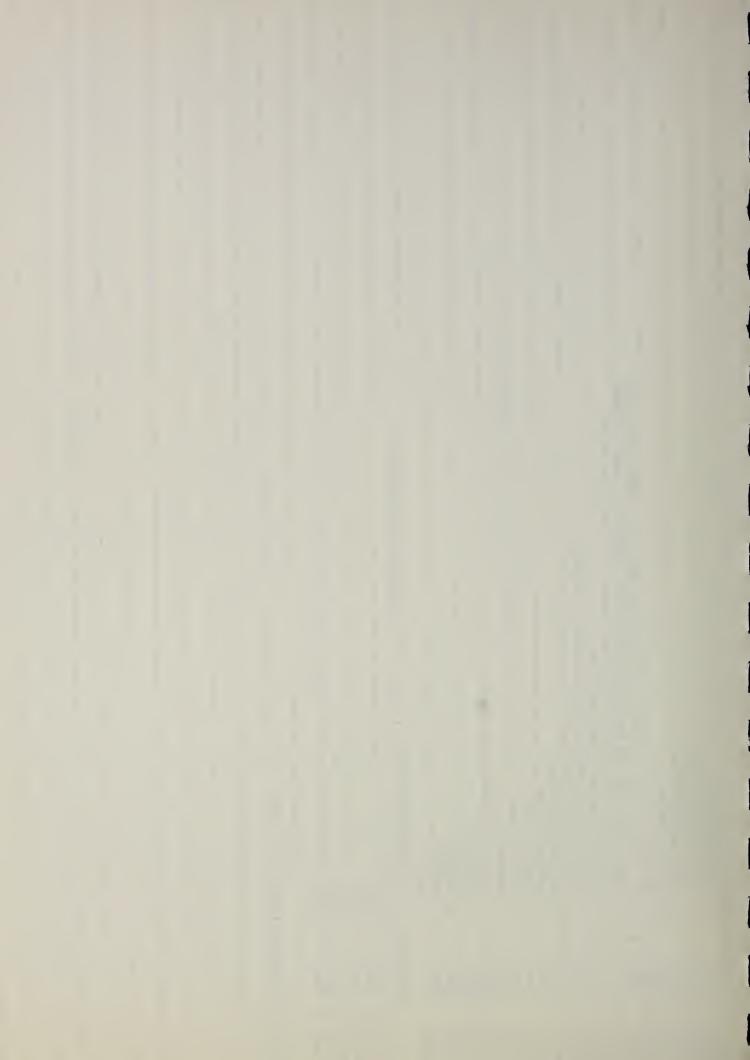


3	126.	XX(M) HXX(I)
00330 1	127.	γ (η) = γ ζ (1)
00331	128.	Z = (W) Z
00332	129.	MIM) = MMI
00333	130•	R(M) RR(I)
00334	1310	DNITNO
00336	1320	O TO 6 HF LOCATEF HAS BEEN
00337	134.	JFIND) GO TO 16
00337	135 . C.	THE LOCATEE IS NOT A
00341	136.	P(JFIND, I) = EP(JFIND, 10)
00342	137.	P.(JEIND, 2) = EP.(JEIND.
00344	139*	T (OT IND S) HET (OT IND FIXA)
00345	140.	W(JFIND) = 1 - / (W(JFIND) + RVAR)
00346	•	
00346	142* C	S A FIXED UNIT, SO A WEIG
00346	200	S ALSO CALCULATED.
00347		
00350	146.	D. 4) + & (OF IND) + XNEW + WOL
00351	• / 1	O C TO THE TWO THE WEWOLDS
00353	149.	0 (FIND) * + 2
00354	150+	NEXD (JFIND) #NFXD (JFIND)
00355	1510	20)2
00356	152	A > 4 > 4 > 4 > 4 > 4 > 4 > 4 > 4 > 4 >
00360	154	EP(JFIND, 2) = YNEW
00361	155*	VE W
00361	156+ C	UPDATE THE ESTIMATED POSITION AND TIME OF LOCATION ARRAYS.
00363	158	FP (JF IND S)
00364	159.	EP(JEIND, 6) = ZNEW
00365	160.	EP(JFIND, 7) #XNEW
00367	162.	FP(JFIND.9) * LYEW
00370	163.	N
06371	164.	Y N E
0 (EP(JFIND, 12) = ZNEW
00374	167*	• F
03	: ~	CLK
0	2	₩ ECL
00377	170.	# _
040	e: N	ELVAIDES TIRES OF LIVE IS
40	· ~	
040	174.	EP(J, J) BXX(I)
040	וחו	EP(1,8) #YY(1)
00406	176.	2 .
2 4	V 0	13)+100
1 50	179*	4)
7	180.	EP(J,2)=EP(J,5)
0 4 1	181	9:1
2 4 2	182	μν (Δ, 4) πΕΡ (Δ, 7) στη
		ואין אין



-	- Company and the Company and
00417 184	EP(J,6)=EP(J,9)
00420 185	
-	
00421 186*	TLOC(J,1)=TLOC(J,2)
00422 187.	TLOC (J. 2) = TLOC (J. 3)
00423 188*	36 TLOC(J,3)=CLK
00425 189	1
_	WANT THE REDORTING TO LINETS TO SE SOLVEN
00425 191+	C REEN FIXED FOR TEN LOCATION OFFICE THOSE THAT HAVE
00425 192.	STATEMENT AND DEMONSTRUCK THE ABOVE RETURN
00425 193+	PRINTERNAL STATE OF THE CARD BELOW.
_	
00430 195*	RPT (NWORSTIBLE ALL SE
-	RPT (LFIND) = TRUE
06432 197.	COLUT SHICKON
00433 198.	NONSTAND
00434 199*	Z Z
00437 200.	
	IF (*(!) • GI WORST) CO TO 35
	WORST="%(L)
	Nº ORSTEL
•	25 CONTINUE
-	RETURN
00447 206.	END
11 40 QN3	
11 1	INVACTION FUNITAIN V COMPILATION. O *DIAGNOSTIC* MESSAGE(S)
PHASE 2 TIME =	0 SEC.
3	ŧ
J	O SEC.
PHASE 5 TIME =	1
-	0 > 5 C +

TOTAL COMPILATION TIME . 3 SEC



ENTRY POINT 000464 SUBROUTINE LOCUSE .

STORAGE USED (BLOCK, NAME, LENGTH)

000501	003176	000000	013000	000673
• C 0 D E	0000 *DATA 003176	. BLANK	CB 1	MXYZ
0001	0000 .	0002	0003	0000

EXTERNAL REFERENCES (BLOCK, NAME)

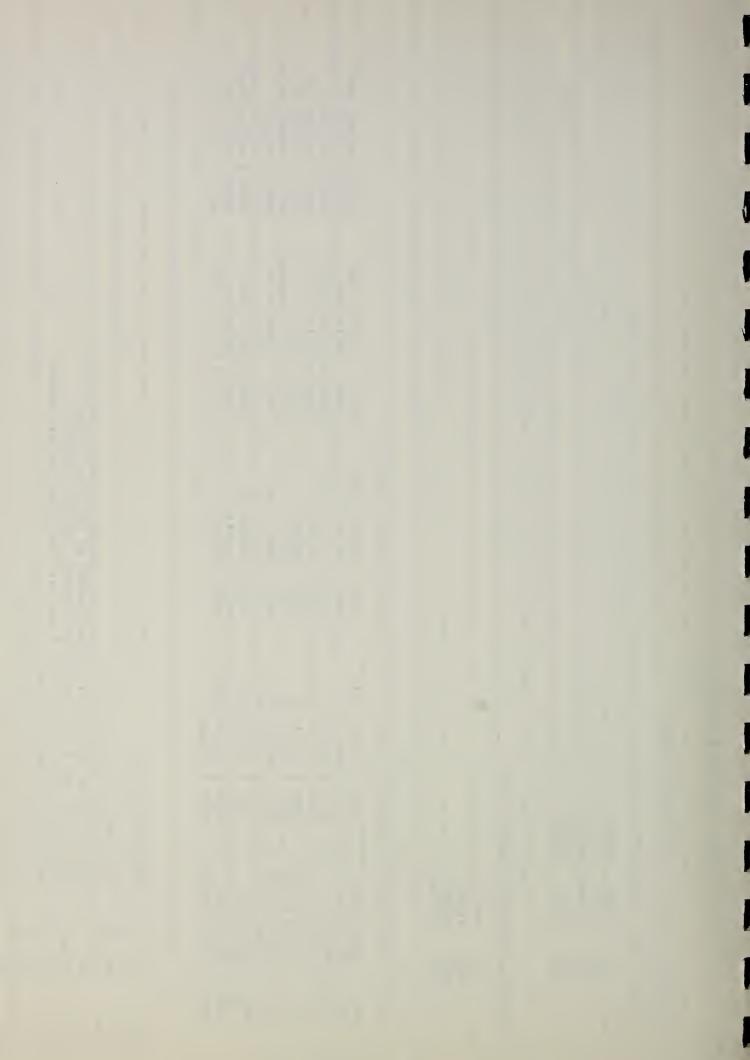
	•		
			-
	-		•
NWOUS	N1025	NEXPIS	NERRA
0005	9000	0000	0010

STORAGE ASSIGNMENT FOR VARIABLES (BLOCK, TYPE, RELATIVE LOCATION, NAME)

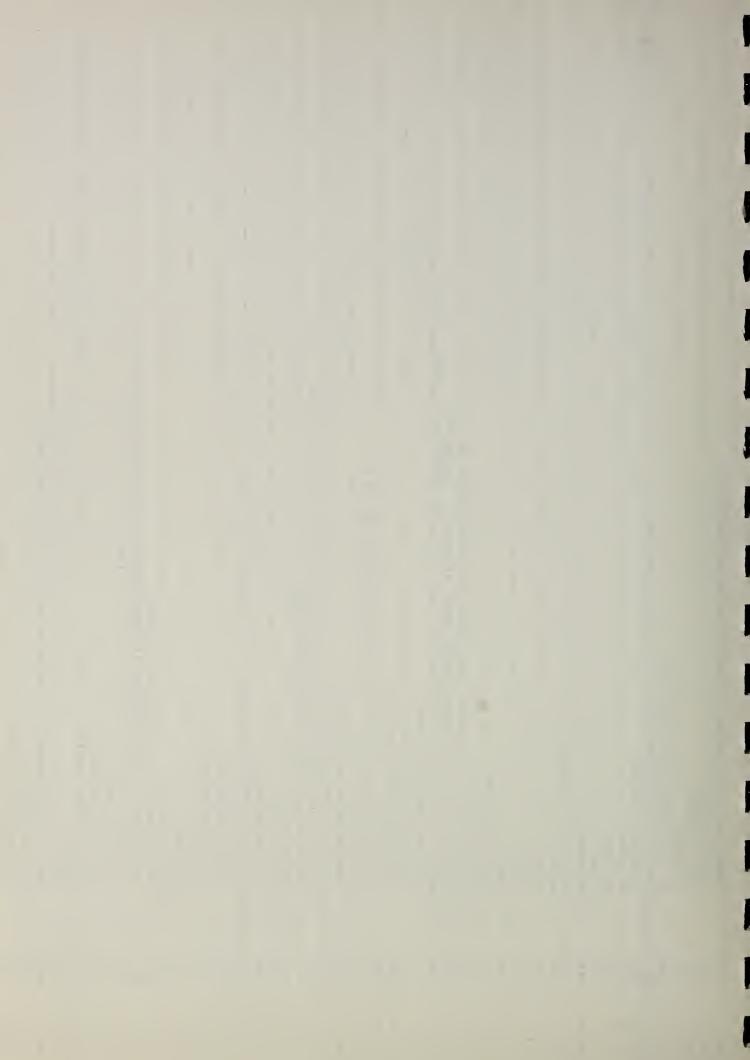
				-							
0001 000376 2416	0000 R 00000 A	0000 R 003116 D	0003 R 011535 FX0	0004 I 000000 M	0000 I 003101 NELIM	0004 L 000672 P	0003 R 007343 TLOC	0000 R 002260 VRS0	0000 R 003111 W1	0004 R 000132 YY	
0001 000333 2166	0000 003126 99F	0000 R 003122 CUTOFF	0000 R 003120 F	0003 I 006116 LAM	0000 I 003114 NBEGIN	0003 I 012437 NTYPE	0003_L_007022_S	0000 R 003121 VAR	0004 R 000412 WW	0003 R 011533 YNEW	
0001 000247 2006	0001 000352 8L	0003 R 011531 CLK	0003_R_000000_EP	0004 1 000001 L	0000 I 003125 N	0000 I 003113 NOFF	0003_R_006460_RR	0000 R 003106 UZ	0003 R 011167 W	0004 R 000002 XX	ы бо чутуну пудавы аражыны аражандаганын, акамаматурану акуретурганун айылгалдагандаларда кымамат
0001 000044 1416	.0001 000177 44	0000 R 001440 C	0000 R 003 24 ELIM	0000 I 003115 K	0000 I 003 23 MLINE	0000 I 003103 NN	0003_R_012076_RPT	0000 R 003105 U1	0000 R 003110 V2	0003 R 011532 XNEW	0004 R 000262 ZZ
0001 000035 1356	0001 000173 31	0000 R 000620 B	0000 R 003117 E	0003 1 011530 JFIND	0000 1 003102 MELIM	0000 1 003104 NLINE	0004_R_000542_R	0000 R 003100 TOL	0000 R 003107 V1	0000 R 003112 WZ	0003 R 011534 ZNEW
											-

SUBROUTINE LOCLSL	LEAST SQUARES LINEAR (LSL). THIS BOUTINE MINIMIZES THE SUM OF THE SOURCE DISCLOSURED	LOCATEE TO THE RADICAL AXIS LINES FORMED BY PAIRS OF CIRCLES.	DISTANCE TO THE LOCATEE FOR ITS RADIUS. SEE FIRST INTERIM REPORT	THIS IS THE TWO-DIMENSIONAL ROUTINE.	PARAMETER L1=225, L4=L1+1 DIMENSION A (400), C (400), VRS0 (400)	JEIND. CLK, XNEW, YNEW, ZNE
SUBR	CLEAS	C LOCA	C DISI	C THIS	PARA	COMP
1.	е • •	5.9	7 *	607.	110	13.
00101	00101	00101	00101	00101	00103	00105

COMMON/CBI/EP(L1,14),LAM(L4),RR(L4),S(L1),TLOC(L1,4),W(L1),



0	- 2	Control of the Contro
00100	* C +	N/1412/11-144/08/11/180/122/86/198
7 -	17.	TOT TOT VED
	8 8 1	TRUE.
	19.	F (P) WRITE(6,99) JFIND, CLK
2 1 2	200	ORMAT (* * LSL2D;
210	+ N	
212	3	ELIM
212	3	3
210	25.	2 NCINE#O
012	27.	U2±0,
013	8	0 = 1 Å
	29.	
. m	31.	W2ED.
5 1 3	32.	F = 1 ,
510	• • •	OFF+1 DATE OF CARCIES TO THE THE THE CONTRACTORY OF
3	2	AXIS LINE A*X+B*Y-C#O, WHERE A*A+B*B#1.
013	9	ENTS OF THE TWO EQUATIONS IN
00137	37 + C	INTERIM REPORT.
7	39.	1F (NI 1NF » FD » 400) GO TO 4
114	40+	
7	+ 11 +	×·
 	V. C	NE+1
510	• • 1 3 7 3	H K
0.15	45.	=RR(L) ** 2 - RR(K) ** 2+XX(K) ** 2
2 2	46*	D=A(NLINE) +A(NLINE) +B(NLINE) +B(NLINE)
210	* / h.	
015	464	NL INE)+
910	0	NLINE) .
910	υ 1. 1. 1. 4.	2 Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z
2 - 0	53.	N L N L N L N L N L N L N L N L N L N L
316	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
516	55+	
	56*	D = U + V 2 - V 1 + U 2
	• •	ABS(U), LE.ABS(U1*V2)) RETURN FM OF TWO FOHATIONS IS NON-STACHLAB
217	59. C	E SQUARED DISTANCES TO EACH
	•09	≖.TRUE.
	61*	XNEw=(#1+V2-V1+W2),D
	No	*#2-#1*U2.7.
	0 0 0	•
020	. 29	(A (M) *
020		VRSQ(M)
0 0	67 +	FLOAT (
020	*69	· GT · NEL 1 M
021		** (4-MELIM)
00212	71.	T L I Z F B Z F B Z F B
4		N. I. L. E. C.

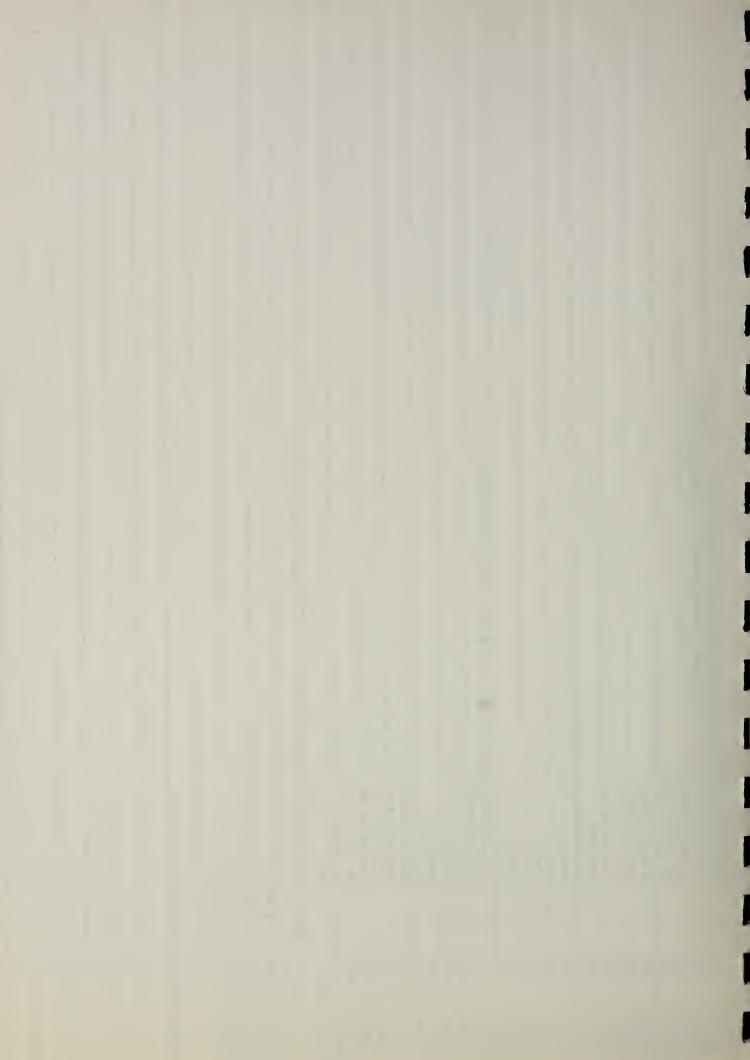


	. QNW	* 50.7	96700
	. 60 109	1	00255
	9 12 2 2 2 C(N) *F	_	00253
	V2 12 V2 + B (N) + F		00252
			00251
			00250
			00247
			00246
	FEB (N / O		00245
	D A (N) + B (N) + B (N)		00244
			00240
THE TWO LINEAR EQUATIONS.	TS OF THE TWO		00237
	1,1 2 ≈ 0 •		00237
	W. # C		00236
	• C H C N	88	00235
	U2=0.	-	. 00233
	U1=0.		00232
	Í		00230
	8 CONTINUE		00226
			00225
	A (NLINE) = A (N)	000	00224
	NLINE=NLINE+1		22200
	IF (VRSO(N) GT ELIM GO TO A	7.8 *	00220
	DO 8 N=1,MLINE	77.	00215
7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	TE MENAGE		00214
	INATE RADICAL AXES WHOSE SO	* 17	00214
	ELIM#CUTOFF*VAR		
	The second secon		ш

END OF UNIVAC 1108 FORTRAN V COMPILATION. O SECONO PHASE 1 TIME # PHASE 2 TIME # PHASE 4 TIME # PHASE 4 TIME # PHASE 5 TIME #

O +DIAGNOSTIC+ MESSAGE(S)

2 SEC TOTAL COMPILATION TIME =



WILLY LOCK S. LOCKS UNIVAC 1108 FORTRAN V LEVEL 2206 0018 F5018P
THIS COMPILATION WAS DONE ON 05 MAY 72 AT 11:41:47

SUBROUTINE LOCLSS ENTRY POINT 000276

STORAGE USED (BLOCK, NAME, LENGTH)

					:
					. 1
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		I			
	_				
636	0000 +DATA 000300	000	000	261	673
00	00	000	130	02	00
0	0	0	0	a	_
ш	4	¥			:
000	DAT	BLA	9.1	33	X Y 7
•	•	٠	Ū	Ü	Σ
_		7	~	4	5
000	000	000	000	000	000
Ü		C		J	

EXTERNAL REFERENCES (BLOCK, NAME)

0006 NEXP15

STORAGE ASSIGNMENT FOR VARIABLES (BLOCK, TYPE, RELATIVE LOCATION, NAME)

								ı					-	
0001 000512 2,	0001 000032 4L	0000 000175 82F	0000 R 000153 DFDX	0000 R 000165 DSQ	0000 R 000000 EE	.0000 R.000132 FRAC	00004 I 000000 IN	0005_1_000001_L	0000 1 000136 MRELOC	0005 L 000672 P	0003 L 007022 S	0003 R 011167 W	0005 R 000132 YY	
	0001 000551 3226	0000 000173 81F	0000 R 000160 DELYSQ	0000 R 000161 050	0000 R 000143 EAVE	0000_R_000167_F	0000 1 000141 11	D000 I 000135 K	0000 1 000140 MELIM	0000 R 000137 OLDEAV	0000 R 000150 RSQ	0000 R 000147 V	0003 R 011533 YNEW	
	0001 000324 2546	0000 000170 80F	0000 R 000157 DELXSQ	0000 R 300154 DGDY	.0000 R 000146 E	0000 R 000151 F	0000 1 000144 1	0003 1 011530 JF.IND	00000 1 0000 M	0003 1 012437 NTYPE	0003 R 006460 RR	0000 R 000156 TW	0005 R 000002 XX	
	0001 000220 25L	0001 000203 BL	0000 R 000166 D	0000 R 000162 DGDX	0000 R 000164 DY	0003 R 000000 EP	0000 R 000152 G	0000 1 000145	0000 1 000134 LR	0000 1 000131 NRELOC	0003 R 012076 RPT	0003 R 007363 TLOC	0003 R 011532 XNEW	0005 R 000262 22

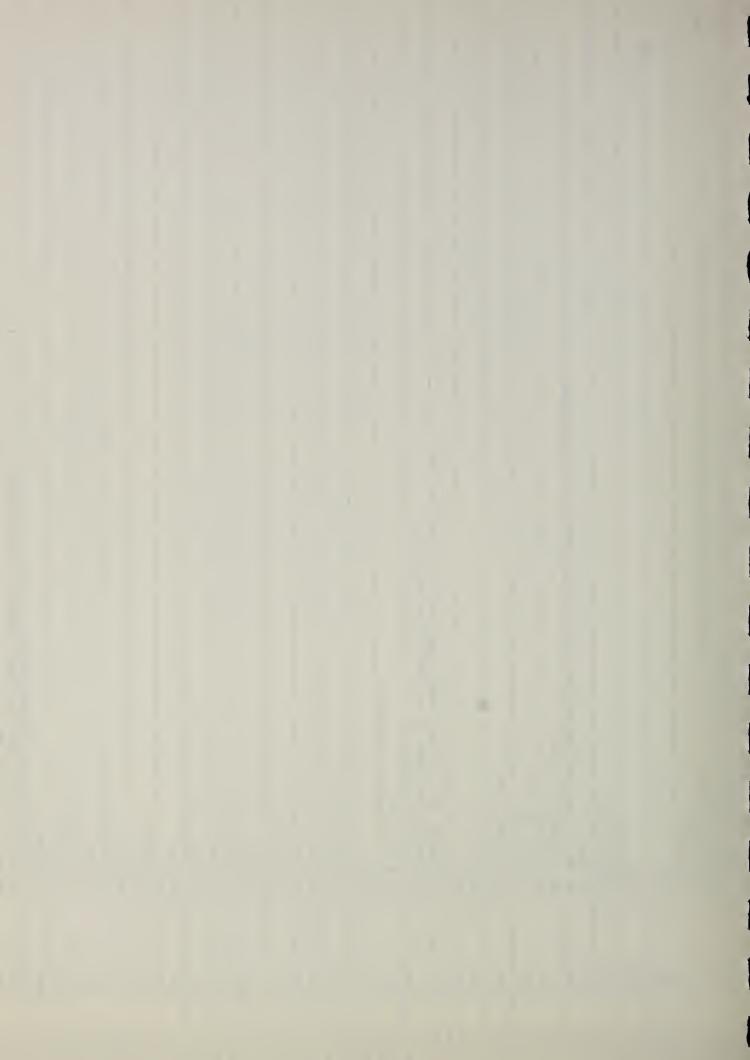
	SQUARES_SQUARED_ROUTINE. IT	LEAVE BY FINDING A POINT WHERE	ITS DERIVATIVES F AND G. WITH RESPECT TO X AND Y ARE ZERO. TO DO	A T 10 N •			RR(L4).5(L1).1LOC(L1.41).W(L11.	JFIND, CLK, XNEW, YNEW, ZNEW, FXD(L1), RPI(L1), NTYPE(L1)		9 (88) % (88) % (88) % (88) % (88) % (88) % (88) % (88) % (88) %
SUBROUTINE LOCLSS	THIS IS THE TWO-DIMENSIONAL LEAST SQUARES SQUARED ROUTINE.	ATTEMPTS TO MINIMIZE THE FUNCTION EAVE BY FINDING A POINT WHERE	ITS DERIVATIVES F. AND G. WITH RES	THIS, IT USES NEWTON-RAPHSON ITERATION.		PARAMETER L1=225, L4=L1+1	COMMON/CB1/EP(L1.14).LAMKL41.RR(L41.S(L1).STLOCAL1.41.WAL11.	. UFIND, CLK, XNEW, YNEW, ZNE	COMMON /CB3/IN (600 2), 19	COMMON/MXYZ/M,L,XX(88),YY(88),ZZ(88),WW(88),R(88),P
•	2. C	3.		2 • C	9 • 9	7.	8.	9.6	10.	11.
10100	00101	10100	00101	10100	10100	00103	00104	00104	00100	00100

DIMENSION EE (88)

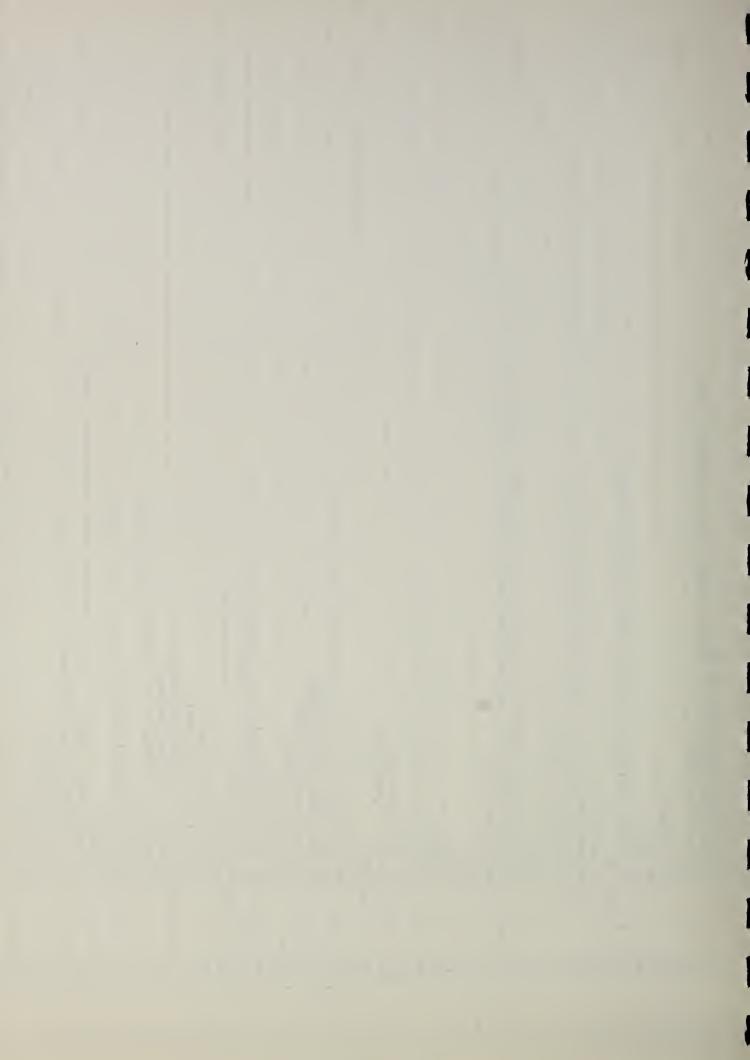
00107



00174 55. \$Z(1)=E 00175 56. E=R(J) 00175 56. R(J)=R(I) 00177 59. R(J)=R(I) 00177 59. E=R(J) 00202 61. R(I)=E 00203 62. I=LAM(J)=LAM(I) 00203 62. I=LAM(J)=IN(I)=IN
74 55.
74 55
74 55• $ZZ(1) = E$ 75 56• $E = R(J)$ 76 57• $R(J) = R(J)$ 77 58• $E = R(J)$ 80 59• $E = R(J)$ 91 60• $RR(J) = R(J)$ 92 61• $RR(J) = RR(J)$ 93 62• $I = LAM(I)$ 95 64• $LAM(J) = LAM(I)$ 96 65 $LAM(J) = LAM(I)$
74 55• ZZ(1)=E 75 56• E=R(J) 76 57• R(J)=R 77 58• E=RR(J) 90 59• E=RR(J) 91 60• RR(J)=RR(I) 92 61• RR(I)=E 93 62• II=LAM(J) 94 63
74 55• ZZ(1)=E 75 56• E=R(J) 76 57• R(J)=R 77 58• E=RR(J) 59• E=RR(J) 50 59• RR(J)=RR(I) 51 60• RR(J)=RR(I)
74 55• ZZ(1)=E 75 56• E=R(J) 76 57• R(J)=R(1') 77 58• R(I)=E 30 59• E=RR(J)
74 55• ZZ(1)=E 75 56• E=R(J) 76 57• R(J)=R(1) 77 58• R(1)=E
74 55•
73 54*
71 52.
70 51•
404
64 47 6 5 48 4
S.*
61 44.
55 41+ 56 42* L=L+1=K
53 40* 1F(EE(1), LE, ELIM) GO T
45 37 C ELIMINATED LOCATORS AT 47 380 ELIMEEAVE & 2 - (3 - MELIM)
35+ I
43 334 4 MELIM#MELIM+1
37 31
34 29*
30 27 C OR DIVERGENCE OCCURS.
MELIM=0
126 23• I
124 21•. 125 22•
2 19* 3 20*
120 17• 1N(19,1)=0
00115 15 LOGICAL P 00116 16 DATA P/-FALSE /



	The state of the s	
00217	710	ELOC+1
00220		0C+GT+NRELOC) GO TO 25
00220	7.50	RELOCATE THE LOCATORS. IF NRELOCAD (SEE DATA STATEMENTS), THIS
2		
022	9	CALL RELOC
00224	77.	MELIM#O
20	79. C	CALCU
22 6	61.0	
9 69 69	80.00	2 X Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z
23		
00237	87. C	NEWTORN-RAPHSON ITERATION. CALCULATE F. G. AND THEIR DERIVATIVES.
00237	88	ND DY, AND INCREMENT XNEW AND YNEW.
00243	906	d l
00244	91.	0=9
00246	93.	DF0 X ≡ U • D G 0 Y ≡ U • D G 0 Y ≡ U • D G 0 Y ≡ U • D G 0 Y ≡ U • D G 0 Y ≡ U • D • D G 0 Y ≡ U • D • D G 0 Y ≡ U • D • D G 0 Y ≡ U • D • D G 0 Y ≡ U • D • D G 0 Y ≡ U
00247	944	DFDY # C + O
00250	• 56	# O # E E E E E E E
00251	-	R, R2, D2
00252	. 98•	petin delita alexandra addenination unioni esc
00256	100+	
00257	101*	SQ = (XNEW-XX(I))
00260	102•	IYNEW-YY (1)) ** 2/RS
00262	• + 0	LXSQ+0ELYSQ) +R Q-1,+DELYSQ
00264	105	(I) = E + E + R S Q
00264	107 ° CC	IF (P) WRITE(6,
00265	108	81 FORMAT(9£14.8)
00267	10.	
00270	1110	E. (YNEW-YY(I)) .W
00272	113.	
00273	114*	FDY=DFDY+2 . * (XNEW_XX(I)) * (
00275	115*	
00300	117.	VE • G • U V E A
00301	118*	GOX=DFDY
00302	1190	* 0 0 0 × 0 0 × 0 0 0 0 × 0 0 0 0 × 0 0 0 0 × 0
00305	1210	DX=(DEDY=6-000V*F);E
00306	122*	DY = (DGDX + F - DFDX + G) / E
00307	1230	X NEW + CX
031	125.	YNEWEYNEW + DI COLETAND + AMAXIO 100 - FOR ANCION 1 T T T T T T T T T T T T T T T T T T
3	126° C	IE (P) WRITE(6.82) DX.DY.XNEW.YNEW.E.G.EAVE
00	127	NEW, YNEW, DE/DX, DE/DY, EA
		L URB



YNEW.							
THE ITERATION DIVERGED. DO NOT CHANGE XNEW AND YNEW. 2 STOP=, TRUE.	RETURN	SUBSOUTINE RELOC	DSG=(XNEW-XX(I)) ++2+(YNEW-YY(I)) ++2	D=.5*(D+DSQ/D) D=.5*(D+DSQ/D)	THE KAL OLD AND AND AND AND AND AND AND AND AND AN	1. ZZ(1) #ZZ(1) +F * (ZNE W = ZZ(1))	END
J			-				
129*	131*	1336	135.	138	404	142	5 5 7 7
00313	00315	00316	00324	00326	00331	00333	00336

END OF UNIVAC 1108 FORTRAN V COMPILATION. O .DIAGNOSTIC. MESSAGE.S. 0 SEC. 0 SEC. 1 SEC. 1 SEC. PHASE 1 TIME B PHASE 2 TIME B PHASE 3 TIME B PHASE 4 TIME B PHASE 5 TIME B

TOTAL COMPILATION TIME = 2 S



SUBROUTINE LSS30 ENTRY POINT 000310

STORAGE USED (BLOCK, NAME, LENGTH)

					ŀ
					- - -
			-		
					·
			:		
9	. 2	0	0		
121	032	000	013000	226	790
00	00	00	0	00	00
L	4	NK			
dóo	DAT	BLA	8 1	93	MXYZ
•	•	•	. U	U	Σ
100	00	0.5	0003 CB1 013000	40	0.5
0	00	0	00	00	00
į		Ì			
				-	

EXTERNAL REFERENCES (BLOCK, NAME)

The state of the same of the s	NEXP18	0007 NERR35	0010 NWOUS	NIOZS
The state of the s	0000 NEXP1	2000	0100	1100

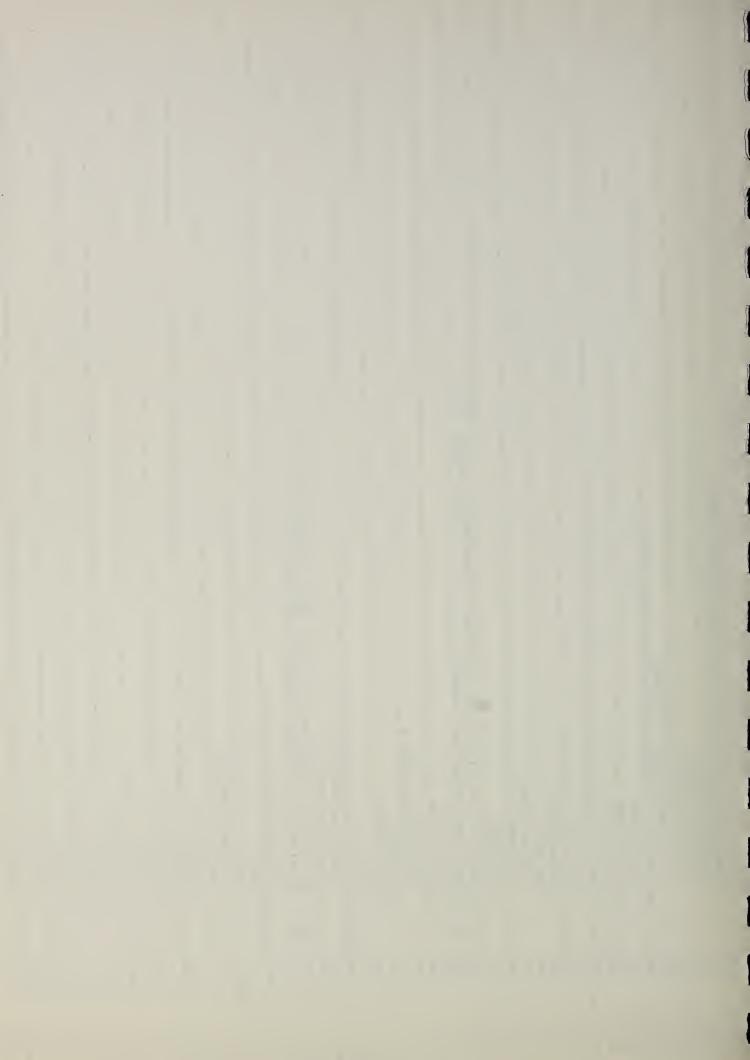
STORAGE ASSIGNMENT FOR VARIABLES (BLOCK, TYPE, RELATIVE LOCATION, NAME)

0001 000040 4L 00001 000040 4L 00000 R 000170 DELXSQ 00000 R 000160 DFDX 00000 R 000165 DHDZ 00000 R 000152 E 00000 R 000131 EX 0000 R 000131 FRAC 0000 I 000144 II 0000 I 000135 K 0000 R 000135 K	
0001 000102 1436 0000 000214 9F 0000 R 000202 D 0000 R 000174 DETINV 0000 R 000177 DE 0000 R 000177 DE	UNUS R UNUZAZ ZZ
0001 000022 133G 0001 000341 260G 0000 R 000145 CUTOFF 0000 R 000173 DET 0000 R 000176 DY 0000 R 000156 PY 0000 R 000156 F 0000 R 000157 H 0000 I 000157 H 0000 I 000151 J 0000 I 000132 NRELOC 0000 R 010132 NRELOC	WOUNT TO THE MENT OF THE MENT
0001 000010 1L 00001 00026 25L 00001 001062 5L 00003 R 011531 CLK 0000 R 000175 DELZSQ 0000 R 000175 DX	Commence of the control of the contr
0001 000234 231G 0001 000234 231G 0000 R 000164 5L 0000 R 000171 DELYSQ 0000 R 000161 OFOY 0000 R 000147 EAVE 0000 R 000147 EAVE 0000 R 000142 EY 0000 R 000142 EY	

SUBROUTINE LSS 1D	THIS SUBROUTINE IS THE 3-DIMENSIONAL LEAST SOURCES METHOD	IT MINIMIZES A FUNCTION, EAVE, BY TRYING TO GET ITS 3 DERIVATIVES.	(F.G.+ RESPECTIVELY).WITH_RESPECT TO X. Y. AND 7 TO RE 7 FRO	NEWTON-RAPHSON ITERATION IS USED TO APPROACH THE TERRES		PARAMETER LIM225, Lum 1+1	COMMON/CB1/EP(L1,14), LAMILA), RRII 4) SKI 1) TI OCK 11	
•	2.0	3 • C	40	2.	9	7.	8.	
_	-th	_	1	-		3	4	
0100	10130	0010	10100		00100	00103	00100	



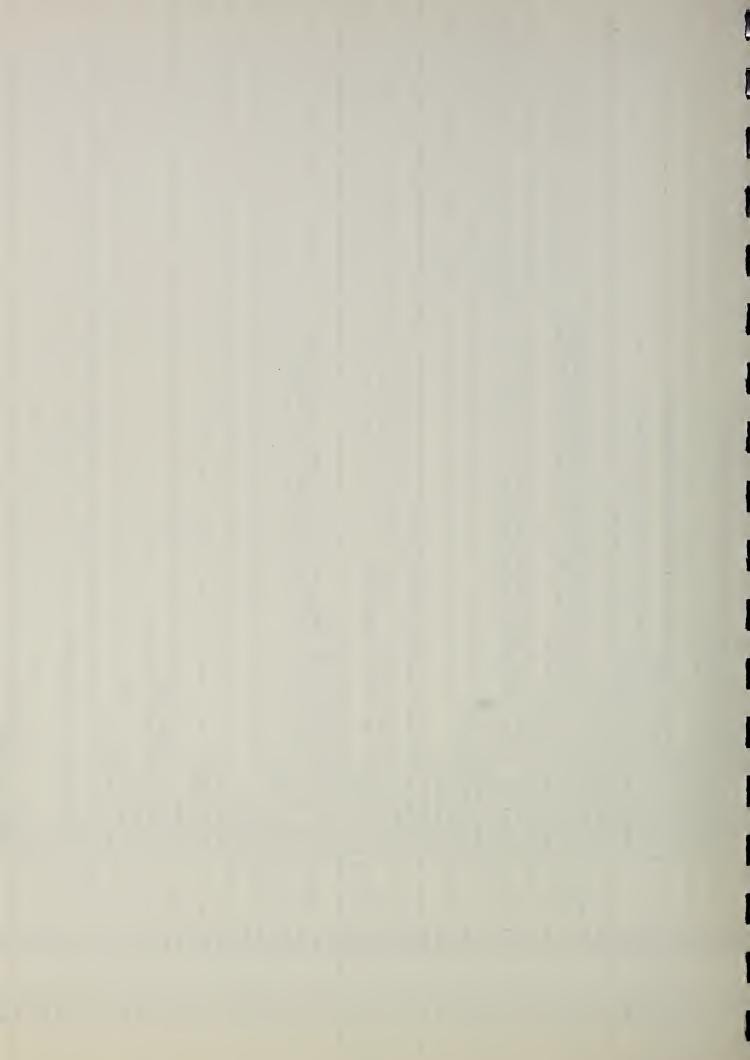
n.		JO . CCK . XNE . S. TNE W . ZNF W . FXD . 1 1 BET
00105	• 01	V(600,2),19
20100	-	L, XX (88
00110		98)
00111		Processor ACVIO
00111	15 • C	IF (P) WRITE(6,99) JFIND,
00116		SS
00117		IN (19.2) # 0
00120	→ ~	R 10
00122		X # 0
00123	ľ	MRELOC#O
00124		1 STOP=,FALSE,
00126		0LDEAV=1.6E30
00127		0
00130	28.	EY=10000.
00131	29 ¢ C	O FOUR ITERATIONS, STOPPING IF CONVERGENCE OCCUES OF
00132		THE FIRST ITERATION DIVERGES.
00135	32*	60 10
00137	33.	TON (11, K
00140	346	IF (S (JFIND)) G
00144	າ ຕ ດ ຊາ	2
00145	37.	X=0
00146	38+	67.
00150	39.0 40.0 40.0 40.0 40.0 40.0 40.0 40.0 4	** (3-MELIM)
00151		OFF #FAVE
00151	42° C	0
00155	, ਅ ਹ ਹ ਹ	
00157	45*	1
00160	46.	-
00161	+ 7 +	IF(1.EQ.J) GO TO 5
90164	+6+	E H S. A. C. L. + S. M. C. L.
. 59100	50.	Ш
00167	5.2 *	E=XX(J) xx(J)=xx(T)
00170		
00172	. n.t.	(1
00173		YY(J) = YY(I)
00174	57*	<u>i</u> =
00176	58.	
00177	*09	2. (1) = E = R(J)
00200	61*	R(J) ER(I)
00201	62.	1
00203	0 4	E+RR(J) RR(J)=RRR(I)
00204	65*	L
50200	66.	
		The state of the s



		l. I
1 DHDZBDHDZ+(E+	1234	מאס מיני
DGDY=DGDY+(E+Z**DELTS DGDZ=DGDZ+Z**(YNEW+YY	122.	00302
DFDZ=DFDZ+Z+(XNEW=XX	120	00200
DFDX=DFDX+(E+2.*DELXSQ)*WW(1)	1184	027
G=G+E (YNE%-YY(1)) * WW(1) HHH+E (ZNE%-ZZ(1)) * WW(1)	1116	00275
THT + E + (XX C L L) + WW	115	00273
	113*	00271
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SUBROUT!	9 7 6	00241
C AND FIND DX, DY, DZ BY SOLVING EQUATIONS (5)	91.	00240
RETURN CALCULATE F. G. H AND	906	06240
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	79*	00224
C RELOCATE THE LOCATORS.	77*	00222
B MRELOC*MRELOC+1 IF (MRFLOC.GT.NRELOC) GO TO 25	75.	00221
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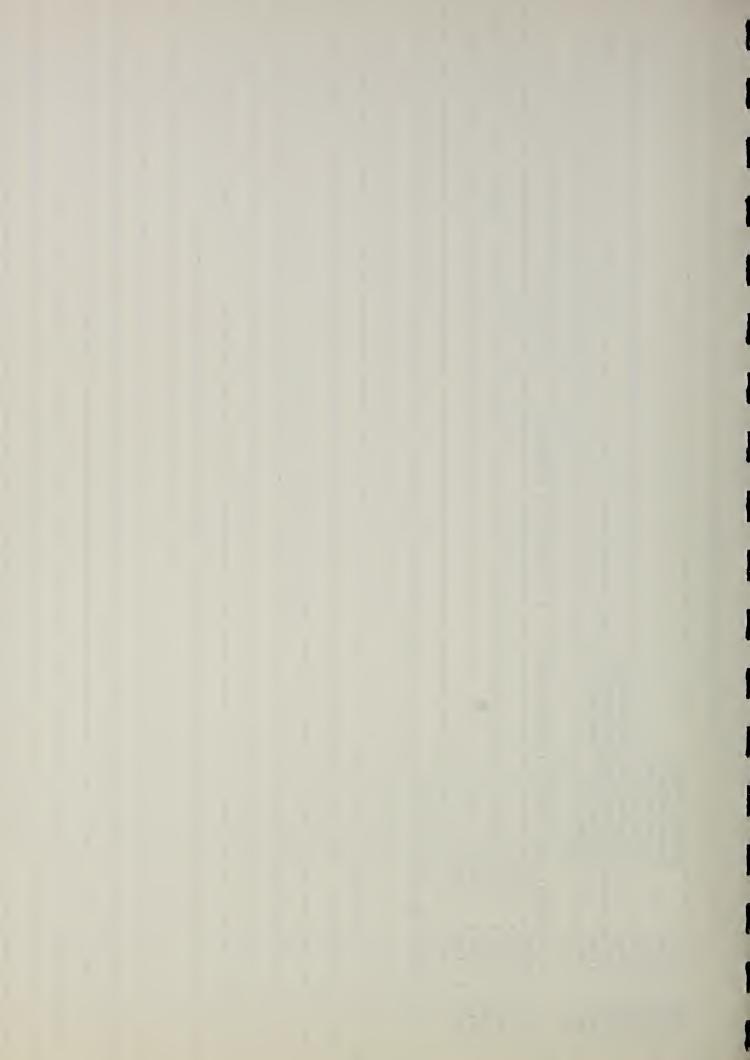
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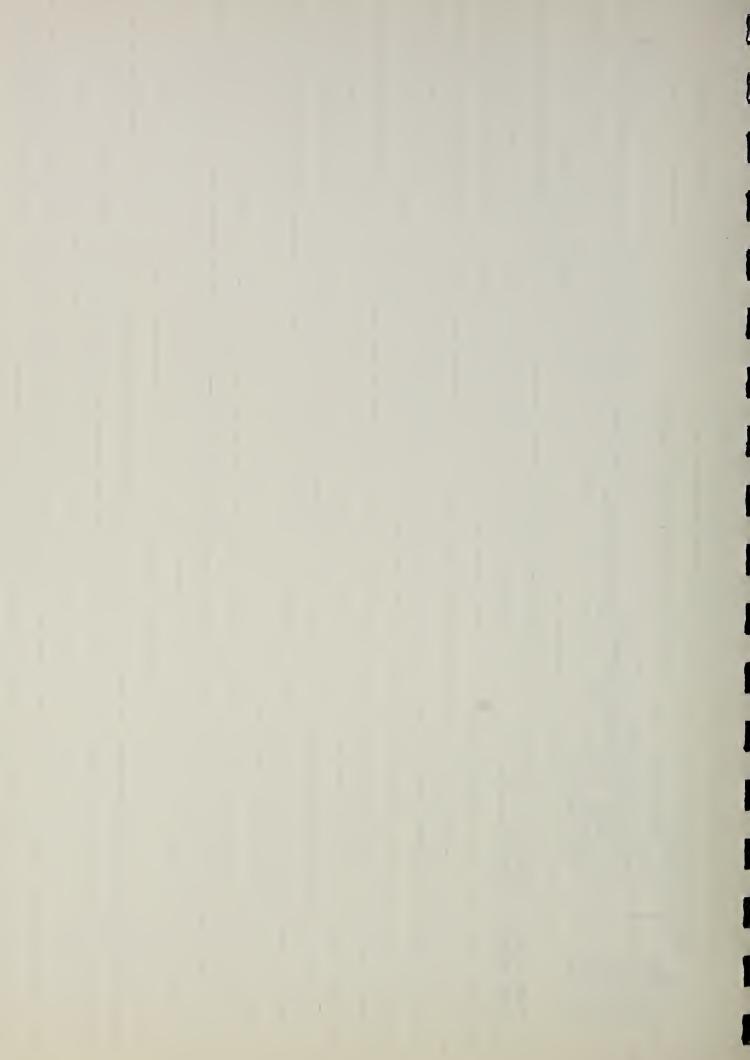
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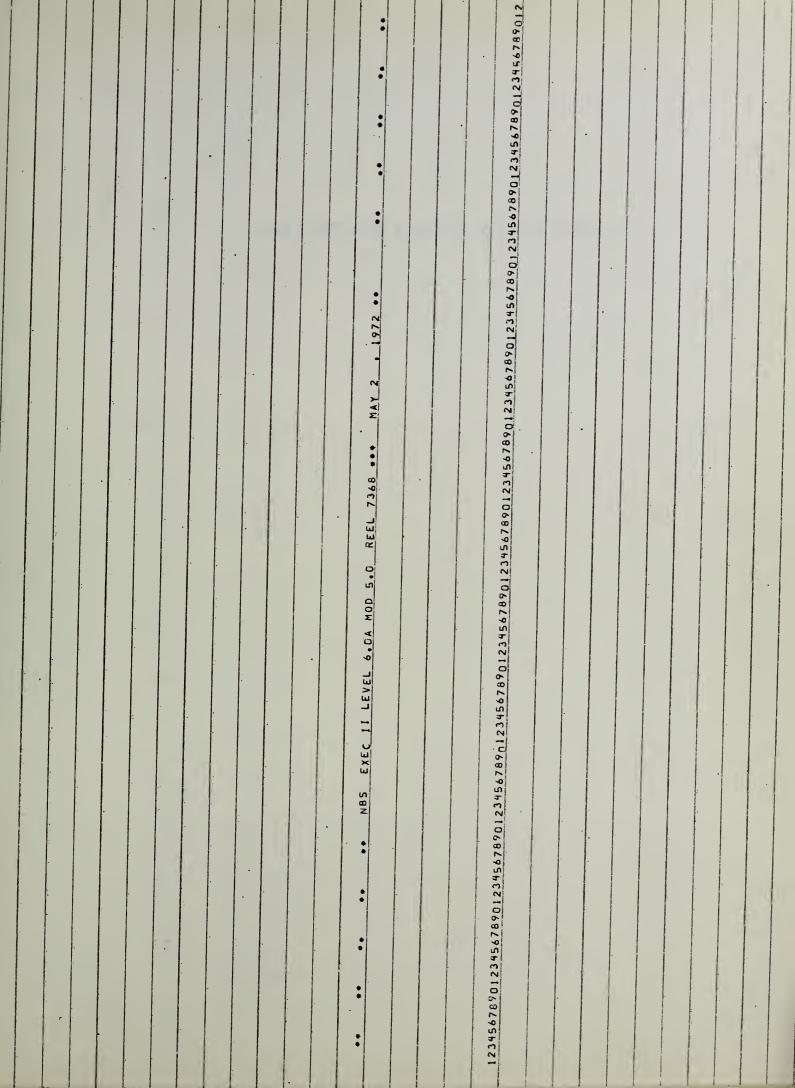


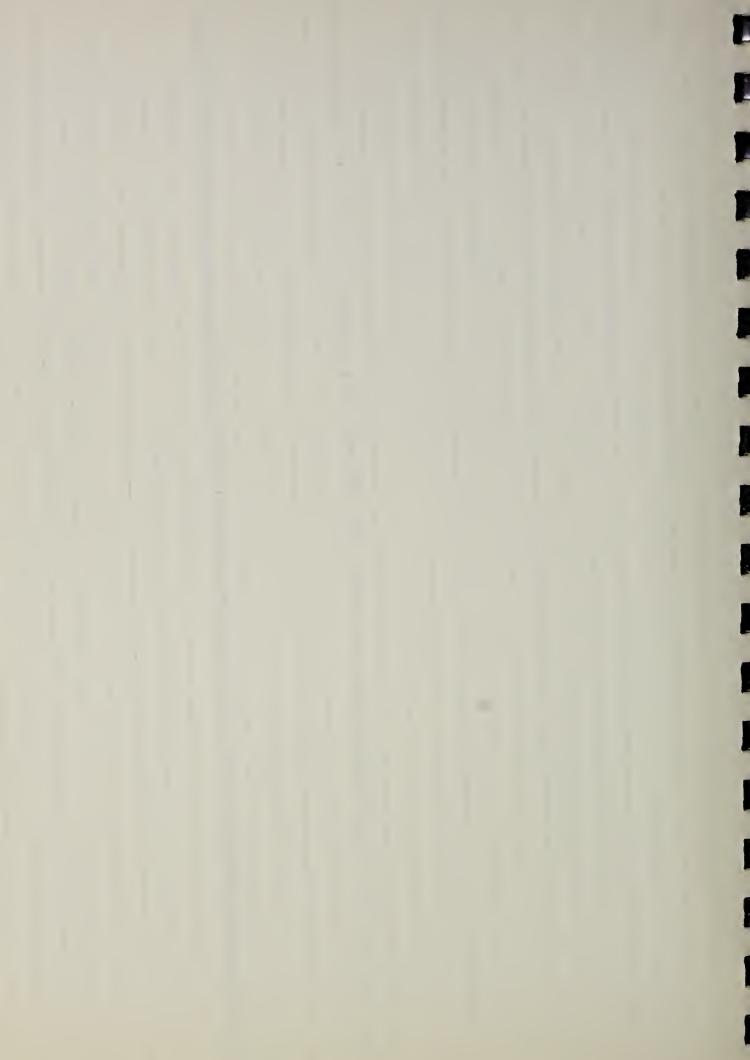
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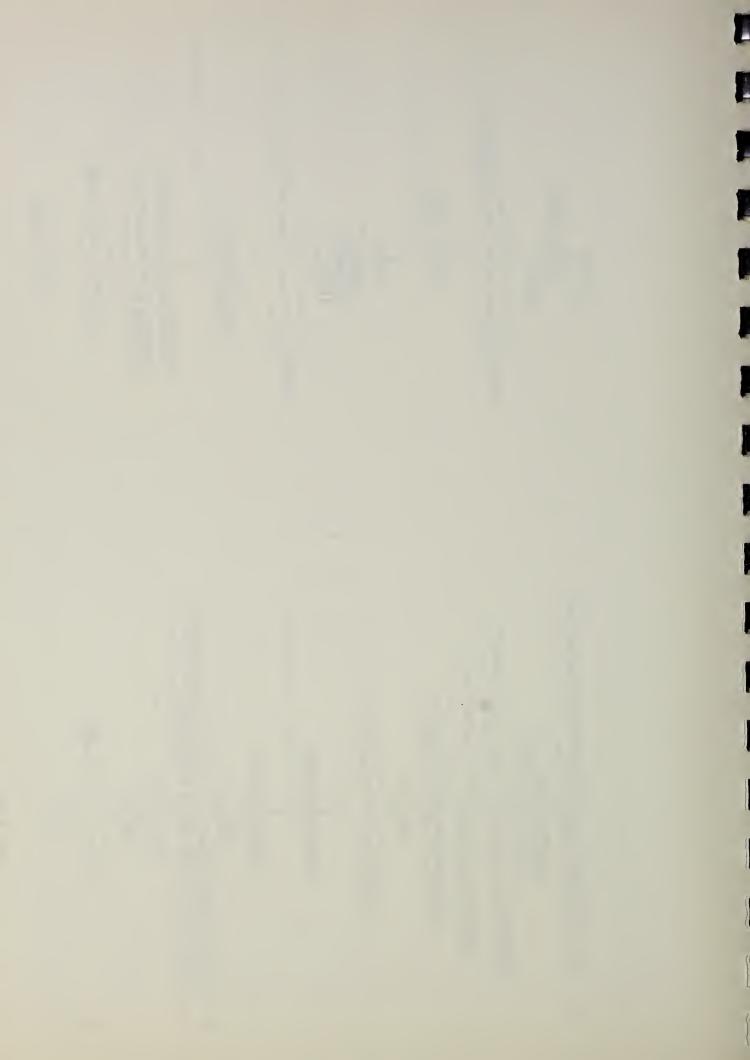
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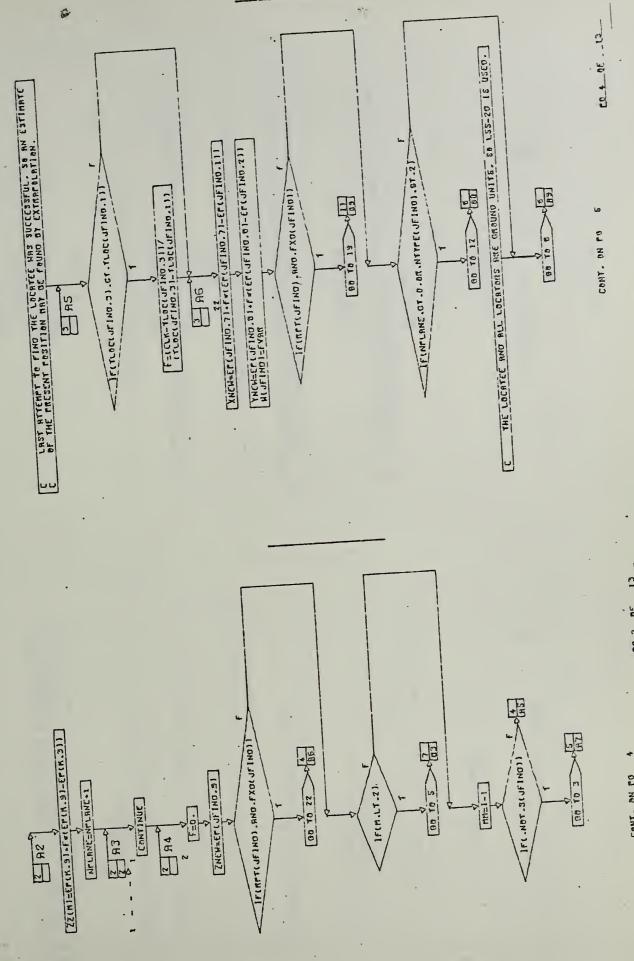
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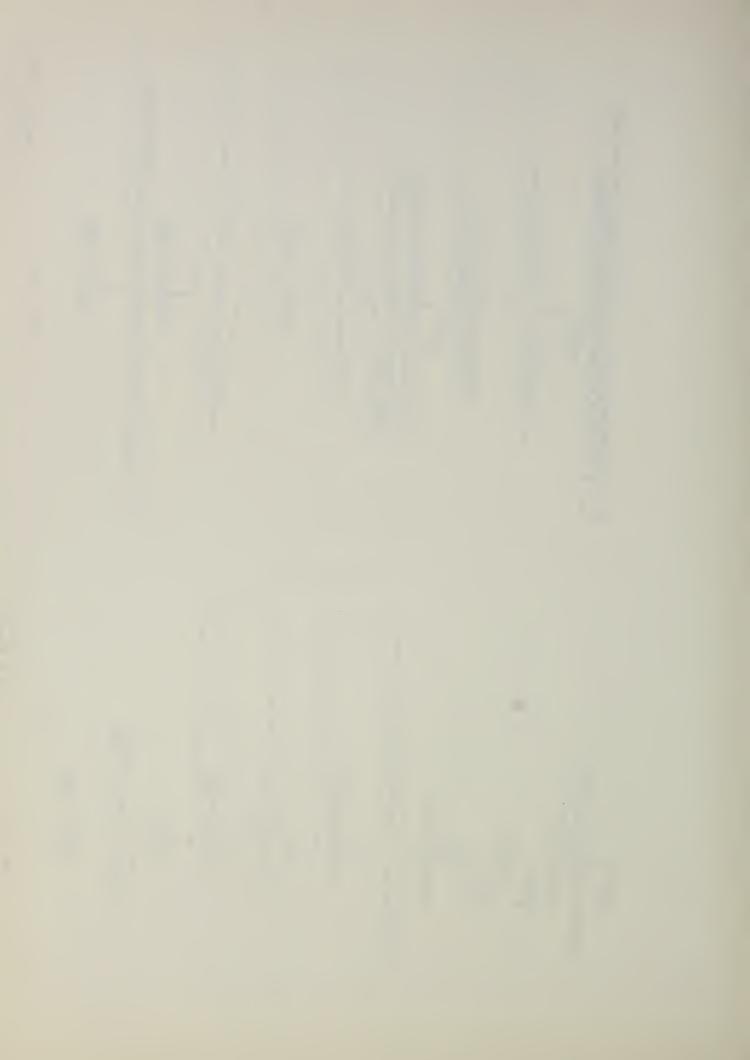
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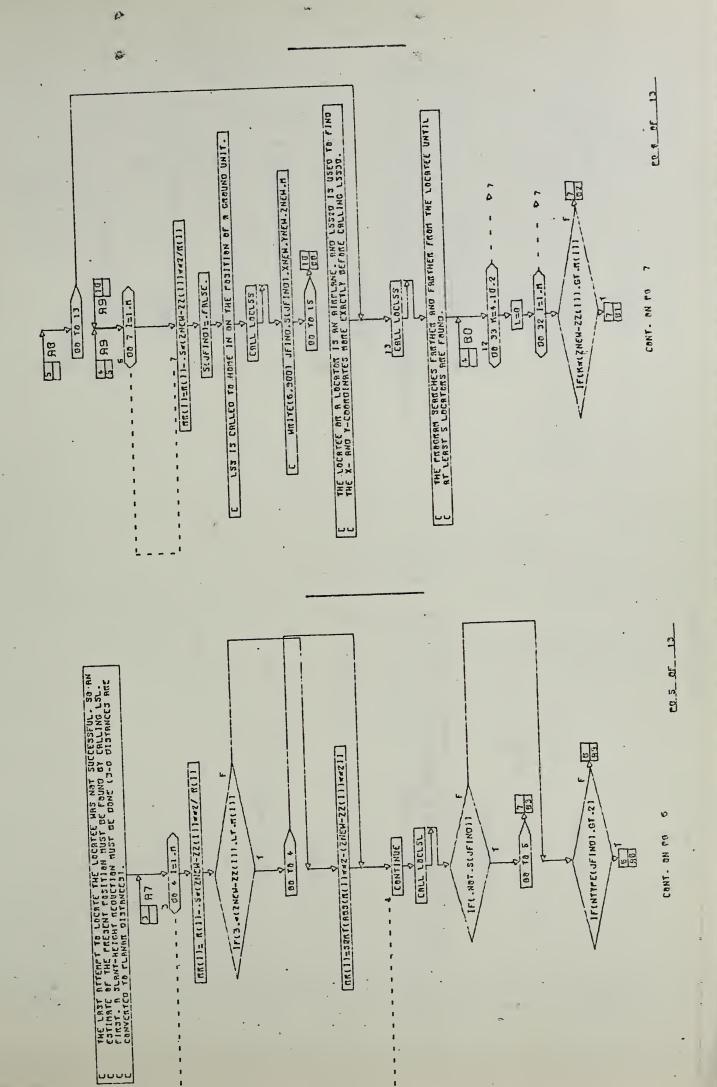
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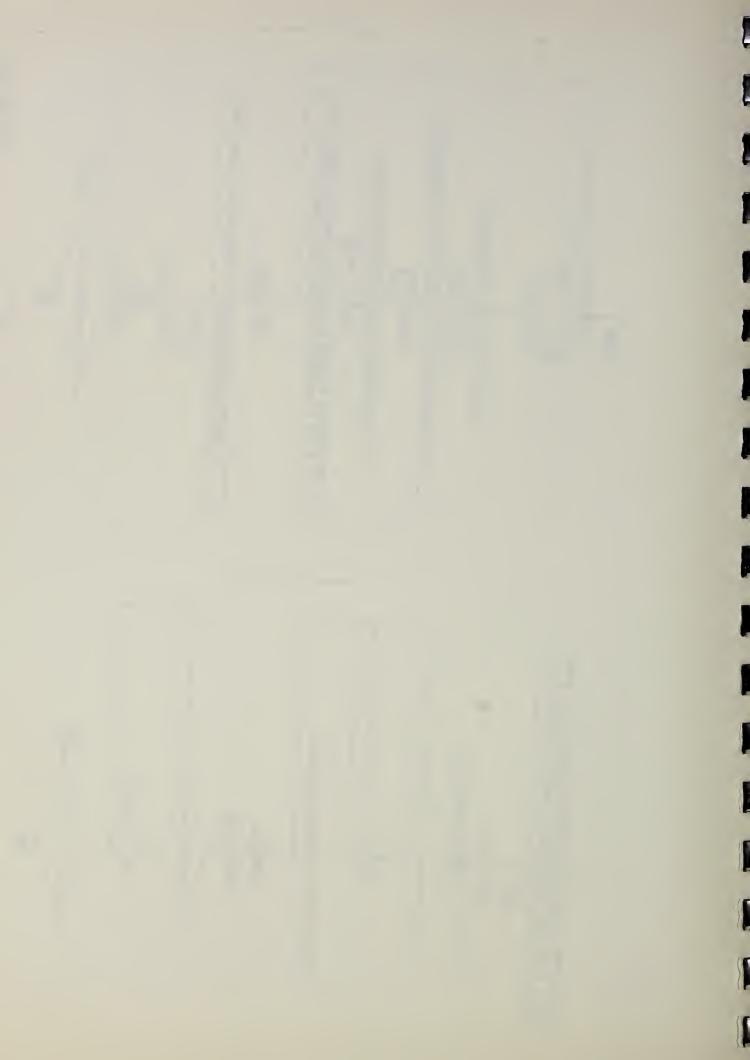


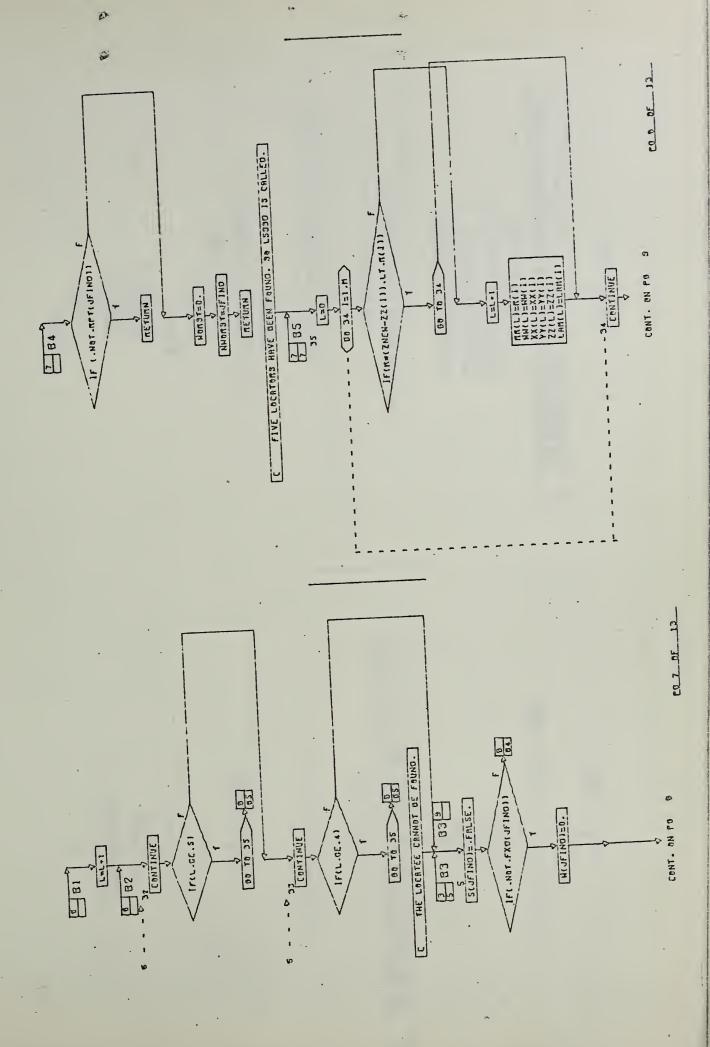


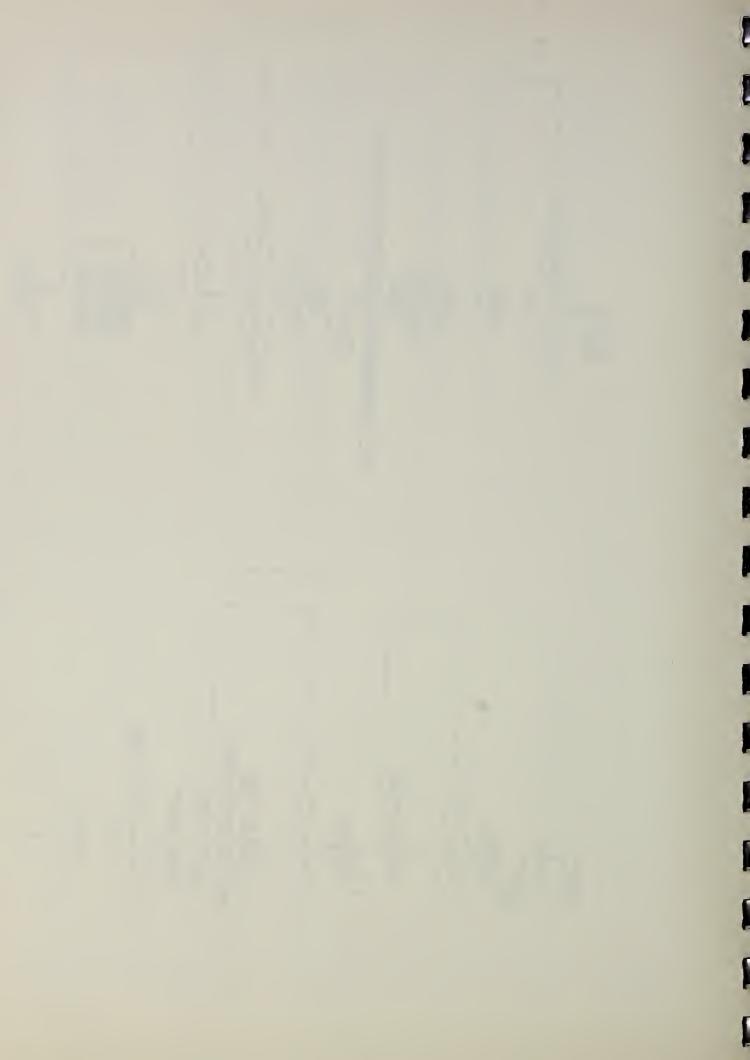
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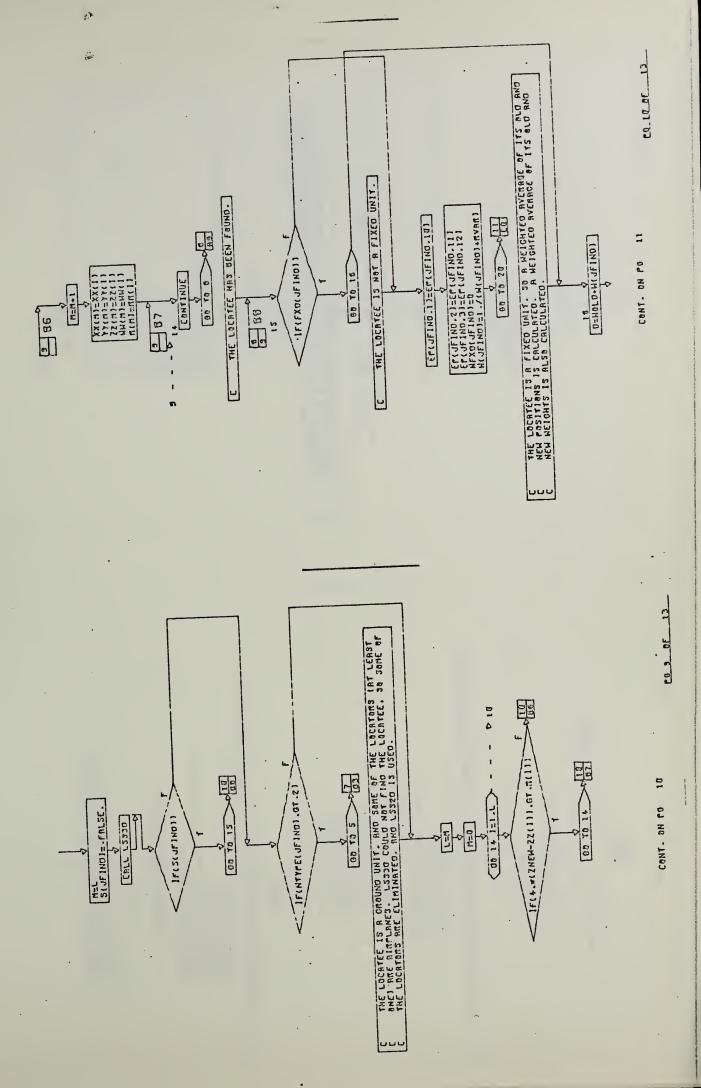


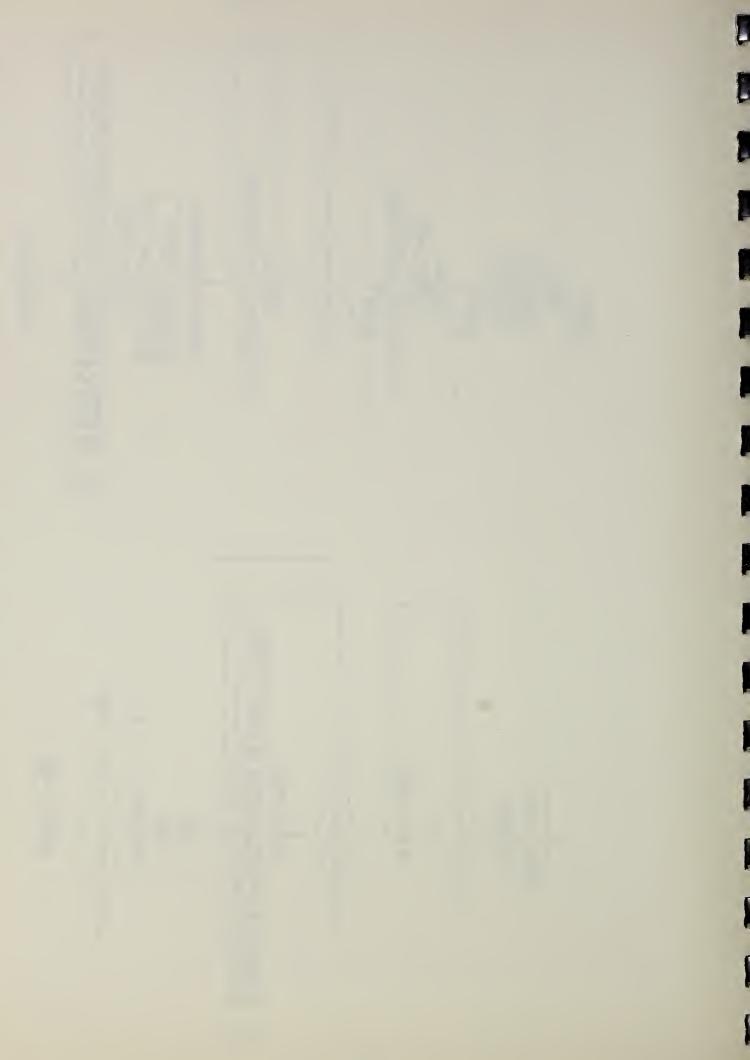


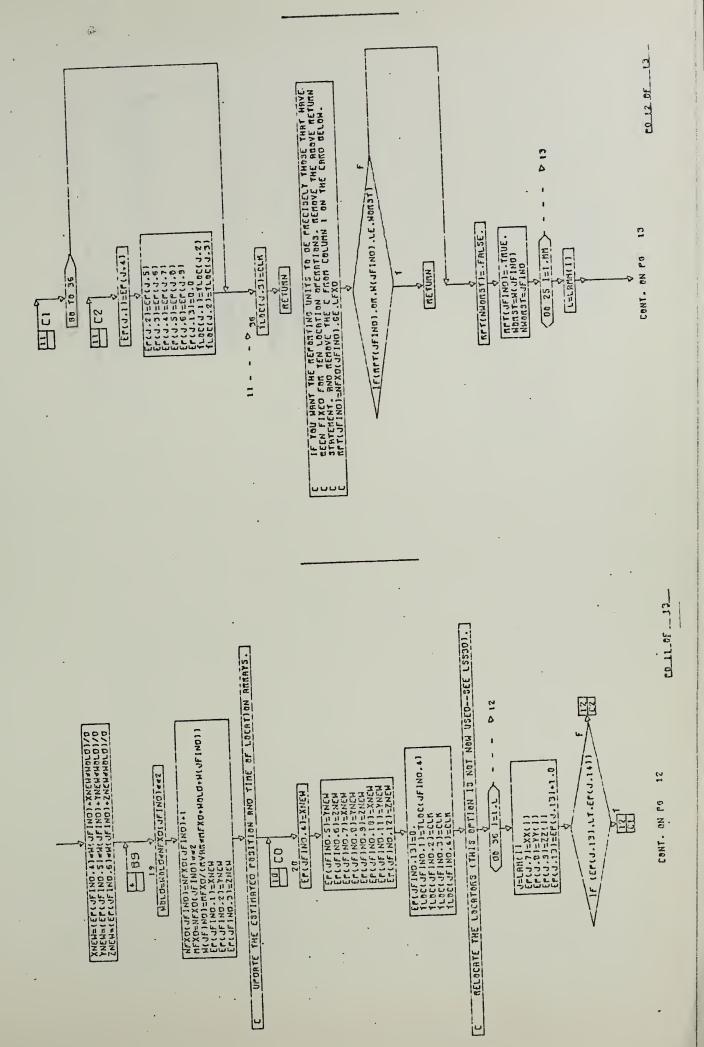


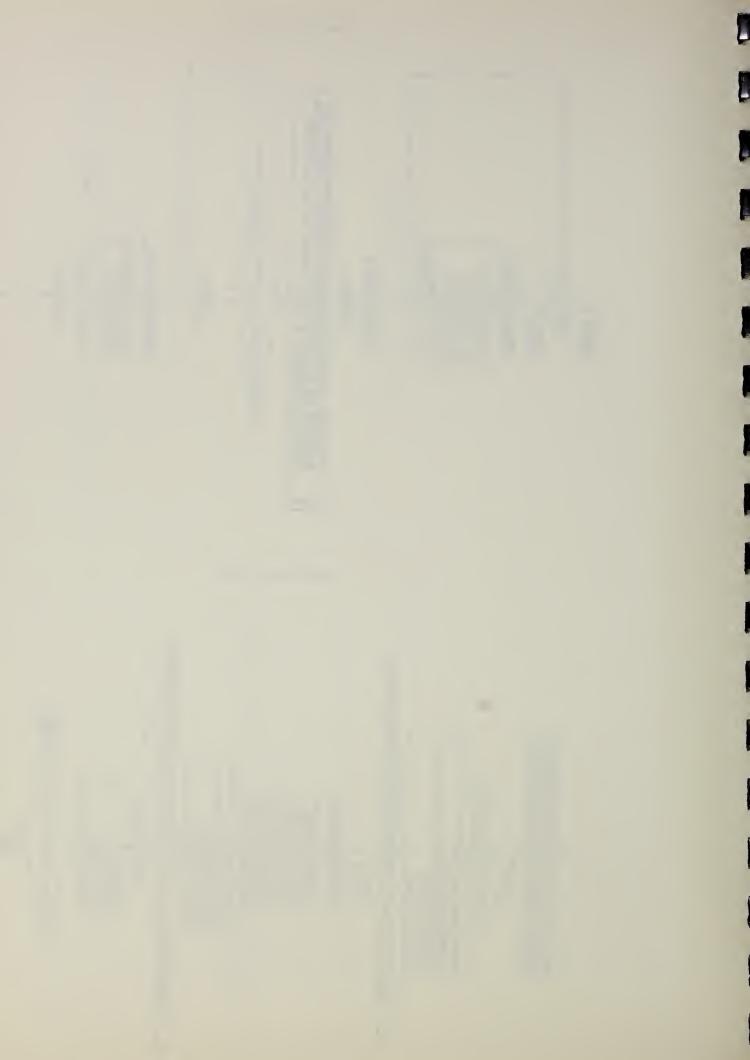


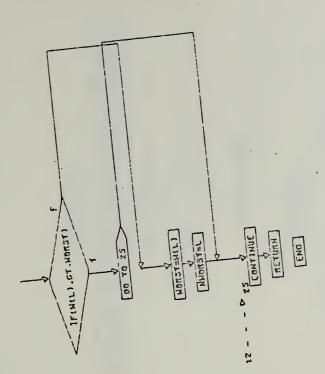




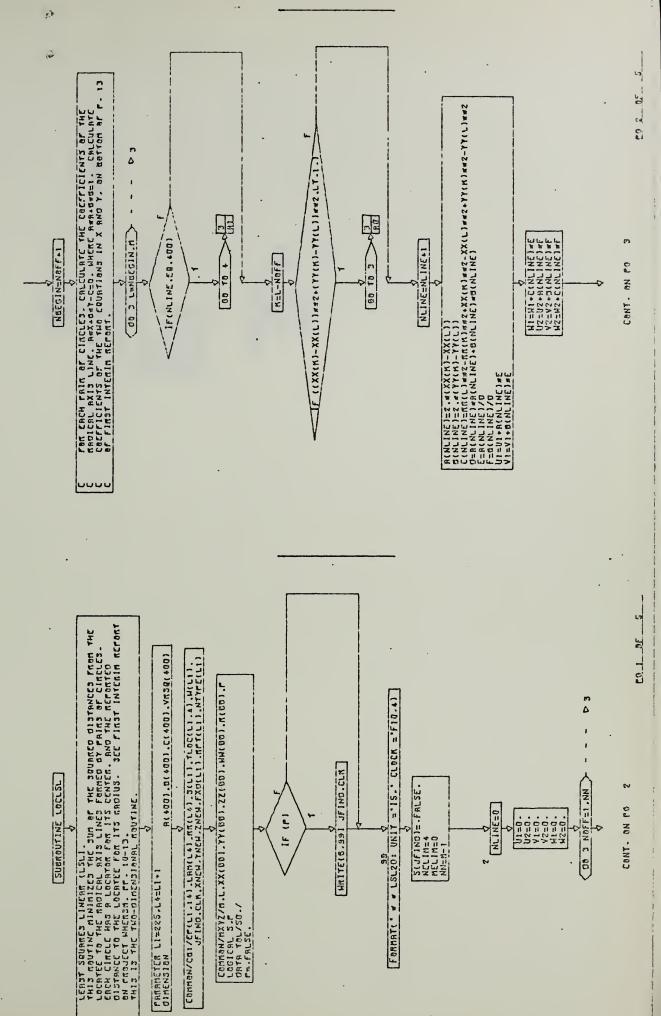




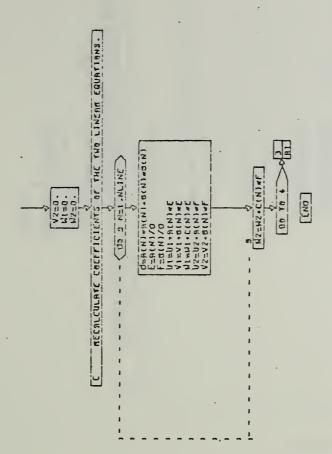


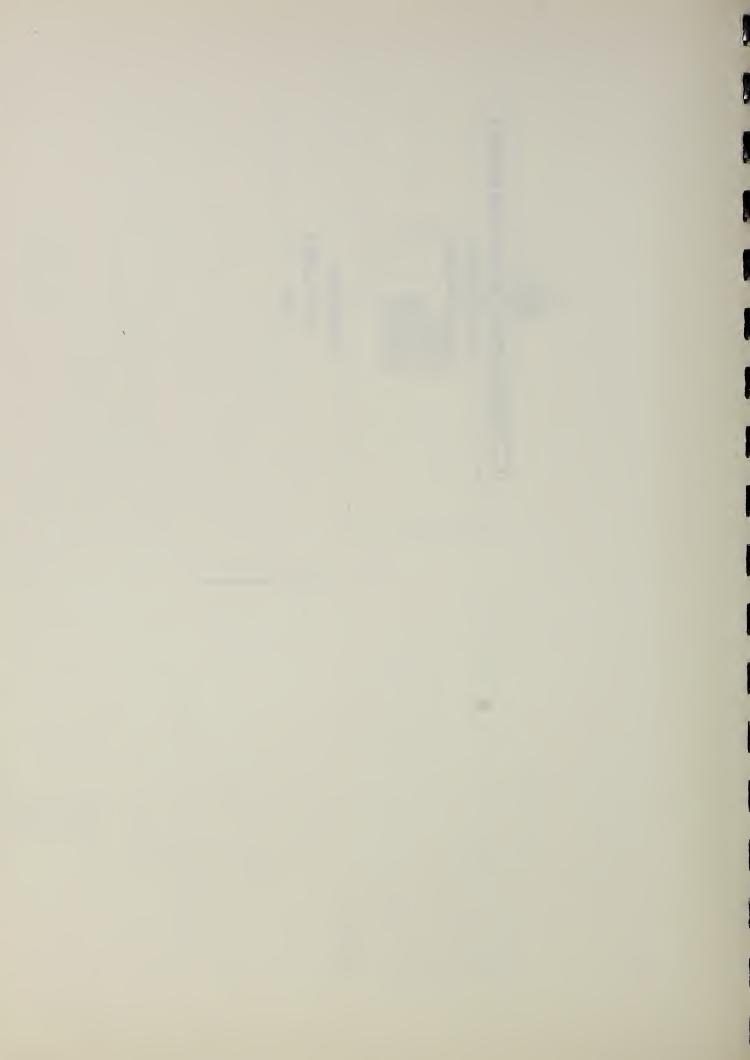






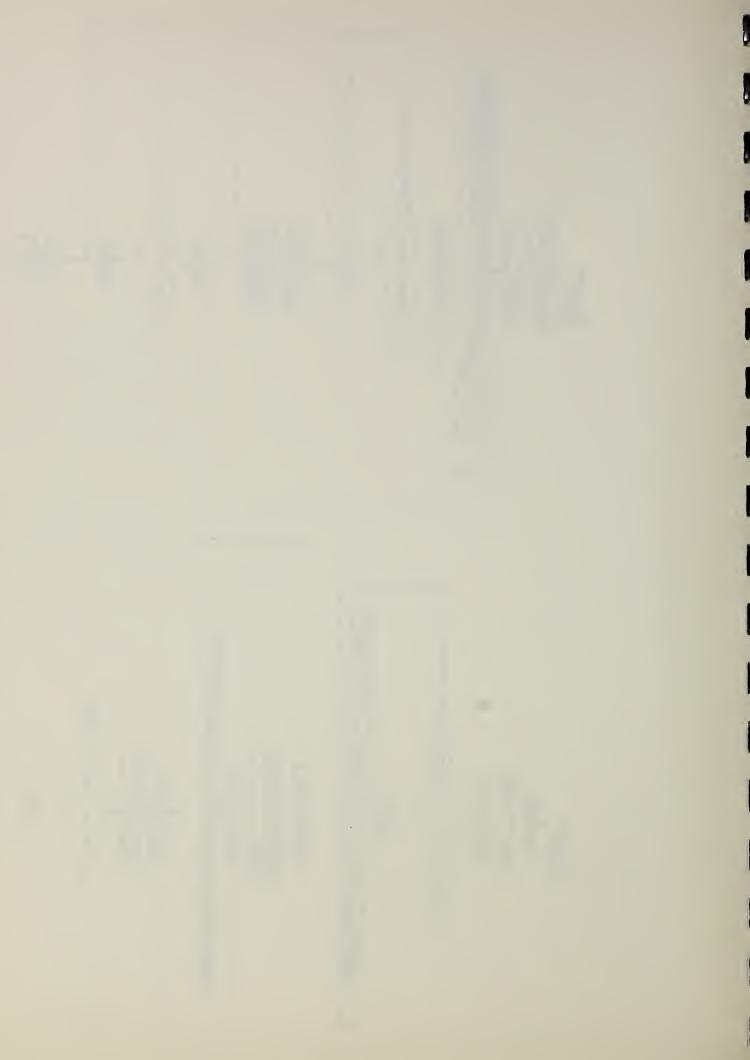


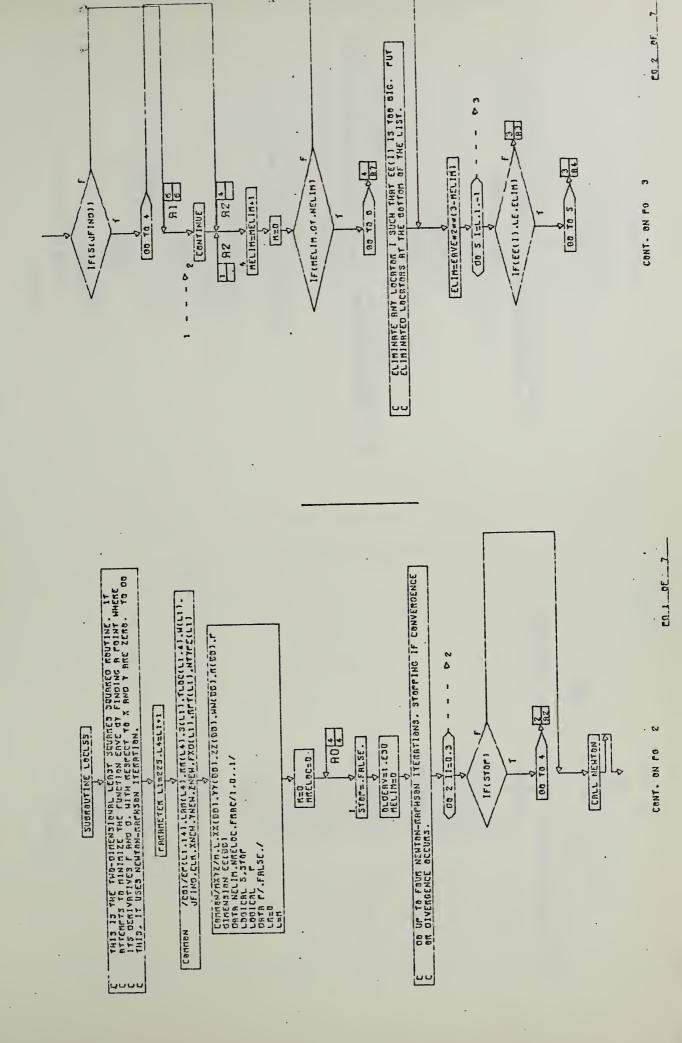


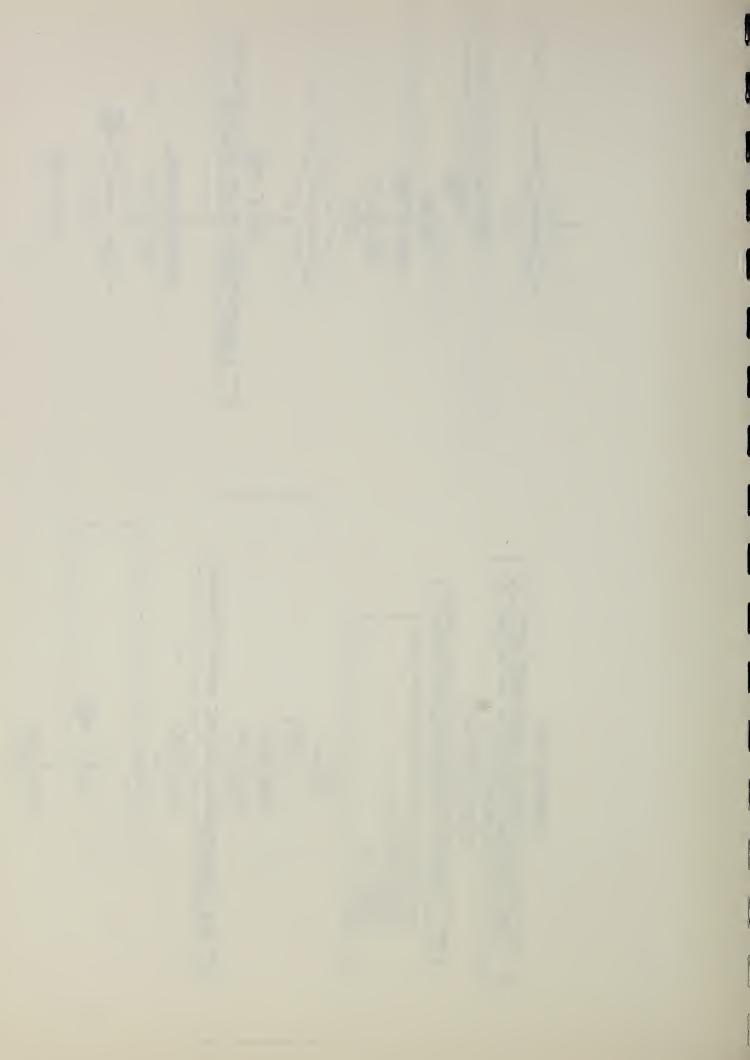


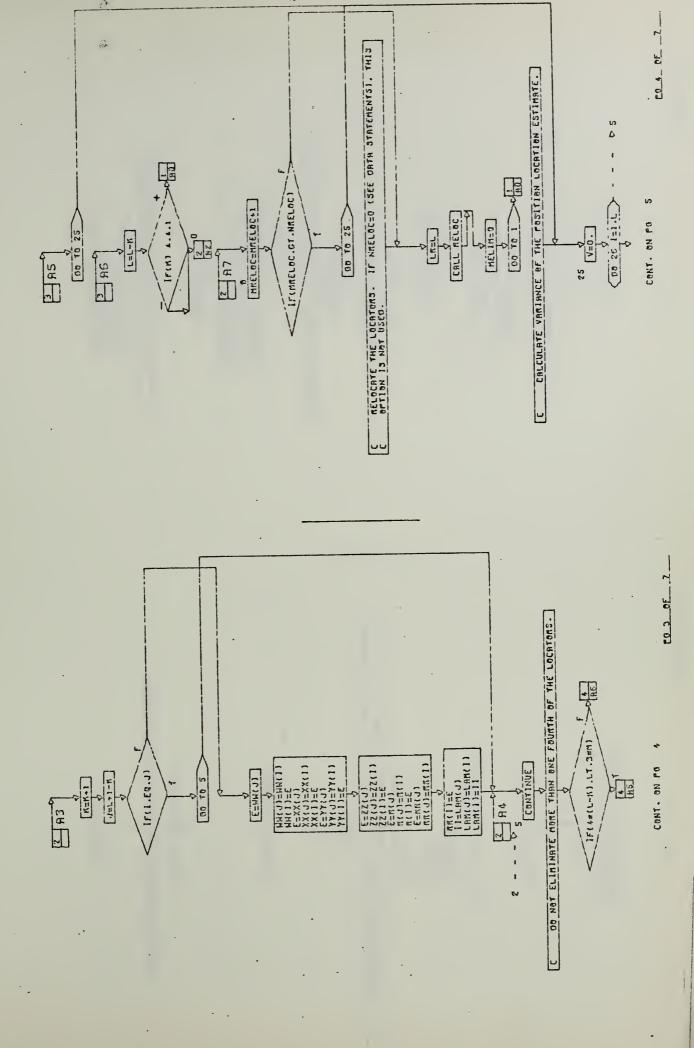
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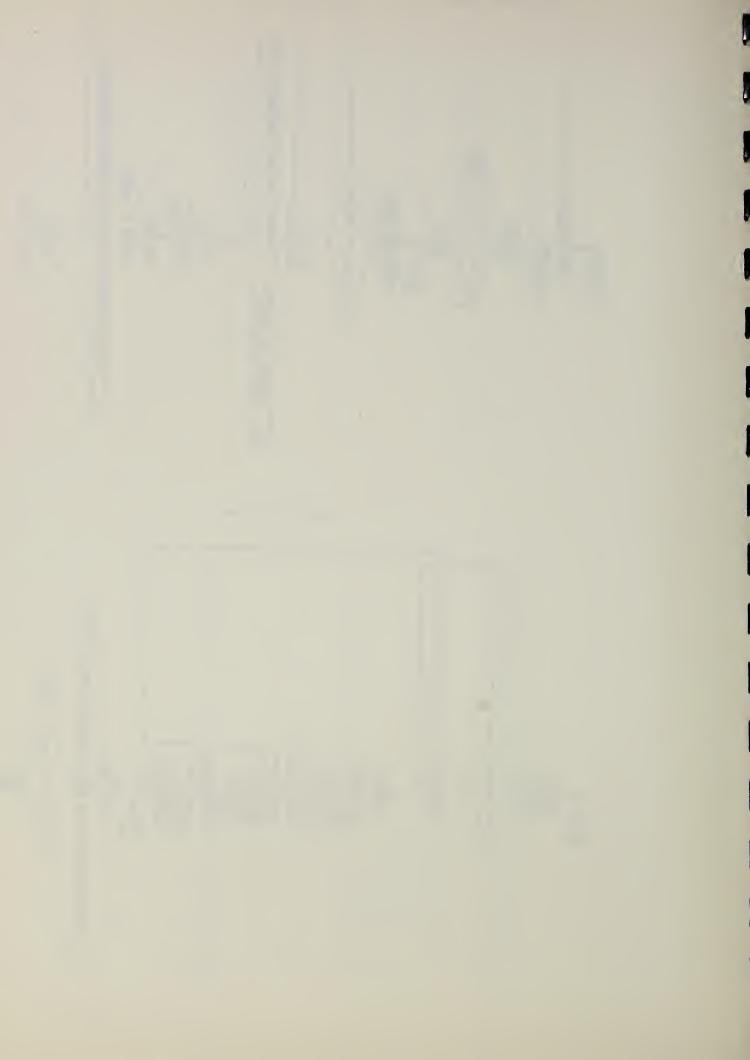
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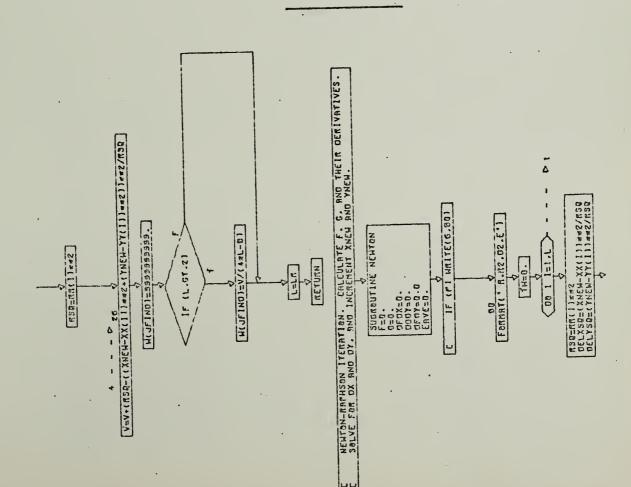






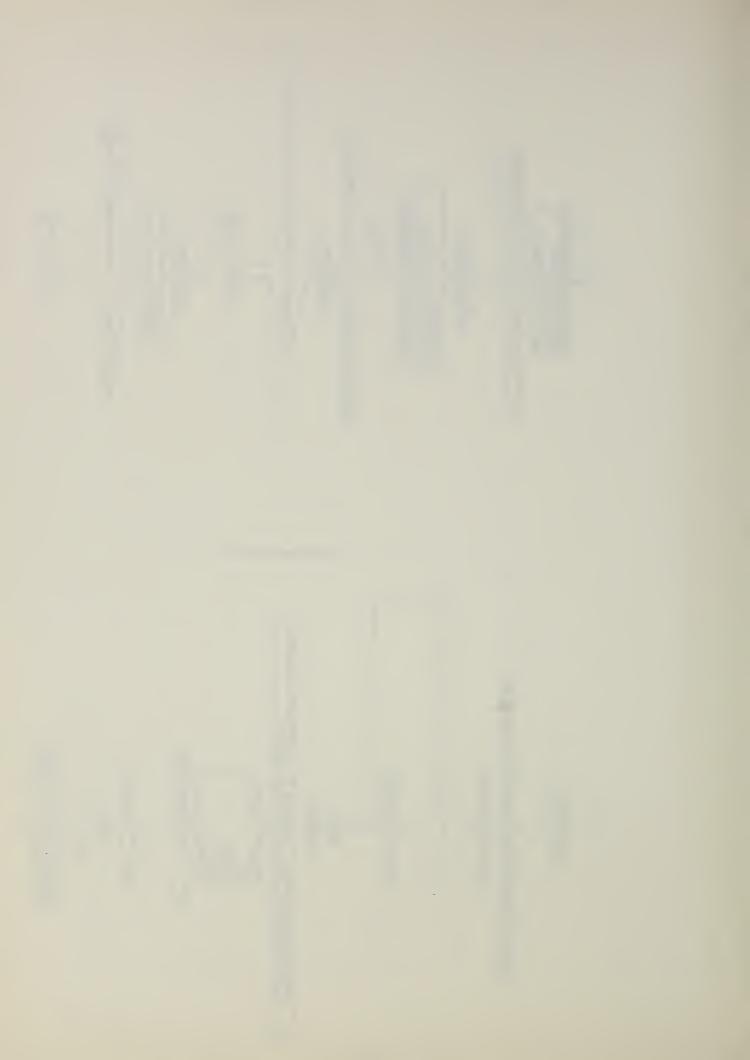


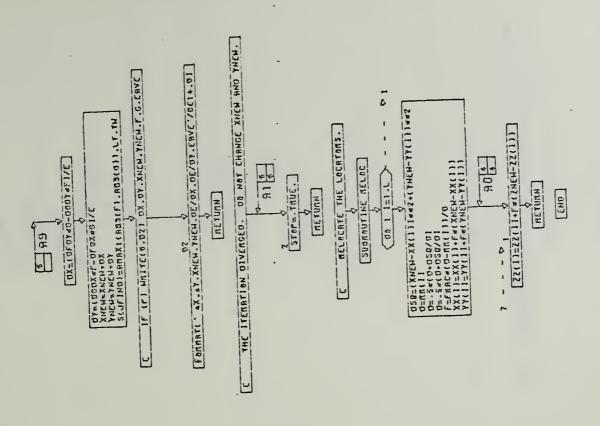




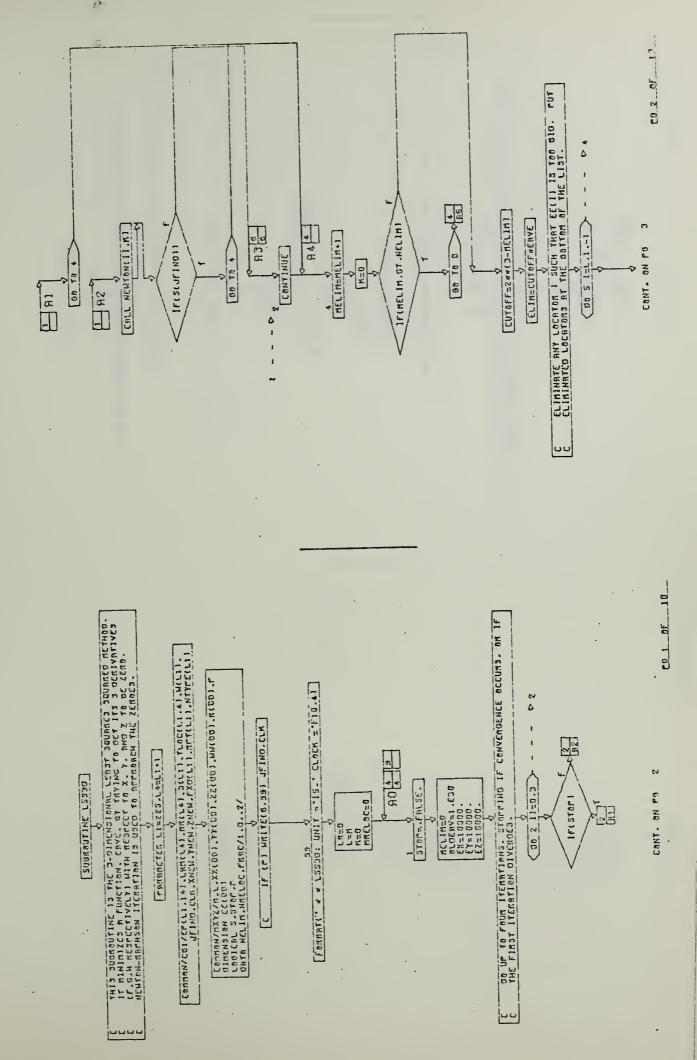
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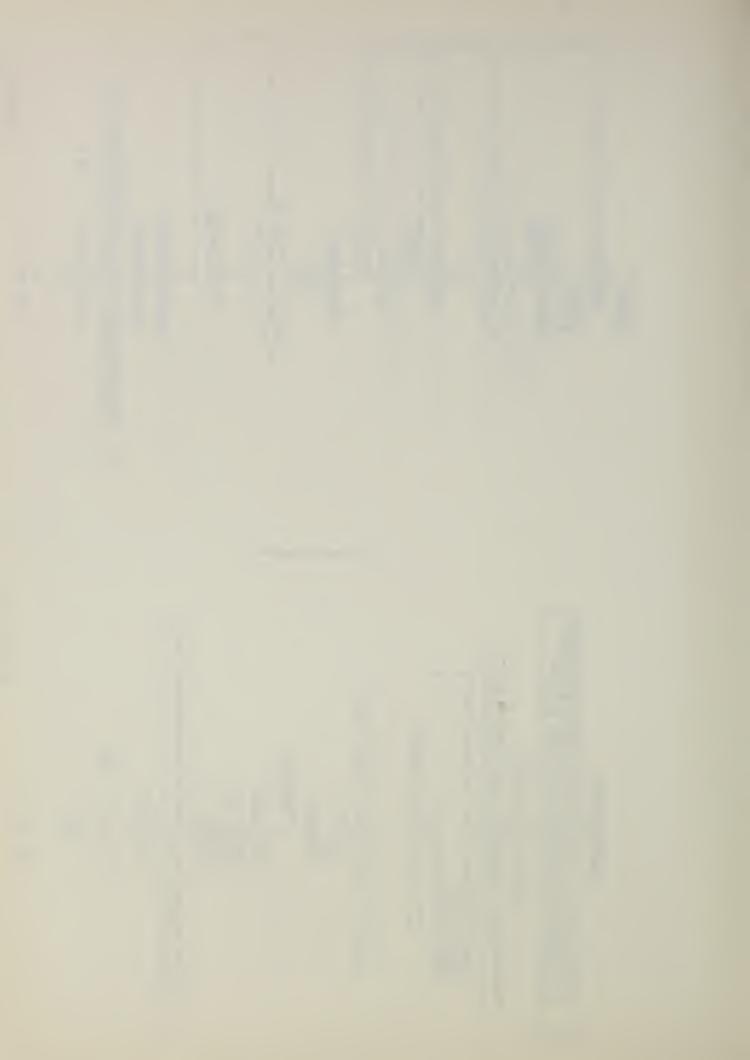
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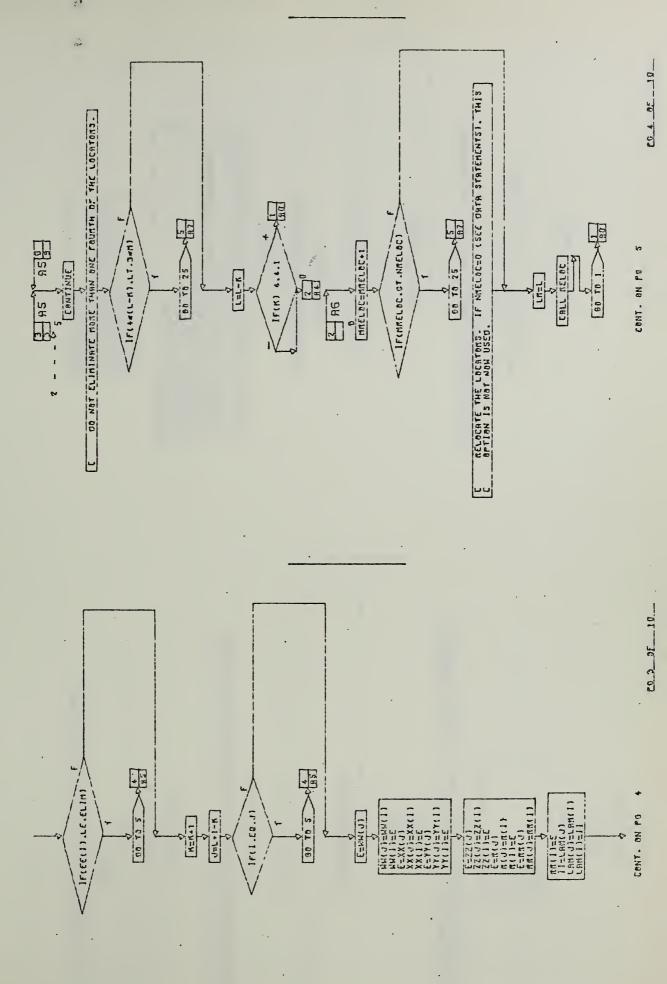




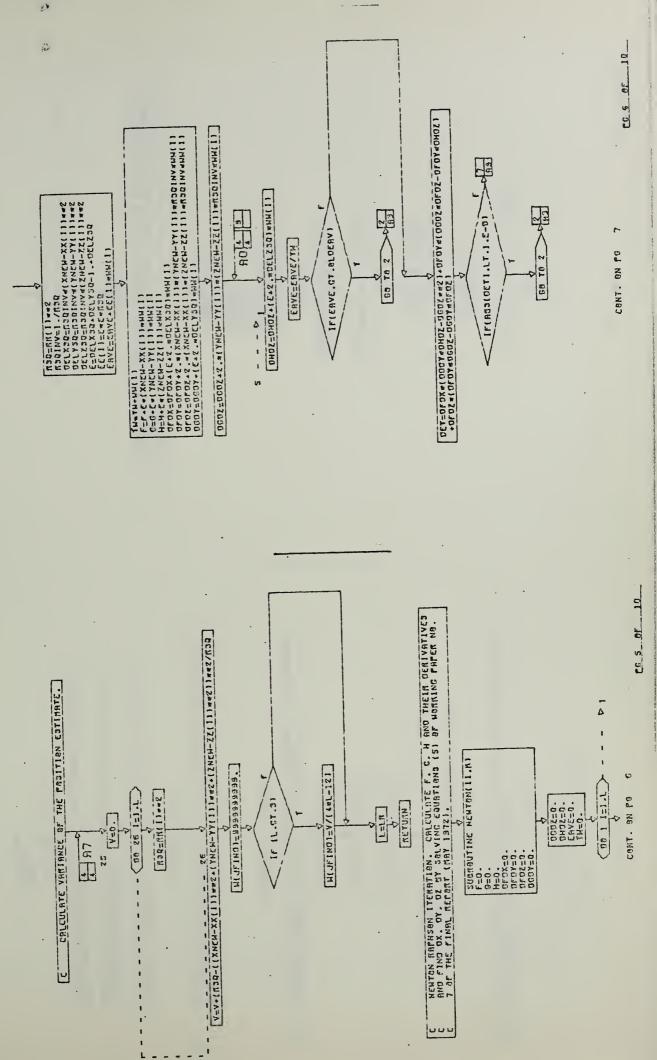














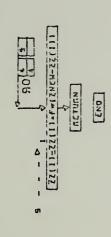
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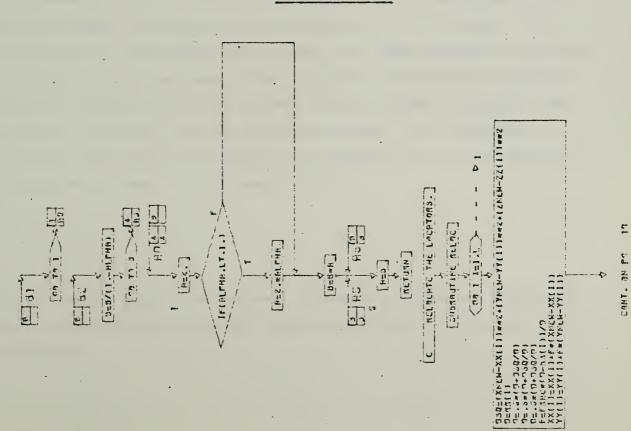
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PROJECT "WHERE" : WORKING PAPER NO. 8

LS, LSS, AND RELOCATION

James A. Lechner

April, 1972

ABSTRACT

In Working Paper No. 2 it was suggested that since the locators' positions are not known exactly, it might prove profitable to re-estimate these positions as an adjunct to estimating the position of the "locatee" unit. This paper presents an iterative method, along the lines proposed in Working Paper No. 2, for handling the computations of such a "relocation" process. The discussion is carried out in the context of the LS(least squares) and LSS(least squares, squared) position-location methods. As background, evidence is given which shows that these two criteria behave very similarly so long as range measurement errors remain small.

<u>Note:</u> Project working papers are informal documents prepared to facilitate discussion and communication; they may contain tentative or relatively unchecked material.



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O. INTRODUCTION

In this paper the term <u>location-operation</u> will be used for a process of attributing a position to one unit (the <u>locatee</u>) on the basis of its recorded distances from n other units (the <u>locators</u>). These recorded distances are of course subject to measurement error.

Roughly speaking, the situation studied in Project "WHERE" is one in which the role of "locatee" varies over some totality of units, with many of these units in motion at any time. From this it is apparent that for any one location-operation, the positions of the locators (which may have been the locatees of previous operations) are not in general known exactly. This point was emphasized in Section 5 of Working Paper No. 2 [" An Iterative Approach to the Location-Operation", A.J. Goldman, 10/71], where it was suggested that the location-operation be expanded to include re-estimation (i.e., relocation) of the locators' positions, based on the latest set of range measurements.

The present paper has as its main purpose the computational specification of such a relocation procedure. This is given in Section 2, which also discusses the respective merits of the LS (least squares) and LSS (least squares, squared) position-location methods in this context. Section 1 presents some relevant background information concerning the relationship between these two algorithms.

We conclude this Introduction by introducing some necessary mathematical notation:

0 = (arbitrary) origin of coordinate system ,

X = position to be atrributed to locatee,

x = vector OX

 A_i = position to be attributed to i-th observer (i = 1, 2,..., n),



 $a_i = vector OA_i$,

 α_{i} = initial estimate of a_{i} ,

 $r_i = ||x - a_i|| =$ estimated distance between locatee and i-th observer,

 ρ_i = measured value of this distance.

If the distinction between a_i and α_i is dropped (i.e., the initial estimates of the locators' position are accepted without revision), then we have the "pure" location-operation, which can be expressed as the problem of making a "good" choice of x, given the ρ_i and a_i . The LS method expresses this problem as that of minimizing the quadratic "penalty function"

$$f(x) = \sum_{i} w'_{i}(r_{i} - \rho_{i})^{2} \qquad (0.1)$$

where the w_i are positive "weights" and x enters \underline{via} the r_i 's ; the LSS approach involves the minimization of

$$g(x) = \sum_{i} w_{i}(r_{i}^{2} - \rho_{i}^{2})^{2},$$
 (0.2)

with "weights" w_{i} . The modification of these formulations, to encompass relocation, will be taken up in Section 2 .



1. RELATION BETWEEN LS AND LSS APPROACHES

In this section, as background for the discussion of relocation in Section 2, we discuss the relation between the LS and LSS approaches to the "pure" location-operation. Three pieces of evidence will be given to show that if the "weights" in these two criteria --- the \mathbf{w}_i of (0.1) and the \mathbf{w}_i of (0.2) --- are properly related, then the two methods will not differ significantly in accuracy so long as the tracking process is under control. (The last phrase means that the units' positions remain well enough known that the discrepancies between measured ranges ρ_i and calculated ranges r_i are small relative to the magnitudes of the ranges themselves.)

The <u>first</u> piece of evidence begins with the observation that the "under control" assumption, $\textbf{r}_i/\rho_i\approx 1$, yields

$$(r_{i}^{2} - \rho_{i}^{2})^{2} = (r_{i} + \rho_{i})^{2} (r_{i} - \rho_{i})^{2}$$

$$= (1 + r_{i}/\rho_{i})^{2} \rho_{i}^{2} (r_{i} - \rho_{i})^{2}$$

$$\approx 4\rho_{i}^{2} (r_{i} - \rho_{i})^{2} ,$$

or equivalently

$$(1/4\rho_{i}^{2})(r_{i}^{2} - \rho_{i}^{2})^{2} \approx (r_{i} - \rho_{i})^{2}$$
.

Thus, if we set $w_i = (1/4\rho_i^2) w_i$, then comparison of (0.1) with (0.2) shows that $g(x) \approx f(x)$; equivalently, if we set

$$w_i = w_i'/\rho_i^2 \tag{1.1}$$



then comparison of (0.1) yields $g(x) \approx 4f(x)$, so that minimization of f(x)--- i.e., the LS approach --- is "approximately equivalent" to the LSS approach (minimization of g(x)).

Equation (1.1) gives the appropriate relation between the two sets of weights. As yet, no rationale has been found for assigning to the w_i any value other than unity. In fact, since the distribution of errors in (unrejected) ranges seems (by best engineering judgement at this time) to be Gaussian, with range-independent variance and zero mean (except for a small percentage of ranges biased by about 8m), maximum likelihood estimation would strongly recommend (1) use of LS with $w_i = 1$ (together with some technique for removing "outliers"), which by the above is approximately equivalent to use of LSS with

$$w_{i} = 1/\rho_{i}^{2} \qquad (1.2)$$

This choice of w_i and w_i will be used throughout the rest of this paper.

The preceding analysis shows that the penalty functions for LS and LSS are approximately equal (when measured and calculated ranges are close together), but one would like some direct assurance that the position-estimates obtained by minimizing these two functions are also nearly equal. This is provided by our second piece of evidence, an analysis for a simple 1-dimensional configuration in which the locators are situated at the points with coordinates R and (-R) with R large, while the locatee is actually situated at the origin. The LS approach calls for the minimization of

$$f(x) = [(R-x) - \rho_1]^2 + [(R+x) - \rho_2]^2$$
$$= 2\{x^2 + (\rho_1 - \rho_2)x\} + const.,$$

⁽¹⁾ See Section 1 of Working Paper No. 2



which is readily found to be given by

$$x = (\rho_2 - \rho_1)/2$$
 . (LS solution) (1.3)

The LSS approach calls for the minimization of

$$g(x) = \rho_1^{-2}[(R-x)^2 - \rho_1^2]^2 + \rho_2^{-2}[(R+x)^2 - \rho_2^2]^2$$
$$= \rho_1^{-2}(R-x)^4 + \rho_2^{-2}(R+x)^4 - 4x^2 + const.;$$

setting dg/dx = 0 leads to the cubic equation

$$(\rho_1^2 + \rho_2^2)x^3 + 3R(\rho_1^2 - \rho_2^2)x^2 + [3R^2(\rho_1^2 + \rho_2^2) - 2\rho_1^2\rho_2^2]x + R^3(\rho_1^2 - \rho_2^2) = 0.$$
 (1.4)

Let E denote a measure of maximum range-error. In the worst-case scenario described by ρ_1 = R-E and ρ_2 = R + E , the LS and LSS approaches yield exactly the same answer, both (1.3) and (1.4) giving x = E . In the alternative scenario described by ρ_1 = R and ρ_2 = R + E , the respective solutions are

$$x_{LS} = \frac{1}{2}E$$
, $x_{LSS} = \frac{1}{2}E[1 - \frac{3}{8}(E/R)^2]$ (1.5)

where the expression for x_{LSS} omits higher-order terms in the small quantity E/R; if for example R is at least 1 km and E is at most 20m, then the two position-estimates differ by at most 0.0015 m.



Our third piece of evidence is empirical in nature. For each of two distributions of range-measurement errors ("small" and "large", respectively), 72 trial 2-dimensional location-operations were carried out using both LS and LSS. Each of 18 units served as locatee 4 times (for each error distribution and each method), with the other 17 units serving as locators. For the "small" case, the locations were as much as 3.32m in error, but the LS and LSS results differed from each other by no more than 0.0004m; for the "large" case, despite location errors up to 31.9m, the two methods yielded locations no more than 0.045m apart.



THE RELOCATION PROCESS

When the location-operation is enlarged to include relocation (of the locators), it can be formulated as making a "good" choice of x and the a_i , given the ρ_i and α_i . The approach given in Section 4 of Working Paper No. 2 is based on two notions, one of which we have found it is useful to modify in a manner described below.

The <u>first</u> notion is that the choices of x and a's should be made so as to minimize a penalty function which generalizes those given earlier [see (0.1) and (0.2)] for "pure" location. Specifically, this function is

$$f(x; a_1,..., a_n) = \sum_i w_i (r_i - \rho_i)^2 + \sum_i w_i ||a_i - \alpha_i||^2$$
 (4.1a)

for the LS approach, and

$$g(x; a_1,..., a_n) = \sum_i w_i (r_i^2 - \rho_i^2)^2 + \sum_i w_i \|a_i - \alpha_i\|^2$$
 (4.1b)

for the LSS approach; the W_i are positive numerical weights.

The <u>second</u> notion is to accomplish this minimization by a process which <u>alternates</u> between <u>location steps</u> (in which the a are held fixed and an appropriate x is chosen) and <u>relocation steps</u> (in which x is held fixed and appropriate a 's are chosen. This process can be formalized as follows:

INITIALIZATION: Set
$$k = 1$$
, and $a_i^{(1)} = \alpha_i$ (all i).

STEP 1 (location, k-th pass): Given the current estimates $a_i^{(k)}$ of the locator positions, choose $x = x^{(k)}$ to minimize the first sum in (4.1), i.e. the part of (4.1) which depends on x.



STEP 2 (relocation, k-th pass): For each i, keep x fixed at $x^{(k)}$ and choose a to minimize the sum of those terms in (4.1) which depend on a . Increase k by 1, and set each $a_i^{(k)}$ equal to the a just found. Return to Step 1.

For Step 1, the material in Section 1 shows that there is little reason to prefer one of LS or LSS over the other so far as location-errors are concerned. We therefore select LSS, since it seems likely to converge more quickly and requires fewer time-consuming calculations per iteration. Thus Step 1 employs (4.1b) rather than (4.1a), and so according to the description above, the treatment of the i-th locator in the k-th relocation step would require choosing a, to minimize

$$w_{i}\{\|x^{(k)} - a_{i}\|^{2} - \rho_{i}^{2}\}^{2} + W_{i}\|a_{i} - \alpha_{i}\|^{2}.$$
 (4.2)

For Step 2, however, it is more convenient to minimize instead the sum of corresponding summands from (4.1a), namely

$$h(a_i) = w_i' \{ || x^{(k)} - a_i || - \rho_i \}^2 + W_i || a_i - \alpha_i ||^2.$$
 (4.3)

The over-all method becomes a kind of LS-LSS hybrid; Steps 1 and 2 in effect involve different penalty functions, so that the "first notion" described above has indeed been modified.

In Working Paper No. 2 it was envisiged that the alternating process would be iterated until it had "settled down" satisfactorily. This idea, too, has been modified after further reflection. The relocation of the i-th locator is based mainly upon a single new datum, namely ρ_i ; it seems



unwise to put too much reliance or to base too much calculation on this one datum (which is subject to measurement-error). Besides, from the viewpoint of reducing total computation time it is desirable to limit the number of iterations. Thus a sensible compromise seems to be: locate the locatee (Step 1); relocate the locators (Step 2); then locate the locatee again (second pass through Step 1), and stop. This truncated version of the full process is assumed below.

We turn now to the execution of Step 2. With superscripts (k) and subscripts (i) dropped for simplicity, the function (4.3) to be minimized can be written

$$h(a) = w'\{||x-a|| - \rho\}^2 + w||a-\alpha||^2.$$
 (4.4)

Consider any trial position a' of a . It lies on a sphere of radius $\parallel x-a' \parallel$ centered at x . Suppose a' is replaced by the point of that same sphere which is closest to α ; then the first summand in (4.4) is unchanged, while the second summand is reduced. Hence the minimum can only occur for such a "closest point". Simple geometric considerations show that such a point lies either on the line segment $[x,\alpha]$ or on its extension through α . Thus, for some scalar $s \geq 0$, we have

$$a = x + s(\alpha - x) ,$$

leading to

$$x - a = s(x-\alpha)$$
, $a - \alpha = (1-s)(x-\alpha)$.

Substitution of these results into (4.4) converts h(a) into a function of s; with the abbreviation

$$r = \| x - \alpha \|, \qquad (4.5)$$



this function reads

$$H(s) = w'\{sr-\rho\}^2 + Wr^2(1-s)^2$$

$$= (w'+W)r^2s^2 - 2r(w'\rho + Wr)s + (w'\rho^2 + Wr^2),$$
(4.6)

and is minimized by setting

$$s = (w'\rho + Wr)/(w' + W)r$$
 (4.7)

(The availability of such a simple explicit solution to the minimization problem justifies our earlier assertion that use of (4.4) rather than (4.2) is more convenient.) If $\rho > r$ then s > 1, signifying that a lies on the extension of segment $[x,\alpha]$ through α (i.e., relocation has moved the locator farther from the locatee); if $\rho < r$, then s < 1 and a lies on the segment (so that the locator has been moved closer to the locatee). These results, which do not depend on w and W, seem quite consistent with what one would expect intuitively.

The only remaining question is the selection of numerical values for the weights $W_{\bf i}$. We have at present no definitive answer to this problem. There are two distinct considerations to be taken into account:

(a) If we consider the current location (and relocation) operation in isolation, then the weight W_i should depend primarily on our confidence in the accuracy of the initial estimate α_i of the i-th locator's position (relative to the accuracies of the other α_j 's , and also of the range measurements). In an idealized Gaussian-error case, for example, maximum-likelihood estimation would dictate weights inversely proportional to the respective variances of the associated random errors. For our practical situation, how can we quantify the degree of confidence merited by the initial estimate α_i ?



It may well prove possible to concoct an appropriate measure based on the sizes of the discrepancies $|r_j - \rho_j|$ obtained during the last previous location-operation in which the i-th of the current locators figured as locatee---probably modified by some "decay factor" to take account of how much time has elapsed since this earlier operation.

(b) However, one needs to consider the "current" operation in the light of the need to maintain stability of the entire location process; the selection (or least the effect) of the $W_{\bf i}$ must reflect not only the one-shot independent-measurement case as in (a), but also the sequential correlated-error many-locator nature of the real problem. If a relocation(based mainly on a single and possible "bad" range measurement $\rho_{\bf i}$) is allowed to be too large, its influence would persist through a number of operations until the unit in question again took its turn as locatee, and so such instabilities in estimation of positions could result in large errors.

The following tactic may prove an acceptable compromise. Weights W_i will be selected according to the considerations in (a) above. The resultant solutions (4.7) of the n minimization problems for relocation (1 problem for each of the n locators) will dictate moving the estimated position of the i-th locator a certain distance (from α_i) in a certain direction along the line through $\mathbf{x}^{(k)}$ and α_i . To "temper" this solution in accordance with the considerations in (b), we will "damp" that distance by a multiplicative factor (say, between 0.1 and 0.6) before actually revising the estimate of the locator's position. Numerical experimentation will be required to test the performance of this approach and to determine what values of the adjustment factor are preferable.



PROJECT "WHERE": WORKING PAPER NO. 9 THE MNPLS SIMULATION ("WHERESIM")

R.H.F. Jackson

May, 1972

Abstract: This paper documents the present version of the MNPLS simulation. The documentation is presented at three levels: the "executive" level (an overview), the "user" level (description of input and output), and the "analyst" level (detailed discussion of the logic flow). It focuses on the concepts indigenous to such a simulation study, namely: movement of units, range computation (including the occurrence of measurement error), and position estimation. A dictionary of variables used in the program, as well as a listing and a detailed flowchart of the program, are also included.

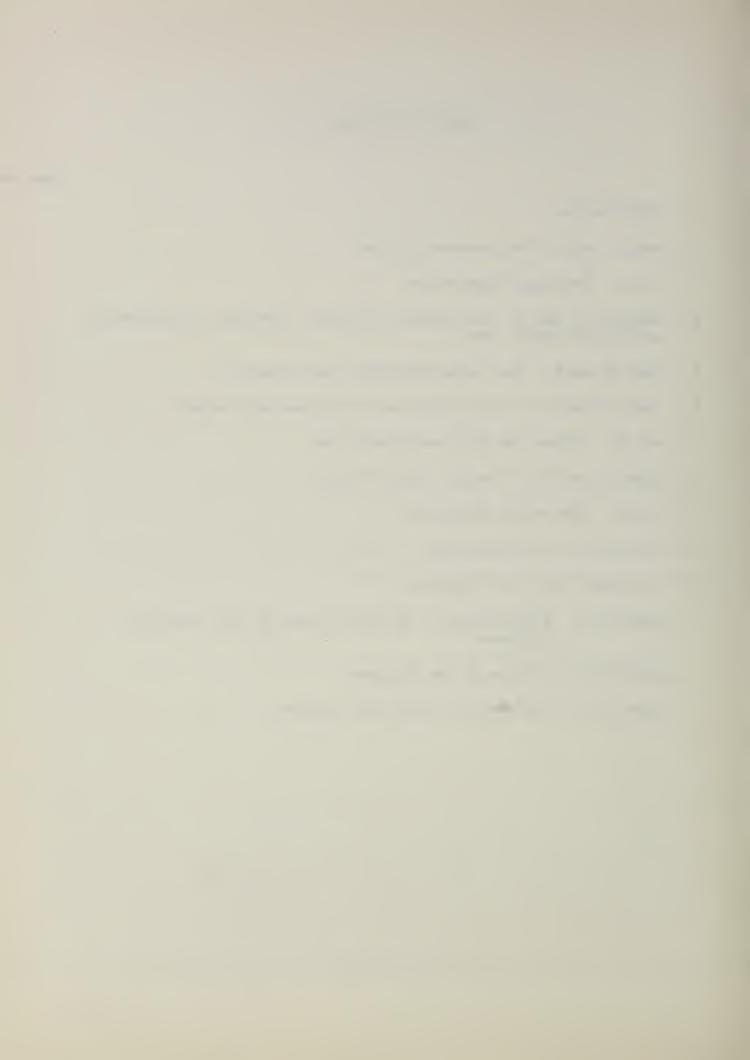
<u>Note</u>: Project working papers are informal documents prepared to facilitate discussion and communication; they may contain tentative or relatively unchecked material.



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1. INTRODUCTION

WHERSM^(*) is a computer code that simulates the operation of a Micro-Navigation Position Location System (MNPLS). It provides a "real life" framework within which the propagation over time of position location errors, resulting from the operation of such a system, can be determined. It further provides a facility for monitoring the operation of such a system under a variety of movement scenarios, and using a variety of algorithms for accomplishing the location operation.

This paper documents the present version of the WHERSM code at three levels: the "executive" level, the "user's" level, and the "analyst's" level. This introductory section, which serves as the executive level of documentation, is aimed at the person who is interested only in an overview of what WHERSM is and what it does. The user's level of documentation is meant for one who is concerned with making a computer run with the code as it now stands; i.e., with no major program modifications. Sections 10 and 11 provide documentation of all the inputs and outputs — the information needed to make a run. The remainder of the paper, Sections 2 through 9 and appendices A, B, and C, is designed with the analyst in mind. By an "analyst" is meant one who needs not only to run the program, but also perhaps to modify it to handle somewhat different situations. This paper should include enough information to start him on his way.

Due to the nature of the MNPLS under study, WHERSM is a "fixed time increment" simulation; i.e., simulated time is advanced by a constant increment, Δt , rather than by variable increments dictated by the occurrence of events, as would be the case in the type of simulation classified as "next event".

^(*) Full name: WHERESIM. Compressed because of computer restrictions to 6 characters per name.

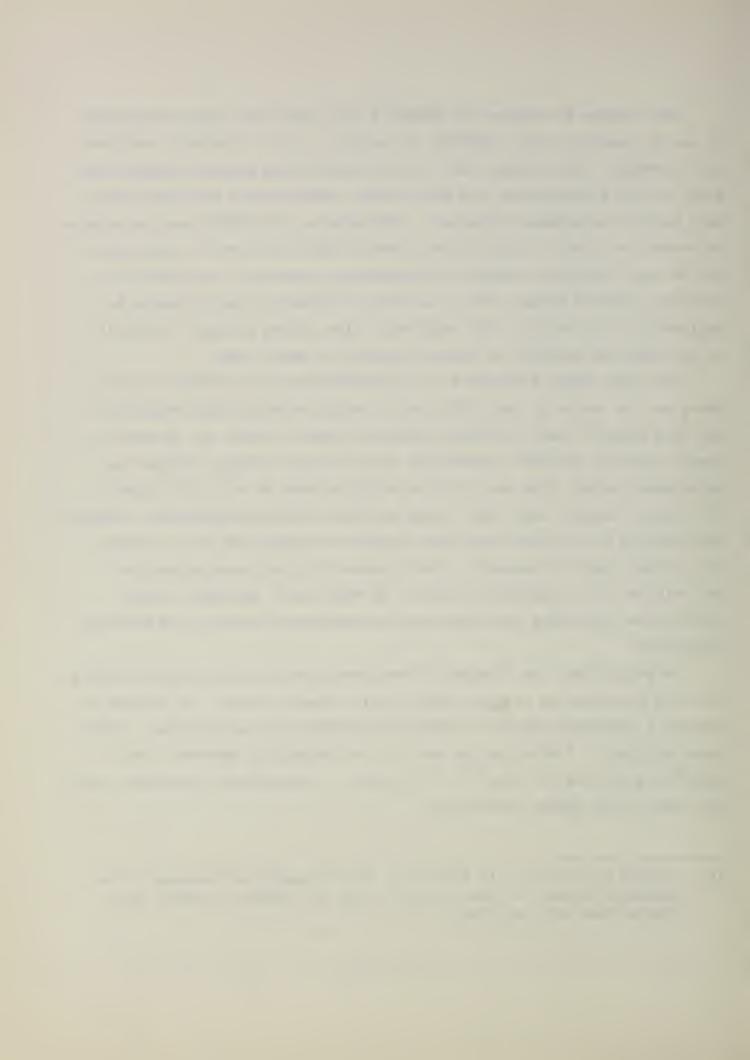


The program is written in FORTRAN V, but with very little conversion it can be compiled with a FORTRAN IV compiler. It is liberally annotated with comments, and although the code documented here employs program overlays, parallel processing, and drum usage, every attempt has been made to keep machine dependence minimized. Furthermore, the WHERSM code is modular in nature, so that the logic flow is kept simple and easy to understand, and so that different concepts in deployment, movement, intervisibility, position location method, etc., can with a minimum of reprogramming be implemented and tested. This modularity also allows extreme flexibility in the type and quantity of inputs required to make a run.

The basic ideas involved in an implementation of the MNPLS are that there are n units in the field, any of which at each moment might (in the most general case) be either moving or fixed. Every Δt seconds, a master computer receives information in the form of ranges, subject to measurement error, from one of these units to some or all of the others. The master computer must then, using position location algorithms, estimate the position of that unit and also prepare to receive the set of ranges for the next unit in sequence. The elements of this description that are relevant to a simulation study of an MNPLS are: movement, range computation (including the occurrence of measurement error), and position estimation.

In particular, the simulation must have some facility for determining the true positions of all the units at all relevant times. It is easy to provide a movement scenario in terms of movements in the xy-plane (longi-tude-latitude). A starting x and y, an azimuth of movement, and a speed will suffice for this (*). It is the z coordinate, the height above sea level, that causes difficulty.

^(*) As will be explained in Section 2, the movements are assumed to be piecewise linear, so that in fact a <u>set</u> of azimuths, speeds, <u>and</u> change times are required.



There are at least two methods of providing the z coordinate in a simulation. One involves a continuous function which yields a value of z for any values of x and y; the other is by means of a discrete function which specifies values of z for particular values of x and y. In the discrete case, values of x and y other than the prescribed ones are assumed to coincide with the nearest available grid point, whose specified height is then used (*). Both of these techniques are explained in detail in section 2.

The next item with which the simulation of the MNPLS must be concerned is the computation of ranges. Of course, given the ability to compute the true positions of all units at any instant of time, the true ranges can easily be calculated, since they are simply Euclidean distances. But, in the "real life" situation, true ranges are never reported to the master computer due to measurement errors intrinsic to the particular method of measuring those ranges. This phenomenon is easily simulated once a probability distribution of measurement errors is specified, since the simulation program can simply compute pseudo-random numbers which satisfy such a distribution law.

Another point relevant to range computation is that a simulation must be capable of determining whether a range should be computed; i.e., whether, for a specified pair of units at a specific moment, a radio line of sight (LOS) exists. There are many ways (**) of providing a simulation program with the ability to determine the existence or non-existence of these intervisibilities. The method used in WHERSM is to maintain a set (***) of "intervisibility snapshot matrices", I_{ijt} (i = 1, 2, ..., n; j = 1, 2, ..., n;

^(*) Four-point interpolation could have been used here, but is very time consuming. And since it was determined that no significant further loss of accuracy occurs with the "nearest point" method, that one was implemented.

^(**) See p.28 of "First Interim Progress Report on NBS Project WHERE in Support of USAAMCA Project MNPLS", NBS Report 10663, December 1971.

^(***) Obtained from the Electromagnetic Compatibility Analysis Center, Annapolis, Md.



t = 0, 20, 40, ..., 120) where I_{ijt} = 1 if unit j can receive <u>and report</u> a ranging signal from unit i at time t minutes into the simulation, and I_{ijt} = 0 if it cannot. Furthermore, in order to avoid drastic changes in the intervisibility pattern at the discrete times indicated by values of the subscript t, each row of a particular intervisibility matrix defined by a specific value of t, say t, is overlaid with the corresponding row of the next-in-sequence matrix (defined by t' + 20) at some randomly chosen time between t' and t' + 20. (These times are chosen independently for each row and for each value of t.) More detail regarding each aspect of range computation will be found in sections 3 and 5.

The last item of concern for the MNPLS simulation is that of position estimation. Although that item is an integral part of any simulation study of this nature (indeed, the most important part), no discussion of the various algorithms used in WHERSM is provided here, since the project staff members responsible for the development and implementation of position location algorithms have presented such a discussion in Working Paper Number 7.

In order to provide the reader with a better understanding of the flow of events within WHERSM, and to facilitate further discussion of the WHERSM program, a flowchart is given in figure 1 which indicates the basic logic of the simulation. With one exception (see section 9), each box in the flowchart corresponds to an easily recognizable module within the WHERSM code listed in appendix B. In every case, entry to box 2 is made just after the simulation's current time is incremented by a constant value. That constant, Δt , is referred to as the <u>subcycle</u> time and is the time during which all the operations required to locate a given unit (one completion of the loop formed by boxes 2 through 7 of the flowchart) must be performed. Cycle time is the time required to locate each unit at least once. This may be larger than $n \cdot \Delta t$, where n is the total number of units, since certain faster moving units may need to be located more often

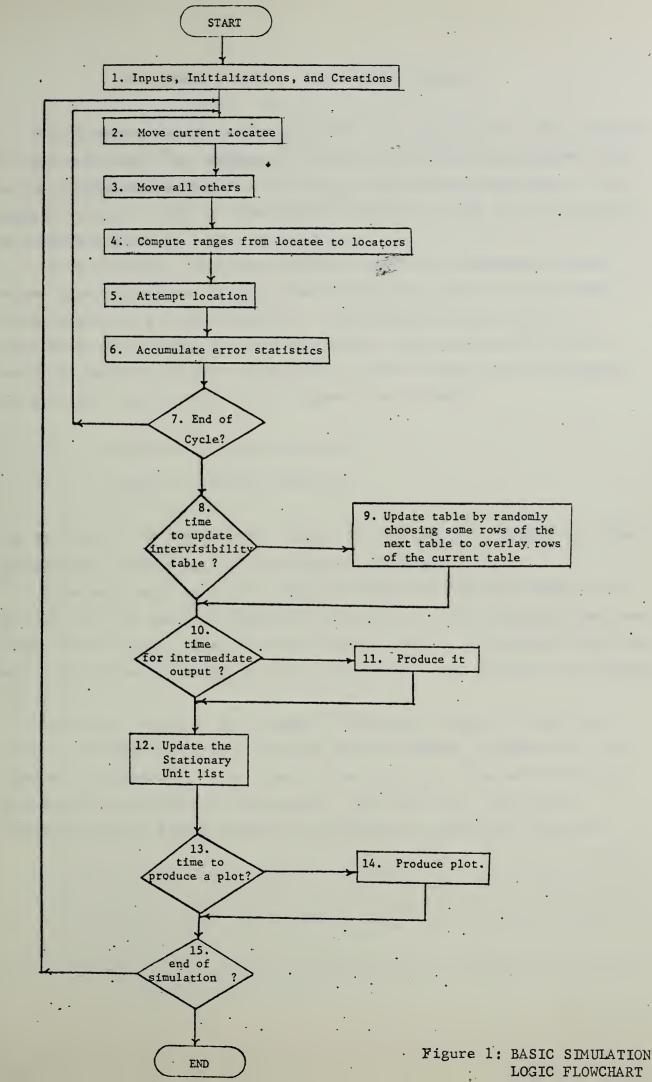


than do slow moving units. Locatee refers to that unit which, at any instant of simulated time, is in the process of being located, and locator refers to a unit whose range to the locatee is used to estimate the position of the locatee.

The remainder of this report discusses the workingsof WHERSM at a more detailed level. Section 2 explains Boxes 2 and 3 of the flowchart in figure 1, while Section 3 discusses Box 4. Section 4 explains Boxes 5, 6, and 7; Section 5, Boxes 8 and 9; Section 6, Boxes 10 and 11; Section 7, Box 12, Section 8, Boxes 13 and 14; and Section 9, Box 15. Section 10 contains a discussion of the input needed to make a run with the present version of the code; and Section 11 contains a discussion, with examples, of the outputs that will result from such a run. Appendix A is a dictionary of variables used in the program; Appendix B, a listing of the program; and Appendix C, a very detailed flowchart of the program.

Although the remaining section headings refer directly to the flow-chart in figure 1, the content of those sections can be better understood by referring to Appendices B and C.







2. BOXES 2 and 3: THE MOVEMENT MODULES

The movement modules are responsible for computing the true positions of each unit every Δt seconds. In the current version of WHERSM, this is a two-stage process; i.e., x and y are computed, and then z is computed using x and y. The method by which x and y are computed is explained first.

In the xy-plane, units are assumed to move in a piecewise linear manner (the projections of the three-dimensional curves of motion onto the xy-plane are piecewise linear). The piecewise linear motion is effected by maintaining a matrix of current true positions (TP) and a matrix of current velocity vectors (VV), both of which are initialized by card input, and by updating TP linearly as follows:

$$TP(I,1) = TP(I,1) + VV(I,2)$$

$$TP(I,2) = TP(I,2) + VV(I,2)$$

for each unit I = 1, 2, ..., NU, where NU is the total number of units. See Appendix A for a detailed explanation of TP and VV.

After each unit is moved, a check is made to determine whether it is time for that unit to change its direction of motion (change times are stored in VV(I,3)). If so, the new velocity vector is retrieved from the matrix VVI where <u>all</u> velocity vectors are stored, and replaces the existing one in VV.

The second stage of the movement computation, that of computing z, has been implemented in two different ways in WHERSM, although only one appears in appendix B. (The other is too specific to include here and, furthermore, is trivial to implement.) The first one, the one not included here, is simply a matter of coding up a continuous function



representation (*) for the z coordinate and computing a value of z once x and y have been determined.

The method of determining z that <u>is</u> included in Appendix B is somewhat complicated, in that it involves a preprocessor, overlays, a mass storage retrieval routine, and parallel processing. The preprocessor is a routine called BUILD, whose function is to read a tape containing topographical data in the format designed by the Electromagnetic Compatibility Analysis Center (**), decode and unpack the individual altitudes above sea level that are given on that tape, write the individual elevations out on the drum, create an index (NDX) to the information on the drum, and initiate the overlaying of itself by the rest of the WHERSM code.

The subroutine that actually provides the z coordinate, HEIGHT, is mainly a drum retrieval routine. HEIGHT takes the x and y that are input to it, computes the nearest available grid point to that x and y, determines the position on the drum of the altitude associated with that grid point, and initiates the retrieval of that altitude. This last point is important -- HEIGHT only initiates the read. It does not wait for the completion of that operation, but instead immediately returns control to the calling routine, which has the option of waiting for the completion of the retrieval or of performing other tasks that are not dependent on knowledge of the new z coordinate. In view of the fact that the time required to retrieve one elevation from the drum is approximately 4.254 milliseconds, the above parallel processing capability provided by the HEIGHT routine allows considerable time savings to be

^(*) Note that obtaining such a function for "fictitious" terrains is rather easy, but that surface fitting for "real" terrains may not be trivial. See, e.g., Pavilidis, T., "Piecewise Approximations of Functions of Two Variables and its Application in Topographic Data Reduction", Princeton University, Tech. Report No. 86, Sept. 1970, and "A Program Implementing Piecewise Linear Approximations of Functions of Two Variables", Princeton University Tech. Memo. No. 3, March 1971.

^(**) Encoded altitudes above sea level at points that are three seconds of latitude and longitude apart.

achieved through the thoughtful organization of the main routine relative to height retrieval.

The previous comment regarding organization serves to introduce the last point to be discussed in this section — the reason for including two movement modules — one (Box 2) for the current locatee, and one (Box 3) for all other units in the field. Although all units move every subcycle, a new height is determined only when a unit serves as locatee. (In between, heights are treated as remaining constant.) Hence, while the height for the locatee is being retrieved from the drum, the program can continue on with the moving of all other units, thus taking advantage of the parallel processing provided by HEIGHT. There is very little loss of "realism" with this approach, since due to the design criteria no unit moves farther than 44 meters between times when it is a locatee, and further, since the topographical grid points define a rectangle with dimensions approximately 68m x 92m. Hence, only a small distortion of an already grossly simplified terrain structure occurs.

There is yet another reason for separating movement into two modules. Namely, it reduces the effort involved in implementing a very specific type of movement scenario. For example, the code in Appendix B includes a technique for keeping units from spreading out too much, by disallowing movement past a boundary that moves at a speed determined by input. (This is convenient when a randomly generated scenario that includes foot soldiers and ground vehicles is used. By letting the boundary move at foot soldier speed, the ground vehicles can be kept "close by".) In this case, it is wasteful to monitor a unit's movements <u>all</u> the time. To check only when a unit serves as locatee is sufficient. And this of course is easier and faster when there is a separate movement module for the locatee.



3. BOX 4: THE RANGE COMPUTATION

The range computation module is responsible for computing reported ranges by computing true ranges and perturbing them, and for determining whether each range should be reported. The computation of true ranges involves only Euclidean distance calculations, and the perturbation values are obtained by a call to subroutine RG. Subroutine RG generates pseudorandom numbers having a Gaussian distribution with mean zero and variance 36m², and then randomly chooses 1% of them to which it imputes a positive bias by adding 7 meters to each. Except for the biasing procedure, the method used to generate these numbers is the same as the one proposed by A. Rotenburg (*). RG calls RGU which provides uniformly distributed pseudorandom numbers, generated by the multiplicative congruential method. Other distributions, or other parameter values in these, could easily be substituted in these routines. In order to save time, since RGU is called so frequently during the simulation, Rit is written in SLEUTH, the machine language for the UNIVAC 1108. However, it is very short and can easily be rewritten in FORTRAN.

There are two items that determine whether a particular range should be reported. The first of these is the logical matrix RPT, which is initialized at input time, and which, for each unit, has the logical value "TRUE" if that unit is one that reports received ranges, and "FALSE" if it is not. Note that the maintenance of such a matrix allows the testing of scenarios in which the set of reporting units changes during a run, and where such changes are either exogenous or endogenous events.

The second item that determines whether a particular range should be reported is the matrix of intervisibilities (IT), which records whether or not a radio line of sight (LOS) exists between each pair of units

^(*) Rotenburg, A., "A New Pseudo-Random Number Generator", J. ACM 7. (1960), pp. 75-77.



identified by the subscripts for IT. Also, each row of IT is condensed so that 36 row entries fit into one computer word, thereby greatly reducing storage use. Therefore, the only concern of the range computation module regarding intervisibilities is that of locating and retrieving a particular entry in IT from a block of 36 entries, which informs it whether the range between the defining units should be calculated.

In summary, then, for each subcycle the range computation module steps through a list of the units (excluding, of course, the one currently being located) and checks RPT to see first if a particular unit is a reporter. If so, IT is checked to determine whether that unit can "see" the locatee. If that also is true, then the true distance is calculated, RG is called to obtain a perturbation value, and that value is added to the true distance yielding a reported range. Reported ranges are stored in the matrix RANGE, with the unit numbers of the units that reported each range in matrix LOCATR.



4. BOXES 5, 6, and 7: THE LOCATION ATTEMPT, STATISTICS ACCUMULATION, AND "END OF CYCLE" TEST

The discussions of Boxes 5, 6, and 7 have been combined into this one section simply because there is very little to say about any of them.

The location attempt consists of a call to subroutine FINDIT, which is a preprocessor for the actual location algorithms. As was mentioned in Section 1, no discussion of the algorithms is provided here; nevertheless, some discussion of the input to the algorithms from WHERSM should be given. All input to the position location algorithms is achieved via the labeled common block CB1, which consists of the following variables: EP, LOCATR, RANGE, S, TLOC, W, IU, CLK, XNEW, YNEW, ZNEW, FXD, RPT, and NTYPE. For a description of each of these variables, see Appendix A.

The error statistics that are accumulated are: the current coordinate errors (coordinate-wise subtraction of true from estimated positions), the locatee's position location error (Euclidean distance between true and estimated positions in xy-plane), the error in the z coordinate, the max error in the xy-plane over all cycles and over the current block of KIC cycles (KIC is an input parameter), the maximum error in z over all cycles and over the current KIC cycles, and the time to perform the location operation (obtained by interrogating the computer's internal clock). The statistics accumulated here are used to produce the intermediate output explained in Section 11.

The "end of cycle" test (Box 7 of the flowchart in figure 1) is nothing more than the end of a DO loop which steps the simulation program through each one of the subcycles in a cycle.



5. BOXES 8 and 9: THE"INTERVISIBILITY TABLE UPDATE"

The "intervisibility update" module is concerned with maintaining an LOS pattern that is checked by the WHERSM program during range computation (see Section 3). The "current" intervisibility pattern is kept in the matrix IT, which is automatically updated in a manner determined by parameters that are input to the simulation program. This section explains the manner in which IT is updated.

The intervisibility snapshot matrices that have been discussed in Sections 1 and 3 are read in from tape at input time and stored in the matrix ITB. (The format of the tape is explained in Section 10.) At the start of a simulation run, IT is initialized to the first of the snapshot matrices—the matrix that corresponds to a line of sight snapshot taken at time zero. Every K2C cycles thereafter, K3C randomly chosen rows of IT are overlaid with the corresponding rows of the snapshot matrix that is next in sequence. (K2C and K3C are input parameters; see Section 10.) This overlaying process continues until simulated time has been advanced to the time at which that next snapshot was taken, at which point the intervisibility update module completes the overlaying of all rows not previously updated, and prepares to start over again with the new matrix and the one after that.

The choice of a row to be updated is achieved by choosing a pseudorandom number, call it I, between 1 and NU, where NU is the number of units in the field and also the number of rows and columns in IT. If the corresponding row of IT has not previously been updated (determined by a check of the logical matrix ITIND), it is then updated. If that row has been updated, try row I+1. If that row has been updated, try row I+2. This search process continues until either an "updatable" row is found or until the checking process circles back to row I. (This last comment implies, of course, that row NU+1 is considered to be row 1.) If no updatable row is found, nothing changes and the "intervisibility update" module has completed its task.



6. BOXES 10 and 11: THE PRODUCTION OF INTERMEDIATE OUTPUT

This section of code controls the production of intermediate error output as portrayed in figure 3, and which is discussed in Section 11.

Basically, this module's function is to convert the statistics accumulated in Box 6 to a form that is more meaningful for output. For example, sums of previous errors are divided by the appropriate number to obtain averages, coordinate error counts are made to produce quadrant counts, etc.

The frequency with which the intermediate error output is produced is controlled by an input parameter called K1C. The output summary is provided at the end of every K1C cycles.



7. BOX 12: UPDATE THE STATIONARY UNIT LIST

The stationary unit list (logical matrix FXD) is a list that contains "known" information regarding which units are moving and which units are not moving throughout the simulation. By "known" is meant that this information is available to the position location algorithms.

There are two types of real world scenarios that the matrix FXD has been instrumental in simulating. The first of these is the situation where units stop and start throughout the "battle", and send a signal back to the master computer indicating that they have just stopped or that they have just started moving. The second scenario is one in which certain units are "surveyed in" and never move, whereas no other units are ever treated as fixed. Knowledge of these facts is very helpful to the position location algorithms, but the "how" and the "why" of that helpfulness will not be discussed here. For that information, the reader is referred to Section 3 of the parent document to which this Working Paper is an appendix.

In the current version of WHERSM, the starting and stopping of units mentioned above is achieved by maintaining the matrix FXD, and by updating it in a random manner that is controlled by parameters which are input to the simulation. For each unit, FXD is "TRUE" if that unit is currently fixed, and "FALSE" if that unit is currently moving. The input parameter PSS(2) is the average time a unit remains fixed once it stops moving, while PSS(1) is the average time it keeps moving once it starts moving. These times are converted to probabilities, stored back into PSS(1) and PSS(2), and those probabilities in turn are used to determine, at each cycle, whether a unit should have its state ("fixed" or "moving") changed.

The determination of state changes is precisely the purpose of the "stationary list update" module. It is achieved by obtaining a uniformly distributed (0,1) pseudo-random number from the internal subroutine RU, and, if that number is less than the appropriate PSS probability value, changing the state of that particular unit.



It should be noted that in the second scenario mentioned above, one of course does not want the stationary unit list to be changed at all during the simulation. This can be guaranteed simply by letting the values of PSS(1) and PSS(2) at input time be very large numbers. It should also be noted that FXD is initialized at input time.



8. BOXES 13 and 14: PRODUCE THE X-Y PLOTS

This module is very small, consisting mainly of two calls to sub-routine GRAPH. The first call produces x-y plots of the true positions of all the units, and the second call produces x-y plots of the estimated positions of all the units.

There are eight parameters in the call statement for subroutine GRAPH: N, X, Y, IWRD, XMAX, XMIN, YMAX, and YMIN. N is the number of points to be plotted, X and Y are vectors of the x and y coordinates of the points to be plotted, IWRD contains either 'TRUE' or 'EST.' depending on whether the points to be plotted are true or estimated positions, and XMAX, XMIN, YMAX, and YMIN are the upper and lower limits of the axes. Those last (XMAX through YMIN) are part of the input to the simulation program.

For a description of the plots that are produced, see Section 11.

The frequency with which the plots are produced is controlled by
the input parameter K4C; the plots are produced after every K4C cycles.



9. BOX 15; THE END OF SIMULATION

Box 15 of the flowchart in figure 1 is the only one that does not correspond to an easily recognizable module in the WHERSM code. Rather, its function is performed by a set of IF statements scattered throughout the other modules. The IF statements are all identical; they test whether the number of cycles required to run the simulation for the length of time indicated by the input parameter SIMTIM have been completed. If so, then a final set of "intermediate" output is produced before termination.



10. THE INPUT TO THE SIMULATION

There are three types of input used in the WHERSM program: input from cards, tape input, and "hardwired" input in the form of DATA and PARAMETER statements inserted in the program deck. This section will discuss each type of input with regard to input values and formats. Card input is explained first.

The "Catch-All" Cards: These cards contain the various parameters and constants needed by the program; there are two of these cards, and the table below explains their contents. For a definition of the variables mentioned, see Appendix A.

	Columns	Format	Variable Name
Card No. 1:	1-5	15	NU
	6-10	15	NS
	11-15	15	K1C
	16-20	. 15	K2C
	21-25	15	к3с
	26-30	15	K4C
•	31–35	15	INR .
	36-40	. I5	NSP
	41–50	F10.5	PSS(1)
	51-60	F10.5	PSS(2)
	61-70	F10.5	BND
	71-80	F10.5	BNDSP
Card No. 2:	. 1–10	F10.5	CYCTM
	11-20	F10.5	SIMTIM
	21-30	F10.5	XMAX
	31-40	F10.5	XMIN
	41-50	F10.5	YMAX
	51-60	F10.5	YMIN



The "Reporting Units" Cards: These cards contain the unit numbers of the units that will be used at the start of the simulation as reporters. More specifically, the elements of the matrix RPT that correspond to the numbers that appear on the Reporting Units Cards are the only elements that are initialized to the logical value "TRUE". All others are initialized to "FALSE". There are 20 numbers per card, each with a format of I4. The number of unit-numbers that appear on these cards is the value of INR (see Catch-all cards above). Consequently, there will be [(INR-1)/20] + 1 Reporting Units cards.

The "Fixed Units" Cards: These cards contain the unit numbers of the units that will be used at the start of the simulation as fixed units. The elements of the matrix FXD are initialized in the same manner as are the elements of the matrix RPT above. The format for each card again is 2014, and there will be [(NSP-1)/20] + 1 of these cards.

The "Type" Cards: The type cards contain the type number for each unit in the simulation. There currently are four unit types:

Type Number	<u>Type</u>	Speed				
1	Foot Soldier	1 1/2 - 2 km/h				
2	Ground Vehicle	8-10 km/h				
· 3	Low Performance Aircraft	161 km/h				
4	High Performance Aircraft	322 km/h				

There will be exactly NU of these type numbers each with a format of I4, and therefore [(NU - 1)/20] + 1 Type cards.

The 'Movement' Cards: These cards contain all the information needed by the program so that it can provide for the movement of units. There will be one of these cards for each unit in the scenario, hence NU cards in all. Their contents are as follows:



Card Columns	Format	Meaning
1-3	13	Unit number
4-21	3A6	Unit ID (anything)
		Starting latitude:
22-24	. I3	Degrees
25-26	12	Minutes
27-28	12	Seconds
7		Starting longitude:
29-31	13	Degrees
32-33	12	Minutes
34-35	12	Seconds
37-40	F4.0	Time (*) (hrs.)
41-44	F4.0	Azimuth (deg.)
45-48	F4.0	Speed (km/h)
50-53	F4.0 ·	Time (*) (hrs.)
54-57	F4.0	Azimuth (deg.)
58-61	F4.0.	Speed (km/h)
63-66	. F4.0	Time (*) (hrs.)
67-70	. F4.0	Azimuth (deg.)
71-74	F4.0	Speed (km/h)

There are two kinds of tape input used in the WHERSM program. The first of these is the tape that contains the height information in the form of a digitized terrain map. The format of this tape is as appears in figure 2, but no further discussion of format will be given here since the terrain tape was obtained directly from the Electromagnetic Compatability

^(*) By "time" is meant the length of time during which the immediately following azimuth and speed are used. Control is passed to the next set when "time runs out" for this set.



F	98																		SS													
	S ₁ S ₂ S ₃ S ₄ S ₅ S											·	-			-			S													
S O	90		Sh (sec)	r (0F)									h121,121		elevations	The maximum			86													
0-1	95	de & (min)	tal Spacing	1 0	t.)	et)	et) ····	Blank					. h2,2;		the number of	挋			\$5													
0	56	Longitude	Horizontal	Owantiza		num Elevation	Elevation (Feet)		Blank	Blank	Blank	Blank	h1,2;		on	on			\$4													
0	2 2		(sec)		13		aximum Ele	aximum Ele	aximum Ele		elevations	Bl	Bl	B]	B.	h ₁₂₁ ,		record depends	This can be	words.	-	S 33										
0	25	0 (min)	Spacing Sv	Security Class,			Mîr	Mîr	Mîr			Ma	Ma	M	Mi	M	Ma	Mā	missing el	- 1							1; h3,1		of the	per word. The	se is 4892	
C		Latitude (Vertical	Elevations per word	•			Number of					hl,1; h2		The length	stored per	record size		s -													
-	S4 S5 S6	INT	INI	INT		Ľ.	[-]						elevations	integer					S & S S S S S S S S S S S S S S S S S S													
	S ₁ S ₂ S ₃	INT	INT	INTRAD ELD	INI	TNI	INI	INT					All elev	are in					SI S2 S3													
A	೦ಜ೦	H	2	C	4	5	9	7	8	6	10	11	12																			

TOPOGRAPHIC DATA RECORD FORMAT

Figure 2 SOURCE: Clemmitt, M, op.cit.



Analysis Center which has published a report (*) that documents such tapes in detail. The terrain tape must be mounted on logical unit number 8.

The other tape used as input to WHERSM is one that is mounted on logical unit number 7 and contains the intervisibility snapshot matrices discussed in Sections 1 and 3. It is a binary tape, created as follows: Let ITB be a three-dimensional matrix that contains the set of "packed" intervisibility snapshot matrices;

ITB(I,J,1),
$$I = 1,2,...,NU$$
; $J = 1,2,...,[(NU - 1)/36] + 1$

is the snapshot matrix taken at the first discrete time value; ITB(I,J,2) is the matrix taken at the second discrete time value; etc. Then the tape should have been created using a write statement of the form;

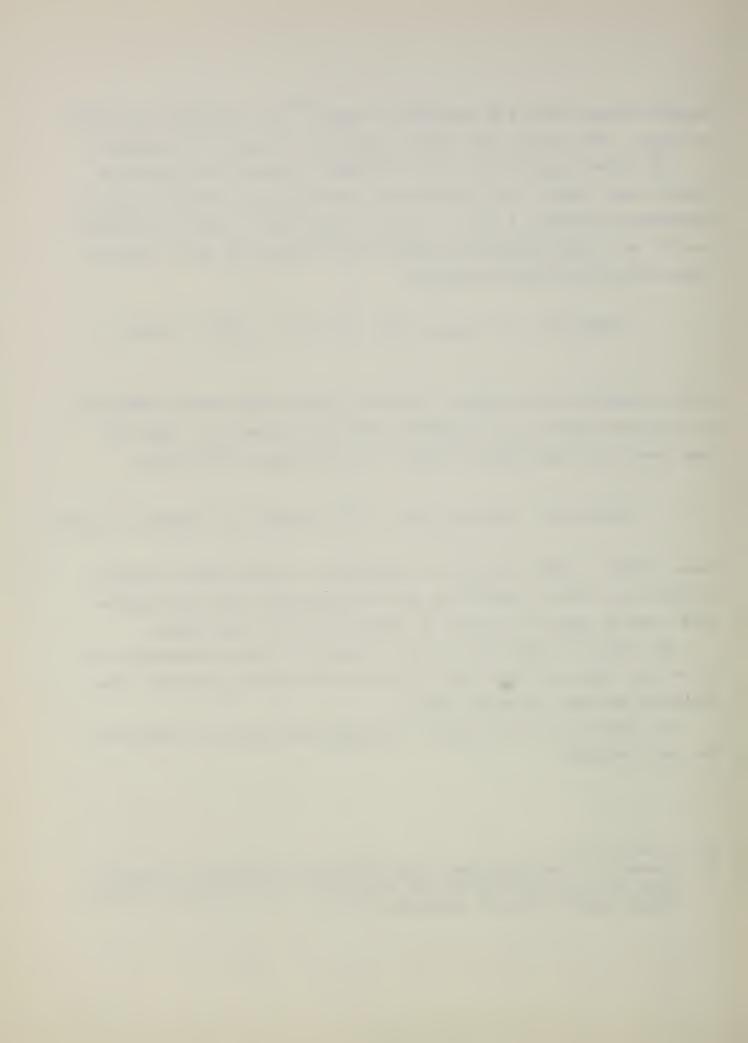
WRITE (7) (((ITB(I,J,K),
$$J = 1$$
, NITCOL), $I = 1$,NU), $K = 1$,K1)

where NITCOL = [(NU - 1)/36] + 1 (implying of course that 36 entries of each row of the 2 dimensional matrices are packed into one computer word), and K1 equals the number of snapshot matrices that exist.

The third and last type of input required to make a simulation run is the type that must physically be inserted in the program deck - the PARAMETER and DATA statement cards.

The table below lists these. The reader is referred to Appendix A for their meanings.

^(*) Clemmitt, M. and Stone, R., "The Topographic Information System", Tech. Note No. ECAC-TN-007-222, June 1969, Electromagnetic Compatibility Analysis Center, Annapolis, Md.



Variable Name	Type of Statement Contained In	Routine Contained In
MNLAT ·	DATA	BUILD
MXLON	DATA	BUILD
TPOUT	DATA	WHERSM
IFREQ ·	DATA	WHERSM
CNX	DATA	HEIGHT
CNY	DATA	HEIGHT
W	DATA	WHERSM
FXDINI	DATA	WHERSM
L1	PARAMETER	WHERSM
L2	PARAMETER	WHERSM'
L6 ·	PARAMETER	BUILD
		WHERSM
		HEIGHT
L7	PARAMETER	BUILD
	·	WHERSM
		HEIGHT



11. THE OUTPUT FROM THE SIMULATION

Figure 3 contains a sample of the intermediate output produced by WHERSM. This section explains the contents of that output sample.

The first line of output contains the cycle number of that cycle after which the summary was produced, the simulation clock time, the average real clock time the program took to provide for the processing of one subcycle, and the average time taken by the algorithms to perform one location operation.

Each row of the table contains statistics for the unit whose unit number appears in column 1. Columns 2-7 contain statistics accumulated over all cycles previous to the current one. They are, in order:

the average error in the xy-plane,
the average error in the z coordinate,
the maximum error in the xy-plane,
the cycle during which that maximum error occurred,
the maximum z error that occurred, and
the cycle during which that maximum z error occurred.

Columns 8-11 contain statistics accumulated over the previous KIC cycles. Those statistics are: the average x-y error, the average z error, the maximum x-y error that occurred, and the cycle during which that error occurred.

Columns 12-14 contain the individual coordinate errors (estimated minus true) that occurred the last time each unit was located prior to the printing of the intermediate output. Columns 15, 16, and 17 list the current values of the S,RPT, and FXD vectors respectively; and column 18 gives the current value of the W vector, the weight.

The last row of the table, which begins with the word "ALL", gives for a column of averages the average of the numbers appearing above it; and for a column of maximums, the maximum of the maximums in the column.



CYCLE CHUBER 140.

11

4199.75a S.

AVERAGE STMULATION SUPCYCLE

TIME

11

• n11't

s.

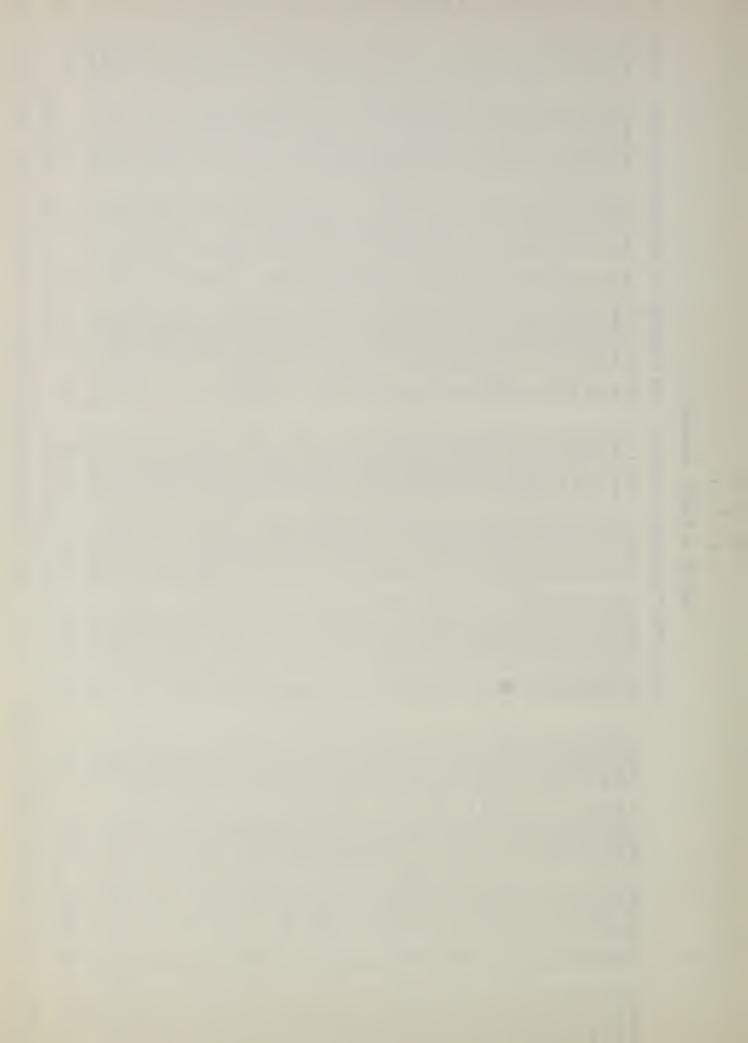
AVERAGE ALGORITHM SUBCYCLE TIME

11

.0063 5.

œ

.36377+n1 .43993+01 .16866+n2 139



The next item of output is the quadrant counts of errors. This is a display of the directions of errors. It is obtained from columns 12 and 13 of the table by counting the number of entries in those columns (by their algebraic signs) that fall in each quadrant.

The last items of output are the xy-plots, an example of which is given in figure 4. The two lines at the top of the graph state whether the graph is of true or estimated positions, list the unit numbers of the units that appear on that graph, and list the plotting symbols used to represent those units. The letters of the alphabet are used as plotting symbols, so that if more than 26 units are in the simulation, a separate graph will be produced for every 26 (or fraction thereof) units. If more than one unit occupies the same graph position, a number will appear in that graph position indicating the number of units in that position. The axis ranges are controlled by XMAX, XMIN, YMAX, and YMIN, which are part of the input to the simulation, and if points fall beyond those boundaries an annotation to the graph will appear indicating the occurence of that situation.





In this appendix, definitions of all non-trivial variables used in the three main simulation routines (BUILD, WHERSM, HEIGHT) are given. In each case, the variable being defined is underlined, and if it is a dimensioned variable, it is written exactly as that variable should appear in a DIMENSION statement. Immediately following the variable name will appear either a B,W, or H (or any combination thereof). By this is meant that the variable being defined is a variable of BUILD, WHERSM or HEIGHT.

Note: All variables conform to the FORTRAN implicit naming conventions regarding mode.

* * * * *

AVASBT W. The sum of real times used to perform position estimations.

AVKTR W. The number of time intervals accumulated in AVASBT and AVSUBT.

AVSUBT W. The sum of real times used to simulate a "real world" subcycle (includes AVASBT).

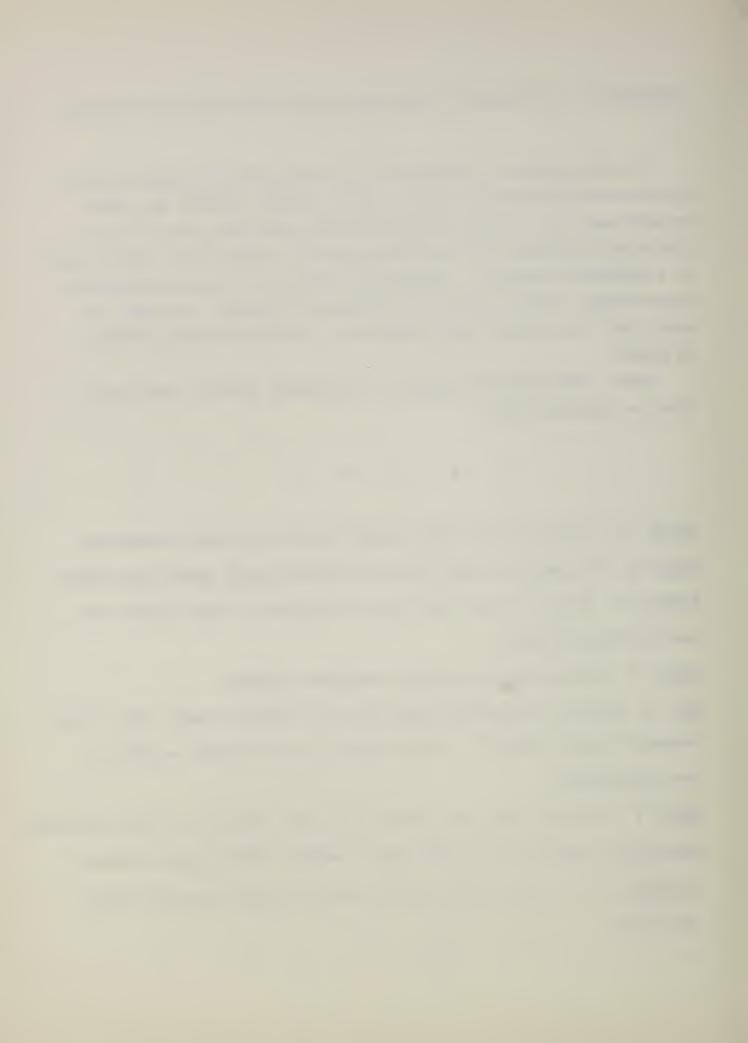
AZ(4) W. Buffer used in reading in movement azimuths.

BND W. Boundary beyond which units are not allowed to move. Unit of measurement is the kilometer. If this option is not desired, set BND to some large number.

BNDSP W. On input, the speed (km/h) with which BND moves in both directions.

Immediately converted to a value that is added to BND at every subcycle.

 $\underline{C(14641)}$ B. An output buffer that contains decoded elevations above sea level.



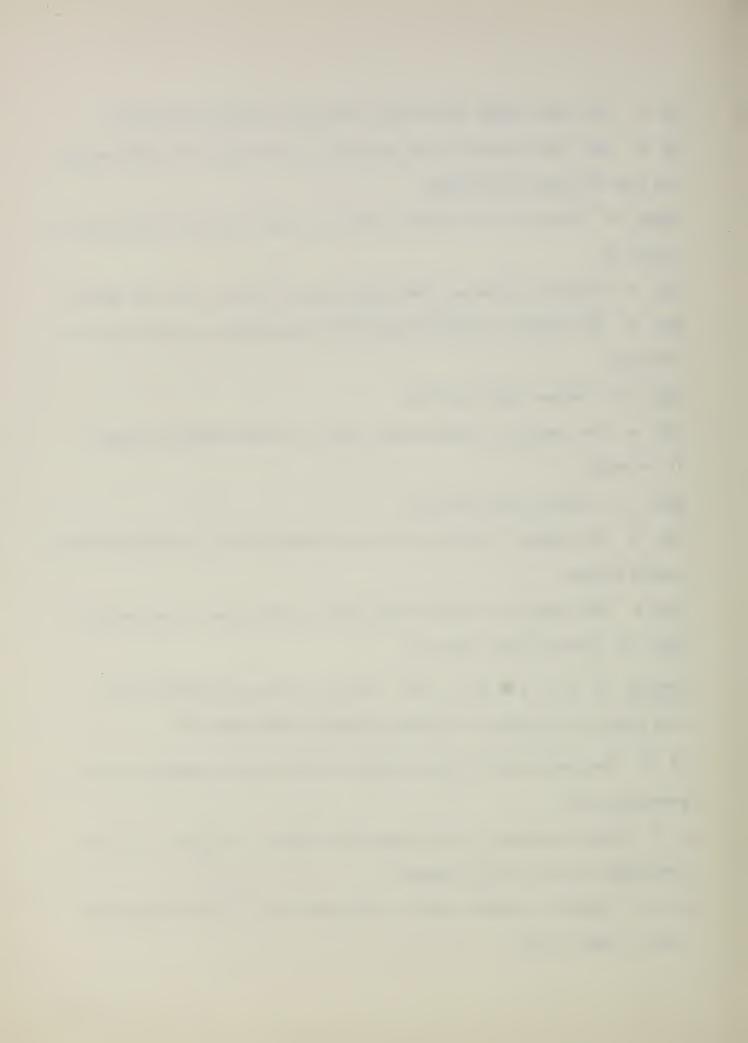
- CLK W. The simulation's clock. Contains simulated time in seconds.
- <u>CNX</u> H. The inverse of the average longitudinal distance (in meters) between grid points on the terrain tape.
- CNY H. Same as CNX but for latitude.
- CT(4) W. Input buffer used to read in the length of time a unit is to move according to a particular azimuth and speed.
- CYCTM W. The "real time" length of a cycle in seconds.
- <u>D(14641)</u> B. Output buffer that contains decoded altitudes above sea level.
- DELTA W. "Real time" length of a subcycle.
- <u>DX(L1)</u> W. List used to store the difference in the x-coordinates of the true and estimated positions. Computed immediately after a unit has had its position estimated.
- DY(L1) W. Same as DX, but for y-coordinates.
- DZ(L1) W. Same as DX, but for z-coordinates.
- EP(L1,14) W. Contains estimated positions for each unit, in addition to some data relevant to those positions. EP(I,1-3) is the estimated position of unit I which was determined the next-to-last time it served as locatee; EP(I,4-6), the last time it served as locatee. The rest of the EP matrix is used to manipulate positions when the relocation option is used (see Working Paper No. 8).
- ERR W. The error in position estimation in the xy-plane and then in the z-coordinate. The Euclidean distance between true (TP) and estimated (EP) positions is used as the error.



- IFY H. Same as IFX, but for the y-coordinate. Units of measurement here are 3 seconds of latitutde.
- IGP W. Pointer to the unit with the largest xy-error over all cycles.
- IGT W. Pionter to the unit with the largest xy-error over the last K1C cycles.
- INR W. Initial number of units allowed to report.
- IP W. Pointer used in constructing VV1.
- IPX H. The x-coordinate of some other position (for which a height is already available), after it has been converted to the units of the terrain.
- IPY H. Same as IPX, but for y-coordinate.
- IQO W. Number of units whose estimated position is exact.
- <u>IQ1</u> W. The number of units whose estimated position is in error in the direction of the first quadrant.
- <u>IQ2</u> W. Same as IQ1, but for quadrant 2.
- IQ3 W. Same as IQ1, but for quadrant 3.
- IQ4 W. same as IQ1, but for quadrant 4.
- IQUAN B. Quantization factor for the block of terrain grid points currently being decoded. (See ECAC-TN-007-222, op.cit.)
- IR W. Counter for the number of ranges computed in a particular subcycle.
- IT(L1,L3) W. The intervisibility table currently being used.
- ITB(L1,L3,7) W. The set of all intervisibility tables.
- ITIND(L1) W. Logical matrix which indicates for each row of IT, whether that row has been updated yet.



- IU W. The unit number of the unit currently serving as locatee.
- $\overline{\text{IV}}$ W. The (0-1) answer to the question of existence of an LOS between the pair of units in question.
- IVMAT W. Pointer to the intervîsibilîty matrix currently being used to update IT.
- IZT W. Pointer to the unit with the largest z-error over all cycles.
- <u>K1C</u> W. The number of cycles after which intermediate output is to be produced.
- K1CC W. Counter used with K1C.
- <u>K2C</u> W. The number of cycles after which an intervisibility update is to occur.
- K2CC W. Counter used with K2C.
- $\underline{\text{K3C}}$ W. The number of rows of IT to be updated when an intervisibility update occurs.
- $\underline{\text{K4C}}$ W. The number of cycles after which xy plots are to be produced.
- K4CC W. Counter used with K4C.
- $\overline{\text{KUF}(\text{L1})}$ W. For I = 1,2,...,NS, KUF(I) is the unit number of the unit which is to serve as locatee during the Ith subcycle.
- <u>KZ</u> W. The seed value for the internal uniform psuedo-random number generator, RU.
- L B. Status parameter for I/O processor NTRAN. L equals -1 until the completion of the I/O command.
- <u>L1</u> W. Parameter variable used in dimensioning. L1 must be greater than or equal to NU.



- L2 W. Parameter variable used in dimensioning. L2 > NS.
- L3-L5 W. Parameter variables used in dimensioning, but since they are strictly dependent on L1, they are automatically set.
- <u>L6</u> B,W,H. Conceptually organize all the 6' x 6' terrain blocks on the terrain tape according to the latitude-longitude of their southwest corner. L6, then, is the number of these blocks when counting from west to east.
- L7 B,W,H. Same as L6, but count from south to north.
- LOCATR(L1) W. The unit numbers of the units whose ranges are being reported in a given subcycle.
- M W. Status parameter for I/O processor. See L.
- M1 B. Status parameter for I/O processor. See L.
- M2 B. Status parameter for I/O processor. See L.
- MAXCYC W. The length of the simulation in terms of cycles.
- MNLAT B. The minimum latitude (in seconds) for which a height is available on the terrain tape.
- MXLON B. The maximum longitude (in seconds) for which a height is available on the terrain tape.
- NBITS B. The number of bits into which the elevation in question is "packed".
- NCYC W. The cycle number of the cycle currently being processed.



NDX(L6,L7) B,H. An index to terrain blocks that are written on the drum by BUILD. NDX(1,1) is the position of the 6' x 6' terrain block whose southwest corner is identified by (MNLAT, MXLON); NDX(1,2) is the position of block (MNLAT, MXLON + 3600); NDX(2,1) is block (MNLAT + 3600, MXLON); etc.

NITCOL W. The number of computer words in a packed row of the intervisibility matrices.

NS W. The number of subcycles in a cycle.

NSP W. The number of units which, at the start of the simulation, will be identified as being stationary.

NTYPE(4) W. The unit type of each unit. If NTYPE(I) is 1,2,3, or 4, then unit I is respectively a foot soldier, a ground vehicle, a low performance aircraft, or a high performance aircraft.

NU W. The number of units in the simulation.

NUMEL B. The number of elevations per word for a given terrain block represented by a logical record on the terrain tape.

PSS(2) W. At input time, PSS(1) is the average time a unit keeps moving once it starts moving, and PSS(2) is the average time it remains fixed once it stops. Subsequently, they are the probabilities of changing state. If no random starting and stopping is desired, set both PSS(1) and PSS(2) to very large numbers on the catch-all-cards.

RANGE(L1) W. The ranges being reported for a given subcycle.



RCON W. Constant used in converting a speed and azimuth combination into direction cosines.

RPT(L1) W. Logical matrix that indicates for each unit, whether or not that unit is a unit that is allowed to report ranges.

<u>S(L1)</u> W. Logical matrix that indicates for each unit whether or not that unit was "successfully" located the last time a position estimation was attempted. S is set by the position location algorithms.

SIMTIM W. The "real time" length of the simulation, in minutes.

SP(4) W. Input buffer used in reading in speeds for each unit.

STAT1(L1,10) W. For each row: column 1 is the sum of position estimation errors (in xy-plane) over all cycles for the unit associated with that row; column 2, the maximum xy-error that occurred over all cycles for that unit; column 3, the cycle number of the cycle during which that maximum error occurred; 4, the partial sum of xy-errors over the current K1C cycles; 5, the maximum xy-error over the current K1C cycles; 6, the cycle number associated with that error; 7, the sum of the z-errors over all cycles for that unit; 8, the maximum z-error over all cycles; 9, the cycle number associated with that z-error; and 10, the partial sum of z-errors over the current K1C cycles.

STAT2(L1,2) W. Column 1 contains, for each unit, the number of times that unit was "successfully" located since the start of the simulation; and column 2, the number since the start of the current K1C cycles.



 $\overline{\text{TLOC}(\text{Ll},4)}$ W. The clock time at which the estimated positions in EP were obtained.

 $\underline{\text{TP}(L1,3)}$ W. The current true position of each unit. $\underline{\text{TP}(I,1)}$ is the x-coordinate; $\underline{\text{TP}(I,2)}$, the y-coordinate; and $\underline{\text{TP}(I,3)}$, the z-coordinate.

TPOUT W. Logical variable that allows for the writing of all intermediate output on logical unit 9, in addition to the standard output unit.

<u>T1-T4</u> W. Parameters in calls to the system's clock. Used in determining AVASBT and AVSUBT.

<u>VV(L1,4)</u> W. Currently used velocity vector for each unit. Column 1 is the x component; column 2, the y component; 3, the time at which that vector should no longer be used; and 4, a pointer into VV1 where the next velocity vector to be used resides.

 $\underline{VV1}(L5,4)$ W. The set of all velocity vectors for all units. The format of each vector is the same here as in VV, but the h (h \leq 3 currently) vectors for unit number 1 are in rows 1 through h of VV1, followed by the vectors for unit number 2, etc.

 $\underline{W(L1)}$ W. Vector used by the position location algorithms to weight the various estimates (see Working Papers No. 7 and 8). W should be initialized to the weight to be assigned to non-fixed units at the start of the simulation.

XMAX, XMIN, YMAX, YMIN W. The upper and lower bounds of the x-and y-axes (in meters) to be used in producing the xy-plots.



<u>ZPSUM</u> W. The sum of the position estimation errors (in the z-coordinate) over all units over the last KlC cycles.

 $\overline{\text{ZTSUM}}$ W. The sum of the position estimation errors (în z-coordinate) over all units over all cycles.



APPENDIX B: LISTING OF THE SIMULATION PROGRAM



G MAP ZAP, ZAP	ZAP	economic control and a second probability of control and control and control and control and control of contro	01 JUN 72	10:55:40,867
1.2.	CHN 1 SEG BUTLD			
ы д • д	CHN 2 SEG WHERSM			
MAP LCC 1104 0036	. 9200 h01			and the second of the second o



10:55:41.23

MAIN PROGRAM

STORAGE USED (BLOCK, NAME, LENGTH)

EXTERNAL REFERENCES (BLOCK, NAME)

0003 NTRAN 00004 CHAIN 00005 NWDU\$ 0006 NIO25 STORAGE ASSIGNMENT FOR VARIABLES (BLOCK, TYPE, RELATIVE LOCATION, NAME)

3 151	2 2201	2 50L	2 9101	CNX	T. P.	-	CON	3 42	}-
000123	00037	00011	71000	00000	01161	11456	11457	11456	111160
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	_				_		. C		_
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ار 0	00	4UL.	٥٢	30L		BIT	×	NLAT	BITS
21 1	2 /41	20 2	71 7	71 9	010	77 II	84 X	00	75 N
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			٠						

פה

PARAMETER L6=5,L7=11	PARAMETER LB=L6*L7	COMMON MALATOMACON CONT. NOX (16.17)	DIMENSION IA (5000) • 18 (5000) • C (14641) • D (14641)	DATA NDX/L8*-1/	DATA MNLAT MXLOV/2544+4302/	CALL NTRAN(8,22)	CALL NTRAV(35,22)	OHON.	Y 110	C READ FIRST RECORD.	CALL NTRAN(8,2,5000,1A,L)	C WAIT FOR END OF TAPE READ.	10 IF (L+1) 20,10,30	C IF ERROR, 900. IF EDF, 200.	20 IF (L+2) 900,200,30	30 D0 40 I=1,L
**	*	*	* †	2*	*9	1 *	8*	*6	10*	11*	12*	. 13*	14*	15*	16*	17*
.10100	00103	00100	00105	00100	00110	00113	00114	00115	00116	00116	00117	00117	00120	00120	00123	00126



```
COMPUTE ITS RELATIVE POSITION IN THE TERRAIN AND SET INDEX
                                                                                                       ELEVATIONS PER WORD, QUANTIZATION FACTOR OF BITS PER ELEVATION.
                                                                                                                                                                                                                                                                                                                                                   THE
                                                                                                                                                                                                                                                                                                                                                  (PROCEDURE IS
                      OF FIRST TERRAIN BLOCK
                                                                                                                                                                                                                                                                                               WAIT FOR CHANCE TO WRITE OUT THIS TERRAIN BLOCK.
                                                                                                                                                                                         DECODE ELEVATIONS IN THE FIRST TERRAIN BLOCK.
                                                                                                                                                                                                                                                                                                                                                  BEGIN PROCESSING SECOND TERRAIN BLOCK.
                                                                                                                                                                                                                                                                                                                                                            SAME AS FOR THE THE FIRST BLOCK.)
                     DECODE LATITUDE AND LONGITUDE
READ.
                                                                                                                                                                                                                                C(I)=(IEL*IQUAN+IBIAS)*.3048
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     D(I)=(IEL*IQUAN+IBIAS)*•3048
INITIATE THE NEXT TAPE
                                                                                                                                                                                                                                                                                                                                        NTRAN(35,1,14641,C,41)
                                                                                                                                                                                                                      IEL=FLD(IBIT,NBITS,IB(N))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          IEL=FLD(IBIT,NBITS,IB(N))
            NTRAN (8, 2, 5000, IA, L)
                                                                                                                                                                                                                                                      60 TO 68
                                                                                                      DECODE NUMBER OF
                                                                                                               BIAS, AND NUMBER
NUMEL=FLD(0,6,18(5))
                                                                                                                                     OUAN=FLD(18,18,18,18(5)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    QUAN=FLD(18,18,18,18(N))
                                                                                                                                                                                                                                                                                                                   910,920,70
                                         LON=FLD(18,18,18(3))
                                                                                                                                                                                                                                                                                                                                                                                                                                                         JUMEL = FLD (0,6, TB(N))
                                                                                                                                                                                                                                                                                                                                                                                                     .ON=FLD(18,18,18(N))
                                _AT=FLD(0,18,IB(3))
                                                                                                                                                                                                                                                                                                                              WRITE IT OUT.
                                                                                                                                                                                                                                                                                                                                                                                            _AT=FLD(0,18,IB(N))
                                                                                                                                                                                                                                                                                                          69,68,70
                                                                        I=(LAT-WNLAT)/6+1
                                                                                   J= (MXLON-LON) /6+1
                                                                                                                                                                                                                                                                                                                                                                                                                = (LAT-MNLAT) /6+1
                                                                                                                                                                                                                                                                                                                                                                                                                          J= (MXLON-LON) /6+1
                                                               TO THE DRUM.
                                                                                              ZDX (I • C) = X * 1 4 6 4 1
                                                                                                                                                                                                                                                      [F (I.E0.14642)
                                                                                                                                                                                                                                                                                                                                                                                                                                     ZDX(I+C)=X*14641
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         IF (I.EQ.14642)
                                                                                                                                                                                                                                                                IBIT=IBIT+NBITS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   IBIT=IBIT+NBITS
                                                                                                                                                                                                             DO 60 M=1.NUMEL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                DO 90 M=1,NUMEL
                                                                                                                                                           NBITS=36/NUMEL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        VBITS=36/NUME
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              BIAS=IB(N+1)
                                                                                                                                               (BIAS=IB(6)
                                                                                                                                                                                                                                                                                                          (M2+1)
                                                                                                                                                                                                                                                                                                                    (M2+2)
                                                                                                                                                                                                                                                                                                                                                                                  11B(5)+t
                                                                                                                                                                                                                                                                                      60 TO 50
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       IBIT=0
                                                                                                                                                                                                    IBIT=0
                                                                                                                                                                                                                                                                                                                                                                                                                                               2+217
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READ THE TWO DECODED RECORDS AT END OF TAPE
                                                                                                                                                                                              GIVE MESSAGE AND ABORT.
                                                                                                                                                                                                                                                                LAST READ WAS 2110)
CURRENT IS 2110)
CURRENT IS 2110)
                                                                                                                                                                          60 CHAIN IN THE SIMULATION.
                            CALL NTRAN(35,1,14641,0,42)
                                                                                                                                            CALL NTRAN(35,1,14641,0,41)
                                                                                                                 NTRAN (35,1,14641,C,M1)
                                                                                                                                                                                                                                                                 TAPE READ.
DRUM WRITE.
                                                                                                       NTRAN(8,2,14641,D,L)
                                                                          NTRAN (8,2,14641,C,L)
                                                                                                                                                                                              ERROR HAS OCCURRED.
                                                                                                                                                                                                                                                                                  ON DRUM.
                                                        GOOD RUN SO FAR.
NTRAN(8,22)
                   IF (M1+2) 910,920,100
                                                                                   (L+1) 211,210,220
                                                                                             F (L+2) 900,900,220
                                                                                                                          (L+1) 231,230,240
                                                                                                                                   IF (L+2) 900,900,240
                                                                                                                                                                VDX (3,6)=(K+1)*14641
         99,98,100
                                                                                                                                                                                                       LATILON
                                                                                                                                                                                                                          WRITE(6,2) LATILON
                                                                                                                                                                                                                                             WRITE(6,3) LAT.LON
                                                                                                                                                       NDX (3,5) = K*14641
                                                                                                                                                                                    CALL CHAIN(2.T)
                                                                                                                                                                          GOOD RUN.
                                                                                                                                                                                                       WRITE(6,1)
                                                                                                                                                                                                                                                                                  FORMAT ( / V
         (M1+1)
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TOTAL COMPILATION TIME = 1 SEC

0 *DIAGNOSTIC* MESSAGE(S)

UNIVAC 1108 FORTRAN V COMPILATION.

END OF

PHASE PHASE PHASE PHASE



10:55:42.867

01 JUN 72

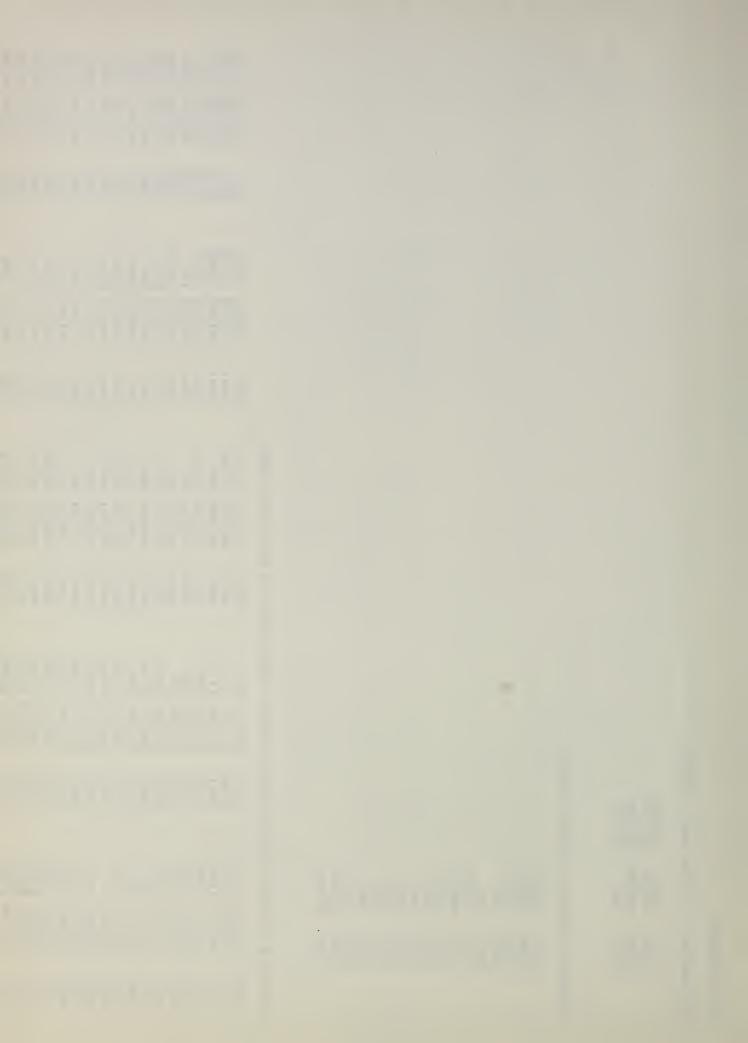
MAIN PROGRAM

STORAGE USED (BLOCK, NAME, LENGTH)

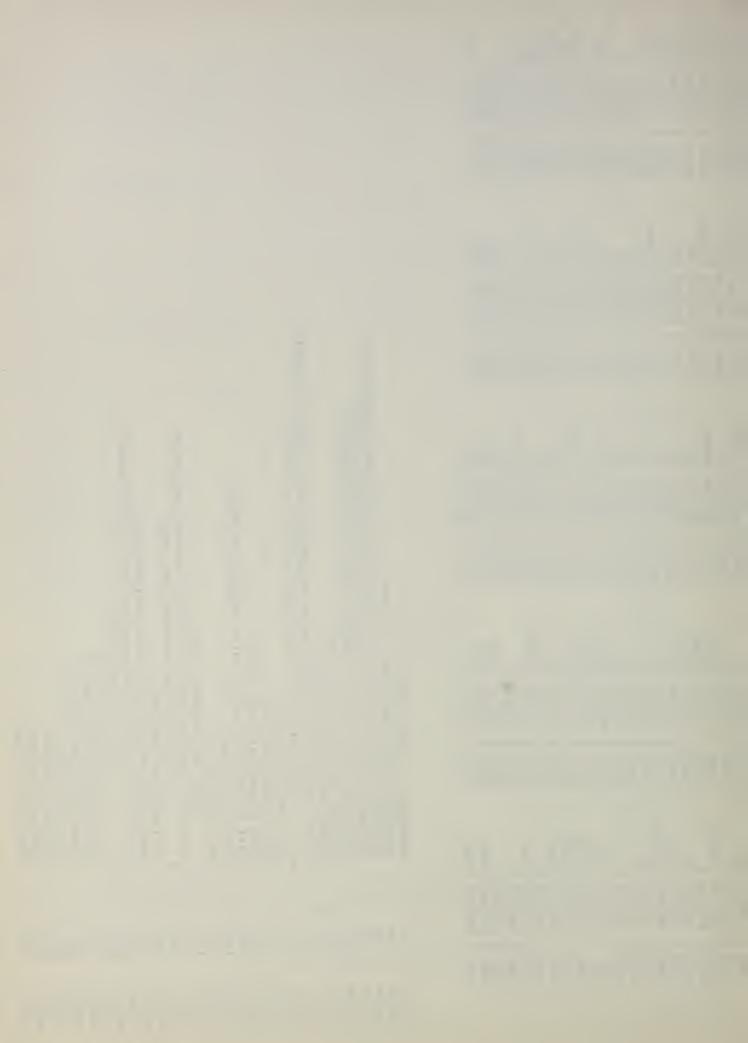
EXTERNAL REFERENCES (BLOCK, NAME)

00094 HEIGHT 0005 GRAPH 00006 CLOCKS 00010 RG 0011 FINDIT 0012 NIDUS 0013 NIDUS 0015 NWDUS 0015 NWBUS 0020 NWBUS 0021 SORT 0022 NWEFS STORAGE ASSIGNMENT FOR VARIABLES (BLOCK, TYPE, RELATIVE LOCATION, NAME)

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001302 1020L 001415 1130L 001503 1260L	•				_			
0001	0000	0001	0001	000	0001	0001	0001	0001
002140 10156 001375 1120L 001433 1200L							_	
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001201 1000L 001357 1110L 051363 12F								
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051333 10F 051342 11F 002530 11776								
0000	00000	0000	0000	0001	0001	0001	0001	0001:
051263 1F 002255 10636 001433 1140L								
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                                                                                                                                                                                                                                                   COMMON /CB1/EP(L1,14),LOCATR(L4),RANGE(L4),S(L1),TLOC(L1,4),W(L1)
IU,CLK,XNEW,YNEW,ZNEW,FYD(L1),RPT(L1),NTYPE(L1)
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                                                                                                                                                                                                                       DIMENSION STATI(L1,10), TP(L1,3), VV(L1,4), VV1(L5,4), DX(L1)
                                                                                                                                                                                                                              DIMENSION DY(L1), DZ(L1), TFREG(4), TTB(L1, L3,7), ITIND(L1)
                                                                                                                                                                                                                                                                                                                                                WRITE(6,13) NU.NS,KIC,K2C,K3C,K4C,INR,NSP,SIMTIM,MAXCYC
        AVASBT
                      CYCTM
                                   GPSUM
               BNDSP
                                                                                                           NITCOL
                                                                                                                                                                                                                                                                                                                   READ(5,3) NUINSIKICIKZCIKGCINRINRINSPIPSSIBNDIBNDSPI
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                                                                                                                                                                                                                                                                                                                                         MAXCYC=(60.0*SIMTIM+DELTA)/(FLOAT(NS)*DELTA)
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                                                                                                                                                                                                           L3=L1/36+1, L4=L1+1, L5=3*L1
                                                                                                                                                                                                                                                                                                             INPUT THE CATCH-ALL-CARDS.
                                                                                                                                                                                                                                                                                                                                                        DELTA, PSS, BND, BNDSP
                                                                                                                                                                                                                                     LOGICAL S.FXD. RPT. TPOUT. ITIND
                                                                                                                      REW
                           DZ
GPKTR
                                        FRED
                                                                                                  LOCATE
                                               Pos
                                                                                                                                                                                                                                                                                KZ.RADS/3141.57.295779/
                                                                                                                                                                                                                                            COMMON MNLAT MXLON CNX CNY
                                                                                                                                                                                                                                                                                                                                                               PSS(1)=CYCTM/(PSS(1)*60.0)
                                                                                                                                                                                                                                                                                                                                                                      PSS(2)=CYCTM/(PSS(2)*60.0
                                                                                                                                                                                                                                                                                                                                                                             RCON=DELTA/3600.0*1000.0
     003072
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                                                                                                                                                                                                                                                                                                                                  DELTA=CYCTM/FLOAT (NS)
                                                                                                                                                                                                                                                                 TPOUT /. FALSE.
                                                                                                                                                                                                                                                                                                                                                                                                  SIMTIM=60.0*SIMTIM
                                                                                                                                                                                                                                                                                                                                                                                                         NITCOL=(NU-1)/36+1
                                                                                                                                                                                                                                                                                                     FXDINI/1.0/
                                                                                                                                                                                                                                                                                                                                                                                           BNDSP=BNDSP*RCON
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COMPUTE NUMBER OF SUBCYCLES BETWEEN LOCATION OPERATIONS FOR
                                                                                                                                                                                                                                                                                                                                                                                                                              SLOT FIRST TRIED IS NOT AVAILABLE, AN AVAILABLE ONE IS FOUND.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        READ(5:30) IU.II.I2.I3.J1.J2.J3.(CT(J).AZ(J).SP(J).J=1.3)
INPUT THE INITIAL REPORTING UNITS, AND SET UP RPT.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CONVERT DEGREES, MINUTES, AND SECONDS TO SECONDS.
                                                                                  INPUT THE INITIAL FIXED UNITS, AND SET UP FXD.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           INPUT MOVEMENT DATA AND STARTING POSITIONS.
                                                                                                                                                                                                                                        MAKE THE UNIT TO SLOT ASSIGNMENTS.
                                                                                                                                                                                                                                                                                                                                                                                               EP(I,14)=FLOAT(NS)/(5.*FLOAT(I1))
                                                                                                                                                                                                                                                                                                                                                                                                                                             TRY ADJACENT SLOTS UNTIL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               F (KUF(IPOS), EQ.0) GO TO 260
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     SN-S04I=S04I (SN-10-S04I) 4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        F (IPOS.6T.NS) IPOS=IPOS-NS
                                                                                                                                                                                                                             WRITE(6.8) (NTYPE(I),I=1,NU)
                                                                                                                                                                                                        READ(5,4) (NIYPE(I),I=1,NU)
                                                                                                                                                                                                                                                                                                                                                                                                                                   FIND SLOT TO ASSIGN.
                                                                                                                                                                                            INPUT THE UNIT TYPES.
               READ(5.4) (KUF(I),I=1,INR)
                                                                                                                                 WRITE(6,8) (KUF(I),I=1,NSP)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  WRITE(6,8)(KUF(I),I=1,NS)
                                      WRITE(6,8) (KUF(I), I=1, INR)
                                                                                                            READ(5.4) (KUF(I), I=1, NSP)
                                                                                                 IF (NSP.EQ.0) 60 TO 240
                                                                                                                                                                                                                                                                                                                                                                                                                                                          POS=IPOS+I2+INT(REM)
                                                                                                                                                                                                                                                                                                                                                 =FLOAT(NS)/FLOAT(I1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   11=(11*60+12)*60+13
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               J1=(J1*60+J2)*60+J3
                                                                                                                                                                                                                                                                                        DO 270 I=NU.1.-1
                                                                                                                                                                                                                                                                                                                THIS UNIT.
                                                                                                                                                                                                                                                                                                                                                                                                            DO 260 13=1,II
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DO 500 I=1.NU
                                                                                                                                                DO 210 I=1,NSP
                                                    DO 200 I=1, INR
                                                                                                                                                                                                                                                                  DO 241 I=1,NS
                                                                                                                                                                                                                                                                                                                                                                         (=X-FLOAT (·I2)
                                                                            RPT(J)=.TRUE.
                                                                                                                                                                                  FXD(J)=.TRUE.
                                                                                                                                                                                                                                                                                                                                      1=1FRE0(11)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           WRITE(6,11)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              P0S=IP0S+1
                                                                                                                                                                                                                                                                                                                           1=NTYPE(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 KUF (IPOS)=I
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       WRITE(6,10)
                                                                                                                                                                                                                     WRITE(6,18)
                                                                                                                                                                      W(J)=FXDINI
                                                                                                                        WRITE(6,9)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      30 TO 250
                              WRITE(6.7)
                                                                                                                                                                                                                                                                                                                                                                                                                           REM=REM+X
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CONTINUE
                                                                                                                                                                                                                                                                            KUF(I)=0
                                                                                                                                                                                                                                                                                                                                                                                       REMHO.0
                                                                  J=KUF(I)
                                                                                                                                                              IPOS=0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        [P=1
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WRITE(6,12) IU.NTYPE(IU),(TP(IU.J),J=1,3),AZ(1),SP(1),CT(1)
                                                                             HEIGHT (-1.,-1.,TP(IU,1),TP(IU,2),TP(IU,3),M)
CONVERT MOVEMENT DATA INTO DIRECTION COSINES AND BUILD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CALL GRAPH(NU.TP(1,1),TP(1,2),'TRUE',XMAX'XMIN,YMAX,YMIN)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        INITIALIZE IT, THE CURRENT INTERVISIBILITY TABLE.
                                                                                                                                                                                                                                                                                                                                                                                                                             IF (TPOUT) WRITE(9) ((TP(I,J),J=1,3),NTYPE(I),I=1,NU)
                            A RANDOM ALTITUDE ASSIGNED TO THEM.
                                                                                                                                                                                                                                                                                                                                        WRITE(6,6) (AZ(J),SP(J),CT(J),J=2,J12) .
INITIALIZE EP, THE ESTIMATED POSITIONS MATRIX.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            * * BEGIN THE PROCESSING OF A CYCLE. *
                                    IF (NTYPE(IU).E0.3) TP(IU.3)=100.+5000.*RU(KZ)
IF (NTYPE(IU).E0.4) TP(IU.3)=100.+4000.*RU(KZ)
GO TO 425
                                                                                                                                                                                     VV1(IP,1)=COS((AZ(J)-90.0)/RADS)*SP(J)*RCON
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  READ(7) ((ITB(I,J,K),J=1,NITCOL),I=1,NU)
                                                                                                                                                                                                                                                                                                                                                                                                                                           INPUT THE INTERVISIBILITY TABLES.
                                                                                                                                                                                                                                                                                                  WAIT FOR END OF HEIGHT RETRIEVAL.
                                                                                                                                                                                                 VV1(IP,2)=COS(AZ(J)/RADS)*SP(J)*RCON
           TP(IU,2)=(I1-MNLAT*60)/(3.0*CNY)
                                                                            INITIATE HEIGHT RETRIEVAL.
                                                                                                                                                                                                                                               F (CT(J), GT.SIMTIM) GO TO 460
TP(IU, 1) = (MXLON*50-J1) / 13.0*CMX
                      IF (NIYPE(IU).LT.3) GO TO 390
                                                                                                                                            IF (CT(J).LE.0.0) GO TO 460
                                                                                                           THE VELOCITY VECTORS.
                                                                                                                                                                                                                                                                                                                                   IF (J12,E0.1) GO TO 500
                                                                                                                                                                                                                                                                                                              IF (M.Eg.-1) GO TO 470
                                                                                                                                                                                                                                                                                                                                                                    DO 480 J=1.3
EP(IU.J)=TP(IU.J)
EP(IU.J+3)=TP(IU.J)
EP(IU.J+6)=TP(IU.J)
                                                                                                                                                                   IF (J.EQ.1) GO TO 430
                                                                                                                                                                                                                                                                                                                                                                                                              EP (IU. J+9)=TP (IU. J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  IT(I,J)=ITB(I,J,1)
                                                                                                                                                                               CT(7)=CT(7)+CT(7-1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DO 530 J=1,NITCOL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    SN-1=61 006h 00
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              CALL CLOCKS(T1)
                                                                                                                                                          CT(J)=3600.*CT(J)
                                                                                                                                                                                                                                                                                  VV1 (IP-1,4)=-5.0
                                                                                                                                                                                                                            VV1 (IP, 3) =CT(J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              DO 530 I=1.NU
                                                                                                                                                                                                                 VV1(IP,4)=IP+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                            DO 520 K=1,7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          NCYC=NCYC+1
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          K4CC=K4CC+1
                                                                                                                                     DO 450 J=1.3
                                                                                                                          VV(IU,4)=IP
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                                                                                             CALL
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WRITE(6,12) IU.NTYPE(IU), (TP(IU, J), J=1,3), AZ(1), SP(1), CT(1)
                                                                          INITIATE HEIGHT RETRIEVAL.
HEIGHT(-1.,-1.,TP(IU,1),TP(IU,2),TP(IU,3),M)
CONVERT MOVEMENT DATA INTO DIRECTION COSINES AND BUILD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CALL GRAPH(NU.TP(1,1),TP(1,2),TRUE",XMAX,XMIN,YMAX,YMIN)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          INITIALIZE IT' THE CURRENT INTERVISIBILITY TABLE.
                                                                                                                                                                                                                                                                                                                                                                                                                             IF (TPOUT) WRITE(9) ((TP(I,J),J=1,3),NTYPE(I),I=1,NU)
                                 AIRCRAFT HAVE A RANDOW ALTITUDE ASSIGNED TO THEM. (NITYPE(IU).E0.3) TP(IU.3)=100.+5000.*RU(KZ)
                                                                                                                                                                                                                                                                                                                                         WRITE(6,6) (AZ(J),SP(J),CT(J),J=2,J12)
INITIALIZE EP, THE ESTIMATED POSITIONS MATRIX.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             * * * BEGIN THE PROCESSING OF A CYCLE. *
                                                       (NIYPE(IU).E0.4) TP(IU.3)=100.+4000.*RU(KZ)
                                                                                                                                                                                         VV1(IP,1)=COS((AZ(J)-90.0)/RADS)*SP(J)*RCON
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  READ(7) ((ITB(I,J,K),J=1,NITCOL),I=1,NU)
                                                                                                                                                                                                                                                                                                                                                                                                                                            INPUT THE INTERVISIBILITY TABLES.
                                                                                                                                                                                                                                                                                                     WAIT FOR END OF HEIGHT RETRIEVAL.
                                                                                                                                                                                                      VV1(IP,2)=COS(AZ(J)/RADS)*SP(J)*RCON
                                                                                                                                                                                                                                                  1F (CT(J), GT, SIMTIM) GO TO 460
                  FP(IU,2)=(I1-MNLAT*60)/(3.0*CNY)
                              IF (NIYPE(IU).LT.3) GO TO 390
                                                                                                                                                  IF (CT(J).LE.0.0) GO TO 460
                                                                                                                  THE VELOCITY VECTORS.
                                                                                                                                                                                                                                                                                                                                      IF (J12,E0.1) GO TO 500
                                                                                                                                                                                                                                                                                                                 IF (M.Eg.-1) GO TO 470
          P(IU, 1) = (MXLON*60-JI)
                                                                                                                                                                         IF (J.EQ.1) GO TO 430
                                                                                                                                                                                                                                                                                                                                                                       DO 480 J=1,3
EP(IU,J)=TP(IU,J)
EP(IU,J+3)=TP(IU,J)
                                                                                                                                                                                                                                                                                                                                                                                                      EP(IU, J+6)=TP(IU, J)
                                                                                                                                                                                                                                                                                                                                                                                                                 EP(IU, J+9)=TP(IU, J)
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SON
                                                                                                                                                                                    CT(J)=CT(J)+CT(J-1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DO 530 J=1,NITCOL
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CALL CLOCKS(T1)
                                                                                                                                                                CT(J)=3600.*CT(J)
                                                                                                                                                                                                                                                                                     VV1(IP-1,4)=-5.0
                                                                                                                                                                                                                                 VV1(IP,3)=CT(J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                DO 530 I=1.NU
                                                                                                                                                                                                                      VV1 (IP,4)=IP+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                              520 K=1,7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          NCYC=NCYC+1
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                                                                                                                                           DO 450 J=1+3
                                                                                                                               VV(IU,4)=IP
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                                                                                                                                                                                                                                                                   CONTINUE
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                                                                                                    390 CALL
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GET THE LOCATEE'S HEIGHT.

IF (NIYPE(IU).LT.3) CALL HEIGHT(X,Y,TP(IU,1),TP(IU,2),TP(IU,3),M)
                                                                                                                                                                                                                                                                                                                                                                 PROCEDURE IS THE
                                                                                                                                                                                                                                                                                                                                                                            SAME HERE AS FOR THE LOCATEE, BUT NO HEIGHT RETRIEVAL AND
                       DETERMINE THE LOCATEE'S NEW POSITION BY INCREMENTING THE OLD POSITION WITH VV. DO NOT MOVE A FIXED UNIT.
                                                                                                                                                                                                                   IF LOCATEE IS BEYOND THE BOUNDARY, CHANGE HIS DIRECTION.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            GO TO 2010
HEIGHT FOR NON-FIXED UNITS, AND STORE IN EP.
                                                                       A NEW ONE FROM VVI.
                                                                                                                                                                                                                                                                                                                                                                DETERMINE ALL OTHER UNITS' NEW POSITIONS.
                                                                                                                                                                                                                             (TP(IU+1).LT.BND) GO TO 1110
(VV(IU+1).GT.0.0) VV(IU+1)=-VV(IU+1)
                                                                                                                                                                                                                                                                                                       VV(IU,2)=-VV(IU,2)
                                                                                                                                                                                                                                                                                                                                         (VV(IU,2).LT.0.0) VV(IU,2)=-VV(IU,2)
                                                                                                                                                                                                                                                                               VV(IU+1)=-VV(IU+1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  WAIT FOR END OF HEIGHT RETRIEVAL.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          COMPUTE RANGES FOR THIS SUBCYCLE.
                                                                       GET
                                                                                                                                                                                                                                                                                          60 TO 1130
                                                                                                                                                                                                                                                                   60 TO 1120
                                                                                                                                                                                                                                                                                                                              (TP(IU,2),6T,0,0) G0 T0 1140
                                                          (VV(IU.3).6T.CLK) GO TO 1020
                                                                                              IF (VV(IU,4).LT.0.0) GO TO 1200
                                                                                                                                                                                                                                                                                                                                                                                                                                      IF (VV(I+3).GT.CLK) GO TO 1260
IF (VV(I+4).LT.0.0) GO TO 1290
                                                                      CURRENT VV IS OUTDATED.
                                                                                                                                                                                TP(IU,2)=TP(IU,2)+VV(IU,2)
                                                                                                                                                                                                                                                                                                                                                                                       BOUNDARY CHECKING.
                                                                                                                                                                     TP(IU,1)=TP(IU,1)+VV(IU,1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            IF (FXD(IU)) 60 TO 4900
                                                (FXD(IU)) GO TO 1200
                                                                                                                                                                                                                                                                                                                                                                                                                            (I.E0.IU) GO TO 1290
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 TP(I,1)=TP(I,1)+VV(I,1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              P(I,2)=TP(I,2)+VV(I,2)
                                                                                                                                                                                                                                                                                                       (VV(IU/2).6T.0.0)
                                                                                                                                                                                                                                                                   (TP(IU+1).GT.0.0)
(VV(IU+1).LT.0.0)
                                                                                                                                                                                                                                                                                          IF (TP(IU.2),LT,BND)
                                                                                    F AVAILABLE.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 IF (FXD(IU)) X=0.0
                                                                                                                                                        VV(IU, U)=VV1(K1, U)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     VV(I+1)=VV1(K1+1)
                                                                                                                                                                                                                                                                                                                                                                                                      I=I NO
                                                                                                                                 K1=VV(IU+4)+.5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       DO 2100 J=1,NU
            SQN8+CN8=QN8
                                                                                                                                             DO 1010 J=1+4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           00 1230 J=1,4
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              X=X+TP(IU+3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CALL HRG(X)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 EP(IU,12)=X
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         EP(IU,6)=X
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    EP(IU,9)=X
IU=KUF(I9)
                                                                                                                       (=TP(IU,2)
                                                                                                           X=TP(IU:1)
                                                                                                                                                                                                                                                                                                                                                     1140 CONTINUE
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IF THE TIME IS NIGH, COMPLETE THE OVERLAYING OF THE CURRENT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               INTERVISIBILITY MATRIX, AND ARRANGE FOR FUTURE USE OF THE
IF LOCATOR CANDIDATE IS NOT A REPORTER, SKIP THAT RANGE
                                                                                                                                    RANGE(IR) = SORT((TP(J.1)-TP(IU.1)) **2+(TP(J.2)-TP(IU.2)) **2
                                                  RETRIEVE INTERVISIBILITY FOR LOCATEE-LOCATOR PAIR.
                                                                                                                                                                                                                                                                            ACCUMULATE ERROR STATISTICS ON THE LOCATEE.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      * * * END OF THE PROCESSING FOR A CYCLE.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           NEXT INTERVISIBILITY MATRIX IN SEQUENCE.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       (CLK.LT.FLOAT(1200*(IVMAT-1))) GO TO 5040
                                                                          IV=FLD(J-J1*36.1,IT(IU.J1+1))
IF NO LOS, SKIP RANGE CALCULATION.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          UPDATE THE INTERVISIBILITY TABLE.
                                                                                                                                                                                                                           GO ATTEMPT TO LOCATE THE LOCATEE.
                                                                                                                                                                                                                                                                                                                                                                                                   IF (STATI(IU,5)-ERR) 4010,4020,4020
                                                                                                                                                                                                                                                                                                                                                                                                                                                               IF (STAT1(IU,8),6E.ERR) GO TO 4040
                                                                                                                          COMPUTE RANGE AND PERTURB IT
                                                                                                                                                  +(TP(J,3)-TP(IU,3))**2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                     STAT1(IU.10)=STAT1(IU.10)+ERR
                                                                                                                                                                                                                                                                                                                                       ERR=SQRT (DX (IU) **2+DY (IU) **2)
                                                                                                                                                                                                                                                                                                                                                    STATI(IU,4)=STATI(IU,4)+ERR
                                                                                                                                                                                                                                                                                                                                                               STAT2(IU.1)=STAT2(IU.1)+1.0
                                                                                                                                                                                                                                                                                                                                                                           STAT2(111,2)=STAT2(111,2)+1.0
                           (.NOT.RPT(J)) GO TO 2100
                                                                                                                                                                                                                                                                                                                            DZ(IU) = EP(IU,6) - TP(IU,3)
                                                                                                                                                                                                                                                                                                     DX(IU) = EP(IU,4) - TP(IU,1)
                                                                                                                                                                                                                                                                                                                DY (IU) = EP (IU, 5) - TP (IU, 2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     (ITIND(I)) GO TO 5020
                                       (J.E0.IU) GO TO 2100
                                                                                                 IF (IV.EQ.0) GO TO 2100
                                                                                                                                                                                                                                                                                         IF (.NOT.S(IU)) GO TO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              IT(I,U)=ITB(I,U,IVMAT)
                                                                                                                                                                           RANGE (IR) = RANGE (IR) +X
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             AVASBT=AVASBT+T4-T3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 AVSUBT=AVSUBT+T2-T1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  DO 5010 J=1,NITCOL
             CALCULATION.
                                                                                                                                                                                                               RANGE (IR+1) =-5.0
                                                                                                                                                                                                                                                                                                                                                                                                                            STATI(IU,6)=NCYC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         STAT1(IU,9)=NCYC
                                                                                                                                                                                                                                                                                                                                                                                         AVKTR=AVKTR+1.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ITIND(I)=.FALSE.
                                                                                                                                                                                                                                                                                                                                                                                                                STAT1(IU,5)=ERR
                                                                                                                                                                                                                                                                 CLOCKS(T4)
                                                                                                                                                                                                                                                                                                                                                                                                                                         ERR=ABS(D2(IU))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             STATI(IU,8)=ERR
                                                                                                                                                                                                                                        CLOCKS (T3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CALL CLOCKS(T2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           5020 I=1,NU
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     IVMAT=IVMAT+1
                                                                                                                                                                                       LOCATR(IR)=J
                                                               J1=(J-1)/36
                                                                                                                                                                                                                                                    FINDIT
                                                                                                                                                               CALL RG(X)
                                                                                                                                                                                                    CONTINCE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               4900 CONTINUE
                                                                                                                2035 IR=IR+1
                                                                                                                                                                                                                                          CALL
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UPDATE THE CURRENT INTERVISIBILITY MATRIX BY RANDOMLY
                                                                                                                                                                                                                                                                                                                                                                  OF THE OUTPUT TABLE,
                            FINDING K3C ROWS THAT HAVE NOT BEEN CHANGED AND
                                                                                                                                                                                                                                                                                                                                                                                                                                                     OF TABLE.
                                                                                                                                                                  PRINT INTERMEDIATE ERROR OUTPUT.
                                                                                                                                                                                                                                                                                                                                                                                                                                                      ACCUMULATE STATISTICS FOR LAST LINE
                                                                                                                                                                                                                                                                                                                                                                                                                       IF (STAT1(1,2),6E,STAT1(1,5)) GO TO 5220
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          IF (STAT1(1,5),61,STAT1(16P,5)) 16P=1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                IF (STAT1(1,2),6T.STAT1(16T,2)) 16T=1
                                                                                                                                                                                                                                                                                                                          WRITE(6,20) NCYC,CLK,AVSUBT,AVASBT
WRITE(6,16) NCYC,KICC
                                                                                                                                                                                                                                                                                                                                                                   PREPARE AND PRODUCE THE BODY
                                                                                                                                                                                                                                                                                                                                                                                                              STAT1 (I+7) = STAT1 (I+7) + STAT1 (I+10)
                                                                                                                                                                                                                                                                                                                                                          (TPOUT) WRITE(9) NCYC, CLK, KICC
                                                                                                                                                                                                                                                                                                                                                                                                    STAT1(I,1)=STAT1(I,1)+STAT1(I,4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       IF (STAT1(1,8),6T,STAT1(IZT,8))
                                                                                                                                                                             IF (NCYC.EQ.MAXCYC) 60 TO 5210.
IF (KICC.LT.KIC) 60 TO 5500
                                                                                   IF (.NOT.ITIND(12)) GO TO 5060
[F (K2CC.LT.K2C) GO TO 5200
                                                                                                                                                                                                                                                                                                                                                                                ONE LINE AT A TIME.
                                                                                                        F (I2.6T.NU) I2=I2-NU
F (I2.NE.I1) 60 TO 5050
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ZPSUM=ZPSUM+STAT1(I·10)
                                                                                                                                                IT(I2, J) = ITB(I2, J, IVMAT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          GTKTR=GTKTR+STAT2(I.1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ZTSUM=ZTSUM+STAT1(I+7)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     GPKTR=GPKTR+STAT2(I+2)
                                                               II=FLOAT (NU) *RU (KZ)+1.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  GTSUM=GTSUM+STAT1(I+1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           GPSUM=GPSUM+STAT1(I+4)
                                                                                                                                                                                                                                                                                                                                                                                                                                   STAT1(I+2)=STAT1(I+5)
                                                                                                                                                                                                                                                                                                                                                                                                                                             STAT1(1,3)=STAT1(1,6)
                                                                                                                                                                                                                                                                                                                    WRITE HEADINGS.
                                                                                                                                                                                                                                                                                                         AVASBT=AVASBT/AVKTR
                                                                                                                                                                                                                                                                                               AVSUBT=AVSUBT/AVKTR
                                            CHANGING THEM.
                                                                                                                                       DO 5070 J=1,NITCOL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         J2=STAT1(I+6)+.5
J3=STAT1(I+9)+.5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                J1=STAT1(I+3)++5
                                                                                                                                                                       PREPARE AND
                                                                                                                                                           ITIND(I2)=.TRUE.
                                                                                                                                                                                                                                                                                                                                                                                            DO 5250 I=1,NU
                                                      DO 5090 I=1,K3C
                                                                                                                                                                                                                                                                                                                                                 WRITE(6,17)
IF (TPOUT)
                                                                                                                              TO 5200
                                                                                                                                                                                                                         GTKTR=0.0
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                                                                                                                                                                                                                                              ZTSUM=0.0
                                                                                                                                                                                                                                                        2PSUM=0.0
                                                                                                                                                                                                     GTSUM=0.0
                                                                                                                                                                                                                GPSUM=0.0
                                                                                                 12=12+1
              K2CC=0
                                                                                                                                                                                                                                                                     IGT=1
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                                                                              2=I1
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I,X,Z1,STAT1(I,2),J1,STAT1(I,8),J3,Y,Z2,STAT1(I,5),J2,
                                                                                                                                                                                                                                                                                                                                                                                           IF (TPOUT) WRITE(9) X,21,STAT1(IGT,2),J1,STAT1(IZT,8),J3,Y,Z2,
                                                                                                              STAT1(I,5), J2, DX(I), DY(I), DZ(I), S(I), RPT(I), FXD(I)
                                                                                                     WRITF(9) I, X, Z1, STAT1(I, 2), J1, STAT1(I, 8), J3, Y, Z2,
                                                                                                                                                                                                                                                                                                                                                                                 WRITE(6,2) X,Z1,STAT1(IGT,2),J1,STAT1(IZT,8),J3,Y,Z2
                                                                                           DX(I),DY(I),DZ(I),S(I),RPT(I),FXD(I),W(I)
                                                             F (STAT2(I+2).6T.0.0) Z2=STAT1(I+10)/STAT2(I+2)
                                                                                                                                                                                                                                                                                                PREPARE AND PRODUCE LAST LINE OF THE TABLE.
                                        F (STAT2(I+1).GT.0.0) Z1=STAT1(I+7)/STAT2(I+1)
                    F (STAT2(1,2),6T.0.0) Y=STAT1(1,4)/STAT2(1,2)
                                                                                                                                                                                                                                                                                                                                                                                                                                              REINITIALIZE STATISTICS ACCUMULATORS
                                                                       WRITE OUT A LINE OF THE TABLE.
                                                                                                                                    ACCUMULATE QUADRANT COUNTS.
                                                                                                                          W(I), (TP(I, J), J=1,3)
                                                                                                                                                                                                                                                                                                                                                                                                                                    WRITE(6,14) IQ2, IQ1, IQ0, IQ3, IQ4
                                                                                                                                                                                                                                                                                                                                                                                                                           PRODUCE QUADRANT COUNTS.
                                                                                                                                                                                                                                                                                                                                                                                                              STAT1 (16P+5) + J2
                                                                                                                                                                  5242,5238,5239
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                                                                                                                                                5235,5236,5237
                                                                                                                                                          5241,5240,5240
                                                                                                                                                                                                                                                                                                                                                             J2=STAT1 (IGP,6)+.5
                                                                                                                                                                                                                                                                                                                                                                      3=STAT1 (IZT, 9)+.5
                                                                                                                                                                                                                                                                                                                                                  J1=STAT1 (16T+3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   I,10)=0.0
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                                                                                                                                                                                                                                                                                                                                       Z2=ZPSUM/GPKTR
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                                                                                                                                                                                                                                                                                                          X=6TSUM/GTKTR
                                                                                                                                                                                                                                                                                                                     Y=GPSUM/GPKTR
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                                                                                   WRITE(6,1)
                                                                                                       IF (TPOUT)
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F (STAT2)
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                                                                                                                                                                                                                                                          IQ3=IQ3+1
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                                                                                                                                                                                          IQ0=IQ0+1
                                                                                                                                                                                                                IQ1=IQ1+1
                                                                                                                                                                                                                                     192=192+1
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                                21=0.0
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STARTING Z'6X'A
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            AVERAGE ALGORITHM SUBCYCLE TIME =+F
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CYC * 4X * XY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                AVERAGE SIMULAT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             * COUNTER ='197' IV UPDATE COUNTER ='197' ROWS IN IV UPDATE ='197
** XY PLOT COUNTER ='197
** MAX NUMBER RANGES ='197' NUM. STAT. UNITS ='197' SIMULATION T
*IME ='F9.27' MAX NUMBER CYCLES ='197' SUBCYCLE DELTA T ='F9.47' A
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  12 FORMAT(15,16,6E14,8)
13 FORMAT(' NUMBER OF UNITS ='19/' OUTPUT
                                                                                                                                                                                                                                                                                            FORMAT(1X14, 3E10.5, I4, E10.5, I4, 2X, 3E10.5, I4, 2X3E9.3, L2, 2L1, E10.5)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  *RIES = "F9.4/" BOUNDARY SPEED = "F9.2)
14 FORMAT (/53x'QUADRANT COUNTS OF ERRORS'//60XI3,5XI3/64XI3/60XI3.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      SRF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    TIME MOVING = 1F9.2/1 AVG TIME STOPPED = 1F9.2/1 UPPER
                                                                                                                                                                                              CALL GRAPH(NU.TP(1.1),TP(1.2),TRUE",XMAX,XMIN,YMAX,YMIN)
                                                                                                                                                                                                           GRAPH(NU, EP(1,7), EP(1,8), 'EST.', XMAX, XMIN, YMAX, YMIN)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CYC'5X'EX-TX'4X'EY-TY'4X'EZ-TZ
                                                                                                                                                                                                                                                                                 FORMAT STATEMENTS AND INTERNAL SUBPROGRAMS FOLLOW.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        Z MAX
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                                                                                                                                                                                                                                                                                                                                                                                                                                        STARTING Y
                                                                                                                                                                                                                                                                                                            FORMAT(/* ALL'3E10.5,I4,E10.5,I4,2X3E10.5,I4)
                                                                                                                                                                                                                                                                                                                                                                                                            FORMAT(/' INITIAL STATIONARY UNITS ARE:')
FORMAT(/' ASSIGNMENT OF UNITS TO SLOTS IS:')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      17 FORMAT(" UNIT XY AVG'5X'Z AVG'4X'XY MAX
                                                                                                                                                                                                                                                                                                                                                                                  FORMAT(/ INITIAL REPORTING UNITS ARE: ")
                                                                                                                                                       PRODUCE THE INTERMEDIATE XY PLOTS.
           UPDATE THE STATIONARY UNIT LIST
                                          AIRCRAFT CANNOT BE STATIONARY.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         FORMAT(13,18X2(13,212),3(1X3F4.0))
                                                                                                                                                                                                                                                                                                                                                                                                                                        STARTING X
                                                                                              IF (RU(KZ).6T.PSS(J)) GO TO 5550
FXD(I)=.NOT.FXD(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                    *ZIMUTH'8X'SPEED'6X'CHANGE TIME')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                18 FORMAT(/' THE UNIT TYPES ARE: ')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             20 FORMAT(/// CYCLE NUMBER'IS''.
                                                                                                                                                                                                                            IF (NCYC.EQ.MAXCYC) GO TO 9000
GO TO 1000
IF (NCYC.EQ.MAXCYC) GO TO 5610
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            *ION SUBCYCLE TIME = FF7.4 . S.
                                                        [F (NTYPE(I).GT.2) GO TO 5550
                                                                                                                                                                   IF (K4CC.LT.K4C) GO TO 1000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   KZ=KZ-(KZ/4194304)*4194304
                                                                                                                                                                                                                                                                                                                          FORMAT(615,5F10,5/6F10,5)
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                                                                                                                                                                                                                                                                                                                                                                                                                                       11 FORMAT(/ UNIT TYPE
                                                                                                                                                                                                                                                      IF (TPOUT) ENDFILE 9
                                                                                                                                                                                                                                                                                                                                                      FORMAT (IS, F5.0, IS)
                                                                                                                                                                                                                                                                                                                                                                  FORMAT (53X3E14.8)
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                          DO 5550 I=1,NU
                                                                                    [F(FXD(I)) J=2
                                                                                                                                                                                                                                                                                                                                                                                               FORMAT (2615)
                                                                                                                                                                                                                                                                                                                                         FORMAT (2014)
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RU=RU*2.3841858E-7 RETURN END 436* 437* 438* 01410 01411 01412

END OF UNIVAC 1108 FORTRAN V COMPILATION.

1 TIME = 1 SEC.
2 TIME = 0 SEC.
3 TIME = 2 SEC.
4 TIME = 1 SEC.
5 TIME = 1 SEC.
6 TIME = 1 SEC.

0 *DIAGNOSTIC* MESSAGE(S)

PHASE PHASE PHASE PHASE PHASE

5 SEC TOTAL COMPILATION TIME =



DIT FOR HEIGHT, HEIGHT UNIVAC 1108 FORTRAN V LEVEL 2206 0018 F5018P THIS COMPILATION WAS DONE ON 01 JUN 72 AT 10:55:48

ENTRY POINT 000270 SUBROUTINE HEIGHT

STORAGE USED (BLOCK, NAME, LENGTH)

EXTERNAL REFERENCES (BLOCK, NAME)

NTRAN NWDUS NIOSS NSTOPS NERRSS 0003 0004 0005 0005 0006

	110L	CN	ΙÞΥ	MXLON	
	000161	000000	00000	00000	
	000	2000	I 0000	, 2000	
NAME)	105L	×ZU	IPX	ANLAT	•
LOCATION			000000		
RELATIVE LO	0001	0002 R	I 0000	0000 I	
IYPE	100L	200L	IFY	11	
(BLOCK)			000003		
VARIABLES	0001	0001	I 0000 .	I 0000	
- 7 J			ΥLI		>0
ASSIGNMENI FOR	000011	000167	000000	000000	40000
SIOKAGE	0000	0001	I 0000	I 0000	1 6000

000004 I 000006 I 000000 I 000000 I

00001 0000 I 0000 I

SUBROUTINE HEIGHT(PX,PY,FX,FY,FZ,M) PARAMETER L6=5,L7=11 COMMON WNLAT,MXLON,CNY,NDX(L6,L7) DATA CNX,CNY,0145515310,0107798475/	CONVERT FROW POSITION IN METERS TO POSITION IN TERMS OF THREE SECONDS OF LATITUDE AND LONGITUDE. IPX=PX*CNX+.5	IPY=PY*CNY+•5 IFX=FX*CNX+•5 IFX=FX*CNX+•5	IF (IPX.NE.IFX) GO TO 100 IF (IPY.NE.IFY) GO TO 100 IF FUTURE POSITION IS ON SAME TERRAIN PLATFORM AS PRESENT POSITION, FEED BACK SAME HEIGHT.	M=1 RETURN COMPUTE THE SUBSCRIPTS FOR THE REQUIRED TERRAIN BLOCK. 100 I=IFY/120+1	J=IFX/120+1 IF (NDX(I,J).6E.0) GO TO 200 IF THAT TERRAIN BLOCK DOES NOT EXIST, UNIT MAY BE ON A BOUNDARY BETWEEN TWO OR FOUR BLOCKS. CHECK EXISTENCE OF
SUE PAR	i d	G H H	H H	Σ. Μ. Η	⊃ ₩ II II'
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00101 00103 00104 00105	00105	00111 00112 00113	00114 00116 00116 00116	00120 00121 00121 00122	00124 00124 00124 00124



```
FORMAT(/' NO HEIGHT FOR'ZE14.8' NEED BLOCK'215' REDUCED COORDINA *TES ARE: 215)
                                                                                                                                                                 COMPUTE SUBSCRIPTS FOR LOCATION OF HEIGHT WITHIN THE BLOCK I1=IFY-120*(I-1)+1
                                                                                                                                                                                                          H
                                                                                                                                                                                                         READ
                                                                                                                                                                                                                                               0 *DIAGNOSTIC* MESSAGE(S)
                                                                                                                                                                                    REWIND THE DRUM, POSITION TO REQUIRED HEIGHT, AND RETURN
RETURN
END
                                                                                                                           CHECK VALIDITY OF TERRAIN BLOCK SUBSCRIPTS.
                               IF (NDX(II,JI),GE,0) GO TO 120
IF (NDX(II,JI),GE,0) GO TO 130
WRITE(6,1) FX,FY,I,J,IFX,IFY
                 GO TO 110
                                                                                                                                                                                                                                              FORTRAN V COMPILATION.
                                                                                                                                  (I.GT.L6) GO TO 105
                                                                                                                                                  (J.6T.L7) GO TO 105
                                                                                                                                          (I.LT.1) GO TO 105
                                                                                                                                                          (J.LT.1) GO TO 105
               IF (NDX(I1,J),GE.0)
THOSE BLOCKS.
                                                                                                                                                                                   U1=IFX-120*(U-1)+1
         [1=(IFY-1)/120+1
                        J1=(IFX-1)/120+1
                                                                            I=I1
G0 T0 200
                                                                                                    60 TO 200
                                                                                                                                                                                                                                              UNIVAC 1108
                                                                                                            I=11
                                                                                            J=J1
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PNO
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PHASE
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                      00131
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TOTAL COMPILATION TIME = 1 SEC



ENTRY POINT 000072 SUBROUTINE HRG

STORAGE USED (BLOCK, NAME, LENGTH)

EXTERNAL REFERENCES (BLOCK, NAME)

HRGU ALOG SORT COS NERR3\$ 00003 00004 00005 00005 STORAGE ASSIGNMENT FOR VARIÁBLES (BLOCK, TYPE, RELATIVE LOCATION, NAME)

0000 ALOG PI R 000000

<u>α</u> α

0000005

0000 R 000006 A2 0000 R 000004

> DATA PI/3.14159265358979/ TO 50 U2=SQRT(A1S-U1**2) IF (A2.6T.PI) U2=-U2 IF (IFLAG.6T.0) GO SUBROUTINE HRG(X) A15=-2.0*ALOG(U1) CALL HRGU(U1,U2) DATA IFLAG/0/ U1=A1*COS(A2) A2=2.0*PI*U2 A1=SORT(A1S) X=U1*14.0 IFLAG=1 RETURN 10* 11* 12* 13* 14* ** 00105 00111 00103 00113 00114 00115 00116 00117 00121 00122 00123 00100

0 *DIAGNOSTIC* MESSAGE(S) END OF UNIVAC 1108 FORTRAN V COMPILATION.

X=U2*14.0 IFLAG=0 RETURN

50

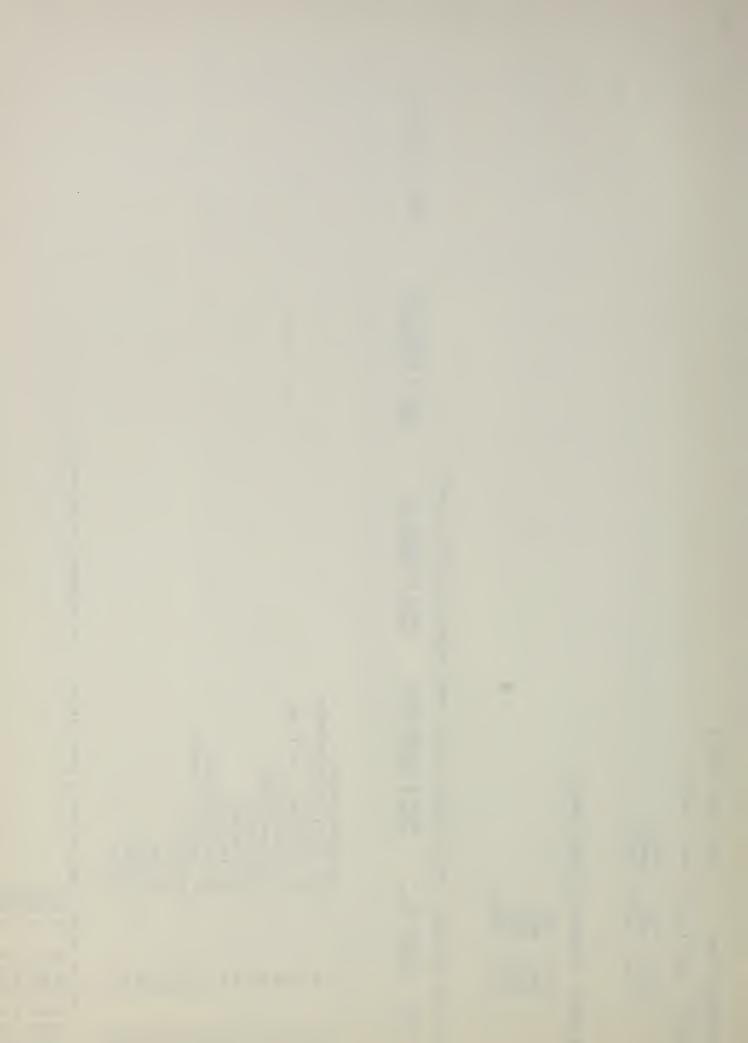
15* 16* 17* 18*

00124

00126

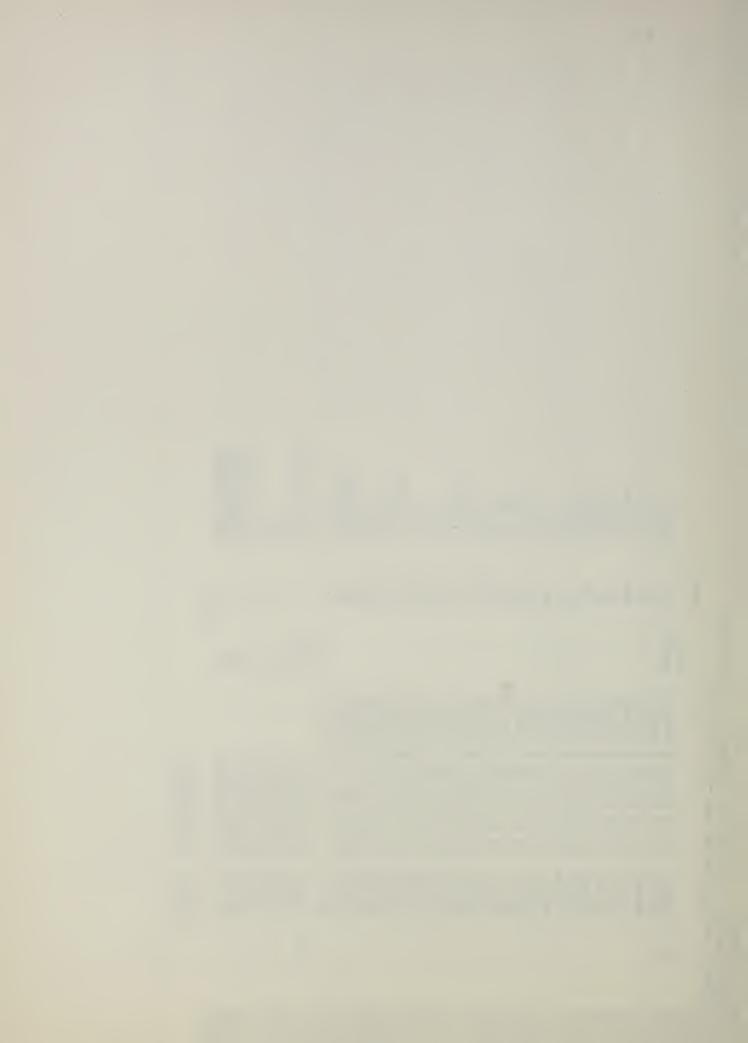
TIME TIME LIME PHASE PHASE PHASE PHASE

TIME



SEC TOTAL COMPILATION TIME = O SEC. PHASE 6 TIME =





000004 IB1 000003 U2



U2=U2*6 IF (IB1.6T.0) U1=U1+7 IF (IB2.6T.0) U2=U2+7	TE E	50 X=U2 IFLAG=0 RETURN END
25 * * * * 27 * * 27 * 4	3 2 3 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8
00140 00141 00143	00145 00146 00147	00150 00151 00152 00153

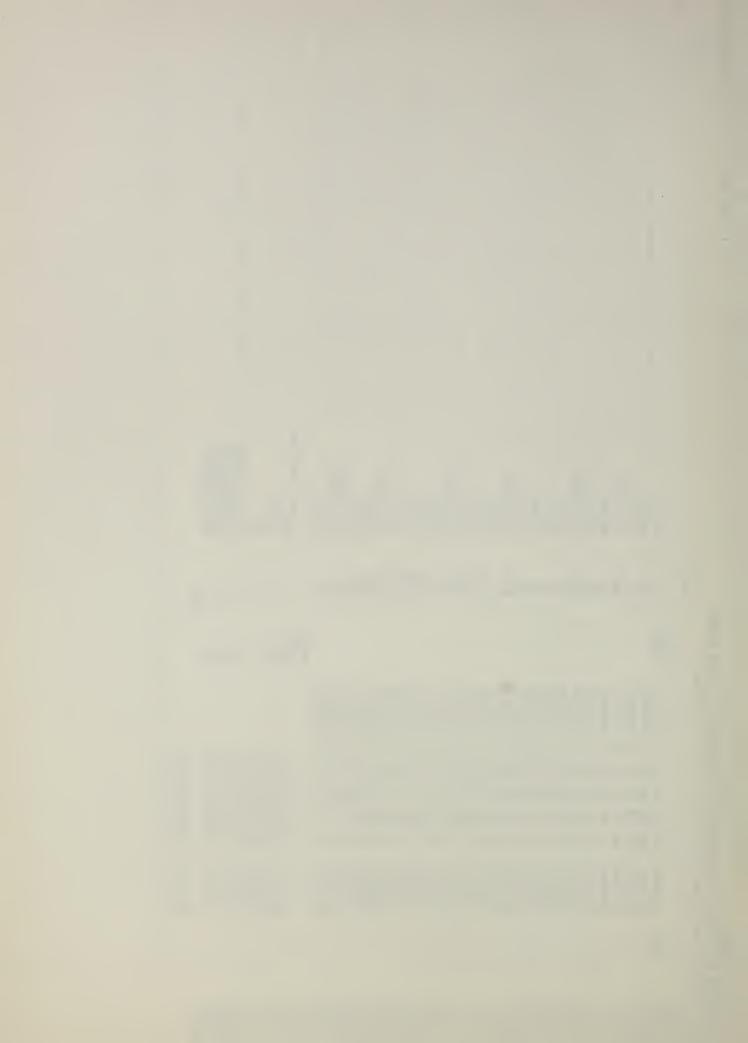
PHASE 1 TIME = 0 SEC.
PHASE 2 TIME = 0 SEC.
PHASE 3 TIME = 1 SEC.
PHASE 4 TIME = 0 SEC.
PHASE 4 TIME = 0 SEC.
PHASE 5 TIME = 0 SEC.

0 *DIAGNOSTIC* MESSAGE(S)

SEC TOTAL COMPILATION TIME =



10:55:52.594				and the second s		en en particular des estados en en en particular des estados en entre en entre				* The state of the		and the state of t					 Application of providing in the discrete was from an injury operation that are made in the company of the company						er er en	·	date, et visitis, sinnives tils in dann milling platfyrangeried, dag gruppmilde kantangenstateriedes	e de la compansión de l					18 **		
01 JUN 72				to the control to defend at these to the second of the sec		Windows Company Compan		enterferente de la companyación		THE STATE OF THE TOTAL PROPERTY AND THE		And the state of t		And the section is the section of th			e effective a destre a pro- description of the endings of the end				The section of the se		The second secon					manus en de la compania e compania de la compania del la compania de la compania de la compania de la compania del la compania	от постоя постоя в предоставления постоя в предоставления в постоя постоя постоя постоя постоя постоя постоя п То постоя посто		entraligio en el constitució en constitució en entraligio en entraligio en entraligio en entraligio de entraligio en en		
The second secon	Service commenter control anno destruction control control anno destruction control co	A0, I2	A0.K2	A0,K3-1) Al, MASK	ASTRO	ANTAN	AS MASK	AD. II	A0,K1	Δ1,(1)	A1. MASK	A2, I1			A1, (0200)		A1,9	A4,A4	SL A4+1	A3, (0200)	A A A A A	A2.*0.X11	A4,*1,X11	3,×11	7777777777	4604	129		27075473833	20867350019	18160161681	
2404 0008A	AXR	\$(1) RGU* LA	-	DA	AND	IW	PAG 4	AND	A	And the case of designation of the case of	AA	AND	SA.	CSC	rss	LA	ANA	JSC USC	Tech	LSS	LA	ANA	AS.	SA	7	MASK +	K1 +	K2 +	+	+ +	I1 I2	END	
EXEC II ASSEMBLER		00000 0 00 00 00 0	00000 0 00 00 00 0	1 10 00 00 0 00000	2 00 01 00 0 00000		1 10 02 00 0 00000	2 00 03 00 0 00000 1 00 04 00 0 00000	000000000000000000000000000000000000	00000 0 00 00 00 0	4 00 01 00 0 00000	2 00 01 00 0 00000	1 00 02 00 0 00000	3 06 02 00 0 00001	3 12 02 00 0 00000	0 00 01 00 0 00001	5 00 01 00 0 00001	3 03 01 00 0 00001	3 06 04 00 0 00002	3 12 04 00 0 00000	0 00 03 00 0 00001	73.03 03 00 0 000021	1 00 02 13 1 00000	1 00 04 13 1 00000	4 04 00 13 0 00000	777777777	0000001000	0000000000	000000000	1156457065	235562477003	£45045040	000000000001
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UNITED TO FORTHAIN V LEVEL ZEUS ONIB PSOIGH THIS COMPILATION WAS DONE ON 01 JUN 72 AT 10:55:54

SUBROUTINE GRAPH ENTRY POINT 000536

STORAGE USED (BLOCK, NAME, LENGTH)

EXTERNAL REFERENCES (BLOCK, NAME)

0003 NWDU\$ 0004 NIO1\$ 0005 NIO2\$ 0006 NERR2\$ STORAGE ASSIGNMENT FOR VARIABLES (BLOCK, TYPE, RELATIVE LOCATION, NAME)

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										7 LIMU			
000150	00021	00031	00075	00040	000047	00045	I nood	I 00041	I 00041	I 000367	3 000400	2 000372	
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55 100F	50 1526	51 2406	34 2746	17 3noL	21 350L	14 910L	53 BLANK	LO ITA	7 × 50	70 LIMA	53 SYM	IS XR	3 YP
							н	-	Н	I 000370	—	œ	œ
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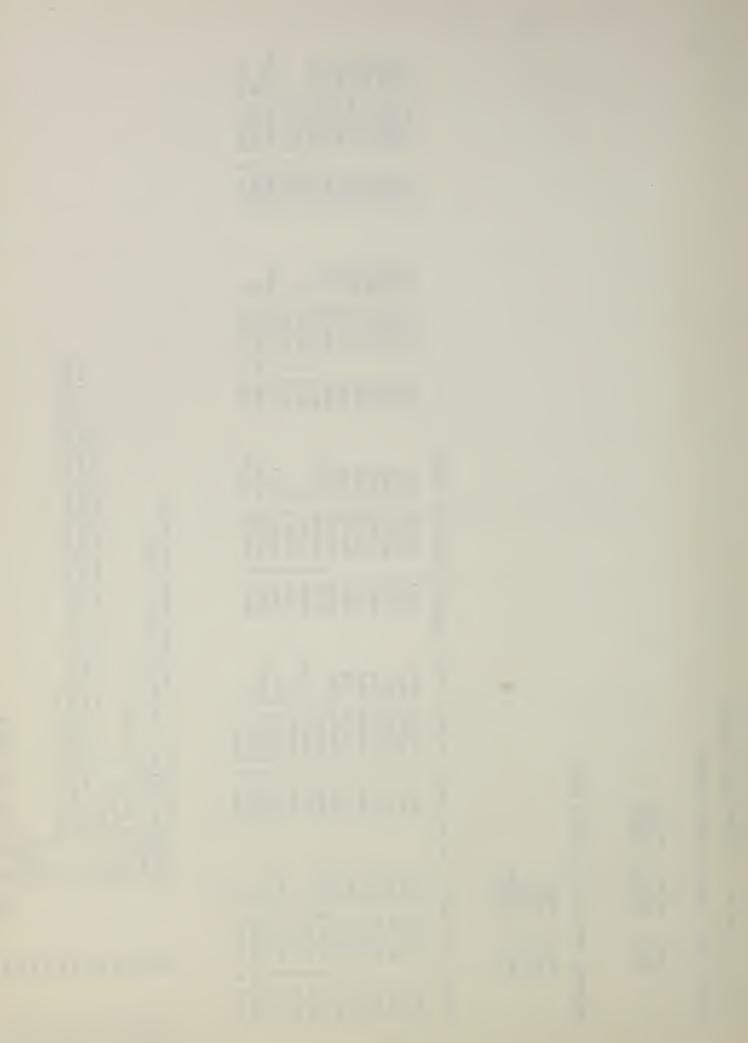
18F

TUO

345G

72L

DATA (NUMB(I), I=1,9)/141,142,143,144,145,146,147,148,149/ DATA (SYW(I), I=1,26)/14A,148,14C,140,14E,14F,14G,144,141,14J,14K, 1HL. 1HM. 1HN. 1HO. 1HP. 1HQ. 1HR. 1HS. 1HT. 1HU. 1HV. 1HW. 1HX. 1HY. 1HZ/ SUBROUTINE GRAPH(N.X.Y.IWRD.XMAX.XMIN.YMAX.YMIN) DIMENSION X(1), Y(1), PRINT(101), XP(6), SYM(26) DIMENSION NUMB(0), ITOTAL(101) = NUMBER OF PRINT TAPE INTEGER PRINT, BLANK, SYM 910 IF (LIMU.GT.N) LIMU=N DATA BLANK/1H LIMU=26 LIML=1 01 ပ 10* 11* 4 * * * * * * * * * 00103 00115 00105 00100 00110 00112 00112 00112 00114 00116 00117 00101



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250
260
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                                                                                                                                                                                                                                                             160
                                                                                                                                                                                                                                                                      170
                                                                                                                                                                                                                                                                                                                                              220
                                100
                                                                                                                                                                             918 FORMAT(* * * * NOTE.*I4, POINTS ARE OUTSIDE THE LIMITS OF THE GRA *PH AND HAVE BEEN OWITTED*)
                                                                                                                                                                                                                                      FORMAT (* ASSOCIATED SYMBOLS ARE 26(3X A1))
       FORMAT (*1.44. POSITIONS OF UNITS 2614)
                                                                                                                                                                                                                                                                                                                                                                                    IF (PRINT(KA)-9LANK) 240,230,240
                                                                                                                                                                        IF (IOUT.GT.0) WRITE(6,918) IOUT
                 WRITE(6,917) (SYW(I4), I4=1, LIMA)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        YL=YL-YDELTA
IF (IFLAG) 265,278,265
DO 275 LA=1,101
IF (ITOTAL(LA)-1) 268,275,268
                                                                                                                                             F (X(1)-XHIGH) 110,109,109
I WRD, (14, 14=L)
                                                                                                                          (Y(I)-YLOW) 109,109,102
                                                                                                                                   F (X(I)-XL) 109,103,103
                                                                                                                  F (Y(I)-YT) 101,101,109
                                                                                                                                                                                                                                                                                                                                                                            F(X(K)-XT) 220,250,250
                                                                                                                                                                                                                                                                                                                       [F(Y(K)-YT) 205,205,260
                                                                                                                                                                                                                                                                                                                                                                   F(X(K)-XL) 250,215,215
                                                                                                                                                                                                                                                                                                                               IF(Y(K)-YL) 260,260,210
                                                                                                                                                                                                                                                                                                                                                                                                                          ITOTAL(KA)=ITOTAL(KA)+1
                                           XDELTA=(XMAX-XMIN)/100.
                                                                                                                                                                                                                             100 FORMAT(14X+101H+-----
                                   YDELTA=(YMAX-YMIN)/50.
                                                                                        XHIGH=XMAX+XDELTA/2.
                                                     YL =YMAX-YDELTA/2.
                                                                      YLOW=YMIN-YDELTA/2.
                                                                                                                                                                                                                                                                                                              DO 260 K=LIML, LIMU
                                                                                                          DO 110 I=LIML, LIMU
                                                                                                                                                                                                                                                                                                                                                                                                       PRINT (KA) = SYW (ITA)
                                                                                                                                                                                                                                                                                                                                                                                              TA=K-(K-1)/26*26
                                                                                                                                                                                                                                                                                                                                                  XT=XMIN+XDELTA/2.
                                                               YT=YMAX+YDELTA/2.
                                                                                XL=XMIN-XDELTA/2.
                                                                                                                                                                                                                                                                                                                                                           DO 255 KA=1,101
                                                                                                                                                                                                                                                                           DO 200 K=1,101
                                                                                                                                                                                                                                                                  J=1,10
                                                                                                                                                                                                                                                                                            PRINT(K)=BLANK
                                                                                                                                                                                                                    WRITE(10,100)
                                                                                                                                                                                                                                                00 350 I=1+6
                                                                                                                                                                                                                                                                                                                                                                                                                                                               XT=XT+XDELTA
                                                                                                                                                                                                    WRITE(6,916)
                                                                                                                                                                                                              FORMAT( . .)
 (6,915)
                                                                                                                                                      109 IOUT=IOUT+1
                                                                                                                                                                                                                                                                                    ITOTAL (K) = 1
                                                                                                                                                                                                                                                                                                                                                                                                                                             60 TO 260
                                                                                                                                                                                                                                                                                                                                                                                                                 50 TO 260
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CONTINUE
                                                                                                                                                                 CONTINUE
                                                                                                                                                                                                                                                                  00 350
                                                                                                                                                                                                                                                                                                                                                                                                                                  IFLAG=1
                                                                                                                                                                                                                                                                                                                                        XL=XMIN
                                                                                                   COUT=0
                                                                                                                                                                                                                                                                                                                                                                                                                                                       XLIX
   WRITE
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260
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             00131
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FORMAT(1X,E12,4,1H+,101A1,1H+)
GO TO 350
                                                                                                                       FORMAT (13X,1H-,101A1,1H-)
                                                                                                                                         WRITE (10,290) YMIN'PRINT
                                                                                  WRITE (10,290) YP, PRINT
          IF (KK-9) 272,272,270
                                                                                                                                                                                                                            F (LIMU.EQ.N) RETURN
                                                                                                             WRITE (10,310) PRINT
                                                       IF(I-5) 285,285,400
                                                                                                                                                                                                                  FORMAT (6(7X, E13.5))
                            PRINT (LA) =NUMB (KK)
                                                                                                                                                                                                          WRITE (IO,420) XP
                                              60 TO (280,300),L
                                                                                                                                                                                                XP(I)=XP(I-1)+XR
                                                                        P=YT+YDELTA/2.
                                                                                                                                                   WRITE (10,100)
269 KK=ITOTAL(LA)
                                                                                                                                                                              (R=20.*XDELTA
                                                                                                                                                                                      DO 410 I=2,5
                                                                                                                                                                                                                                     IML=LIML+26
                                                                                                                                                                                                                                             LIMU=LIMU+26
                                                                                                                                                            XP(1)=XMIN
                                                                                                                                                                     (P(6)=XMAX
                                                                                                                                CONTINUE
                                     CONTINUE
                           272
273
273
280
285
                                                                                                             300
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                                                                                                                      310
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                                                                                                                                                                                                                   420
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350 370 380 390 400

420 430 440 460

410

0 *DIAGNOSTIC* MESSAGE(S) END OF UNIVAC 1108 FORTRAN V COMPILATION.

PHASE PHASE

PHASE PHASE PHASE

PHASE

TOTAL COMPILATION TIME =

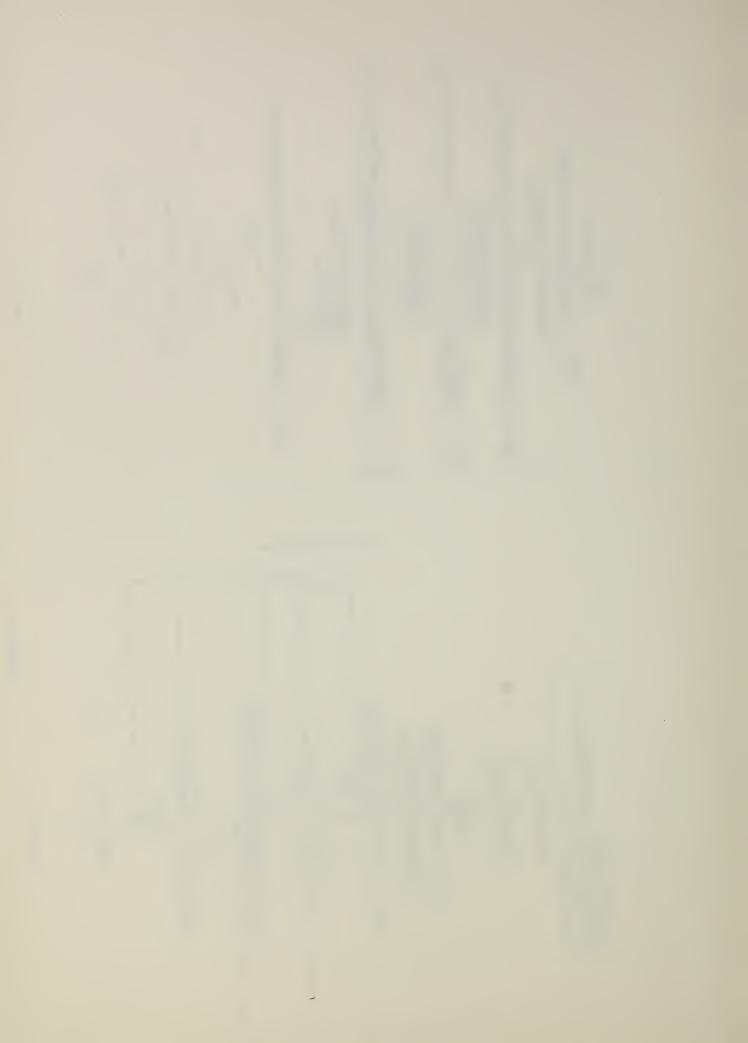
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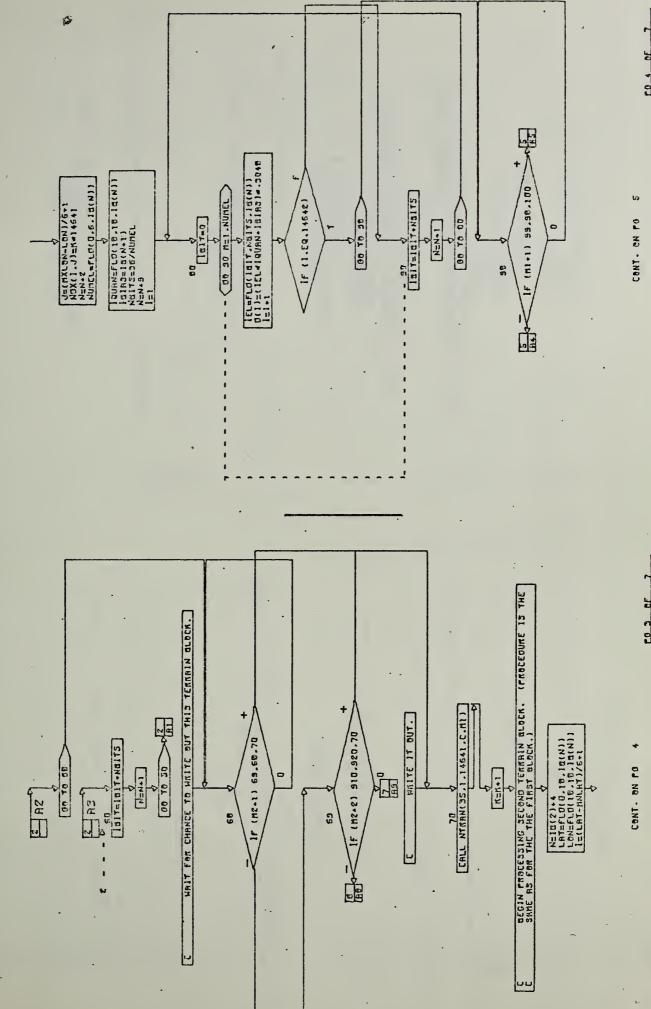
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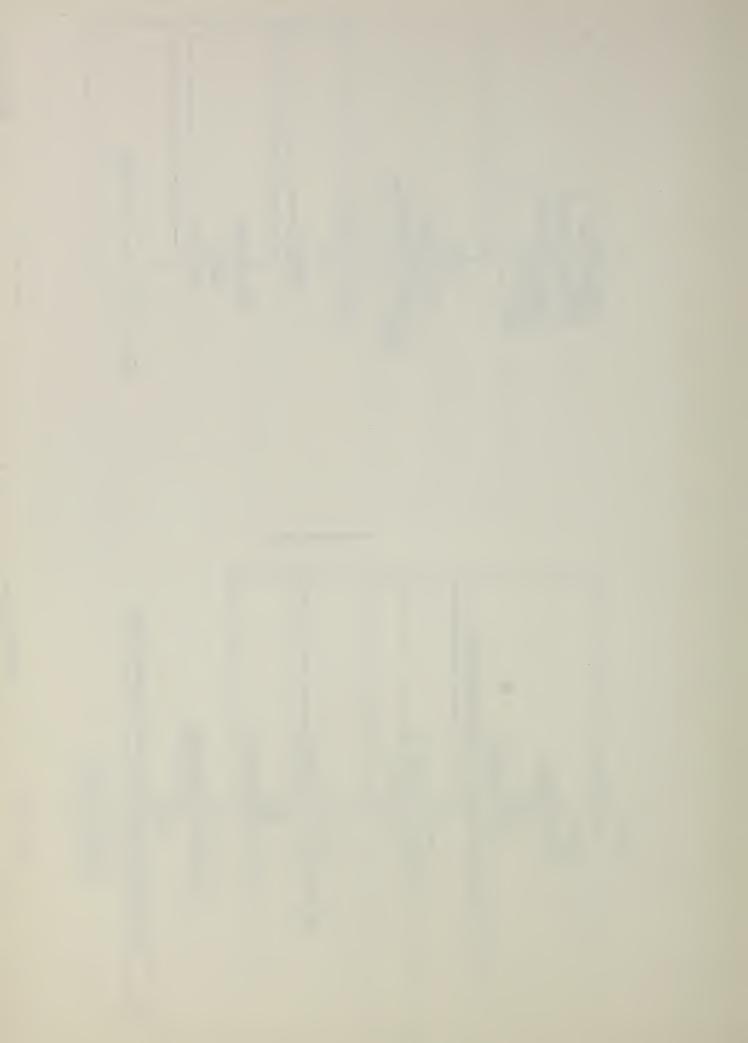


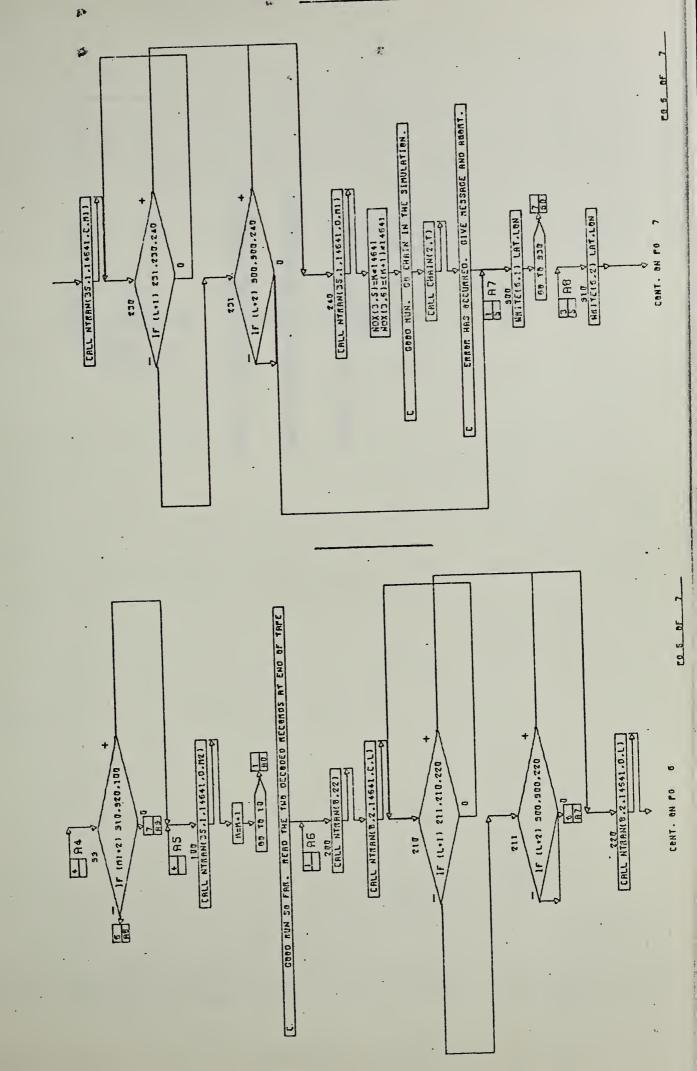
APPENDIX C: FLOWCHARTS OF THE MAIN SIMULATION PROGRAMS



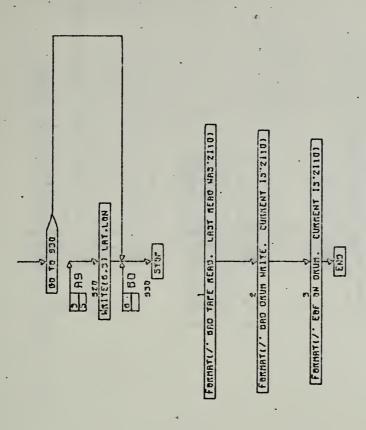


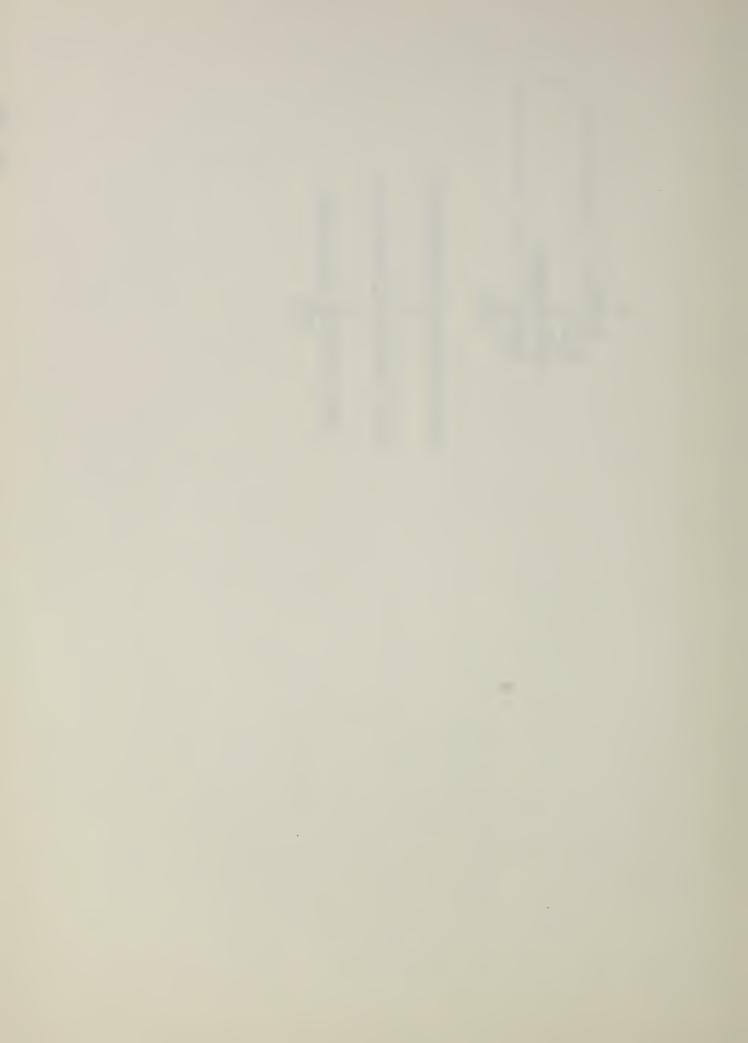


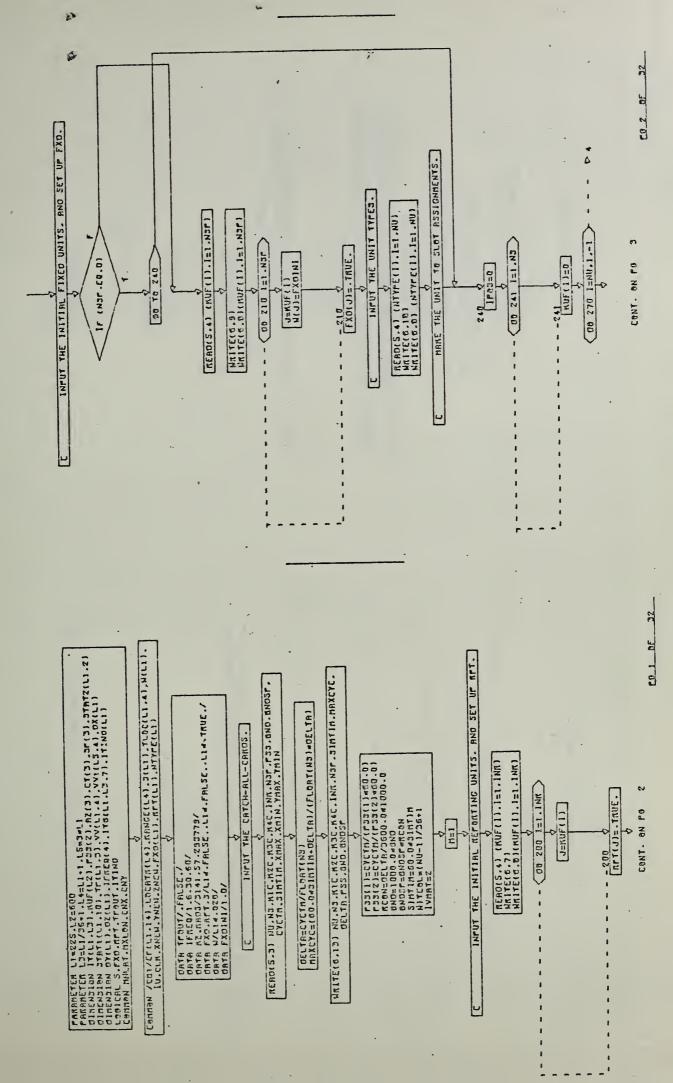


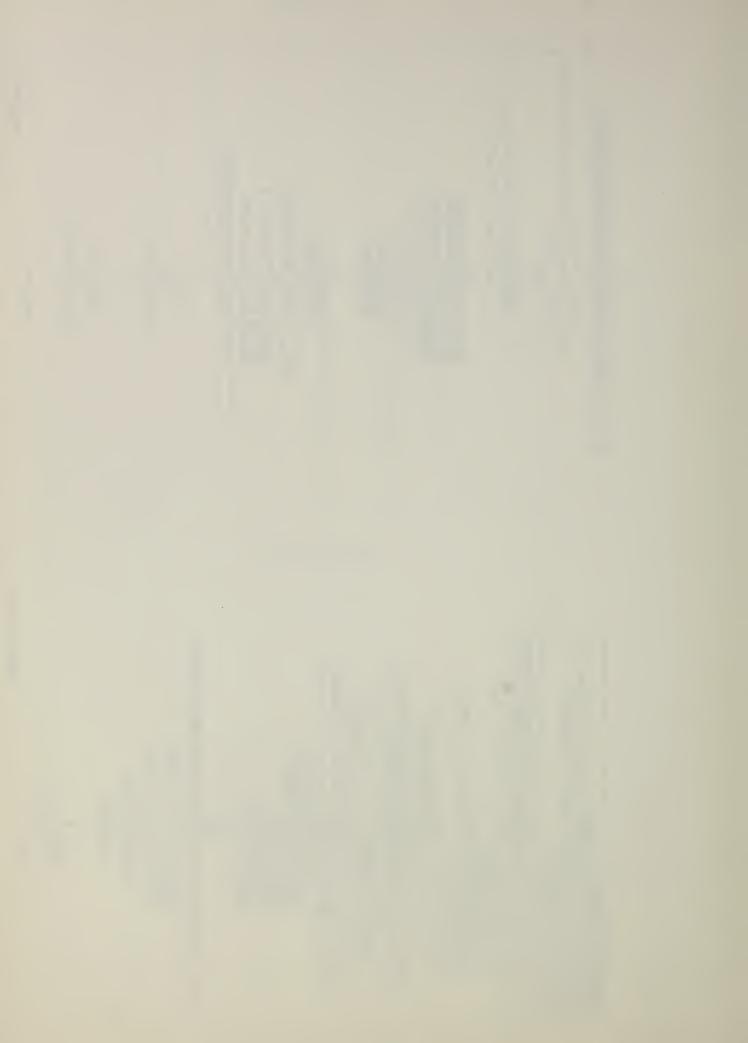


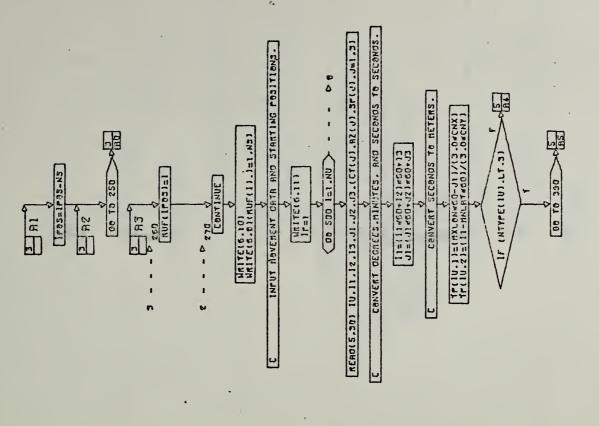


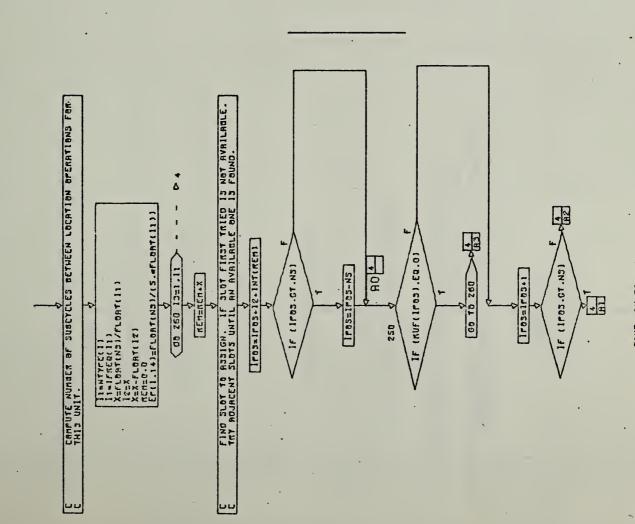


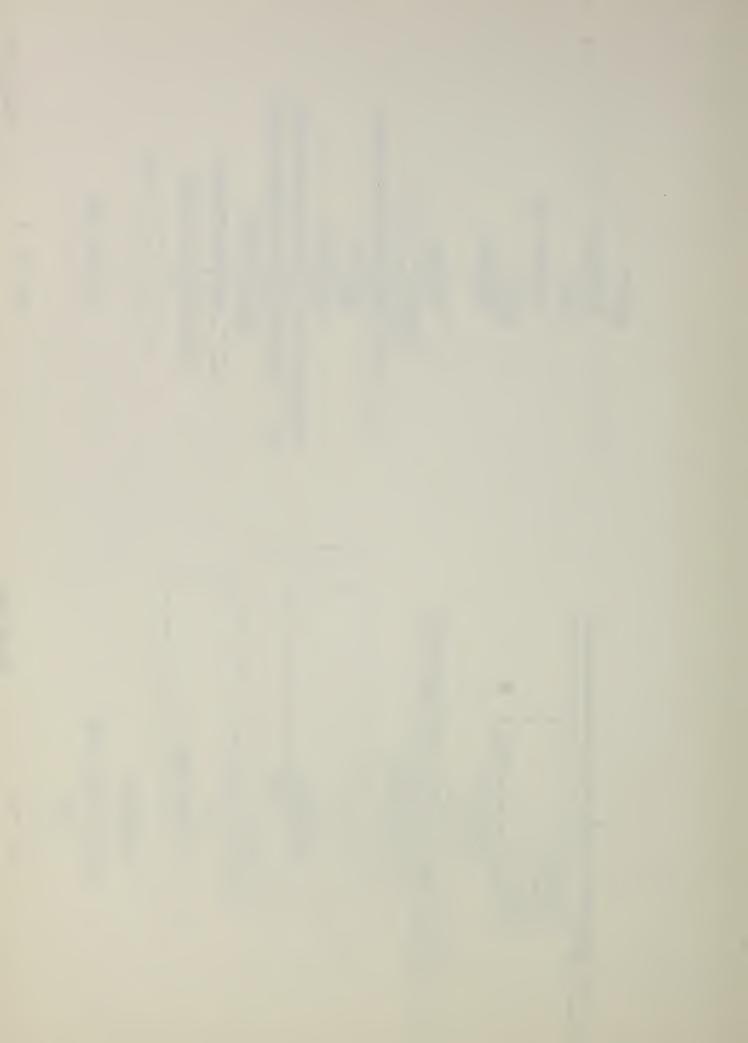


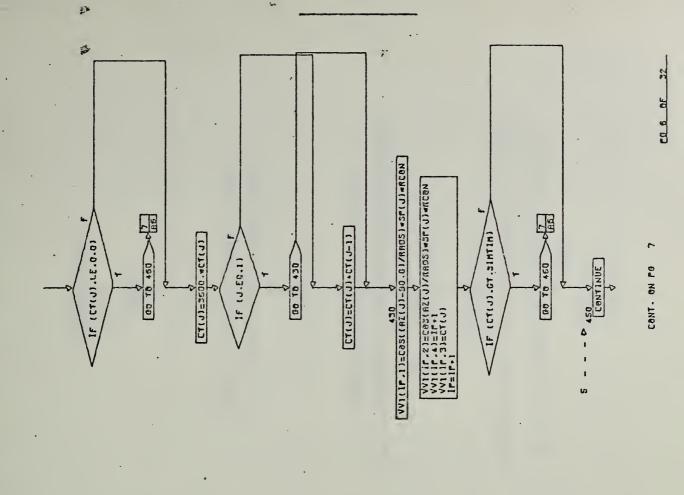


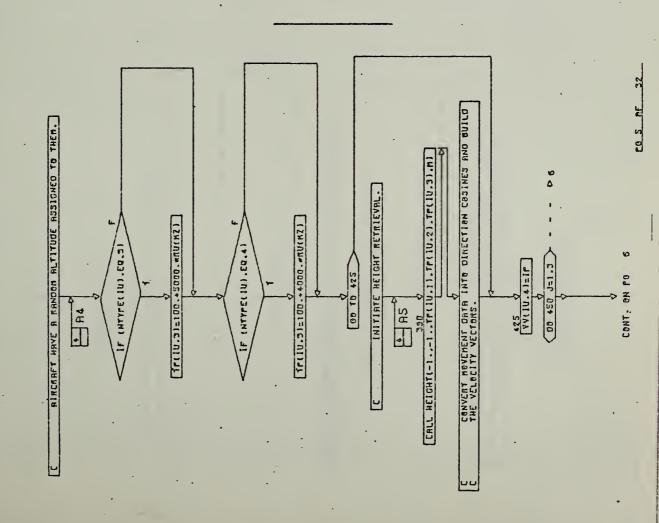


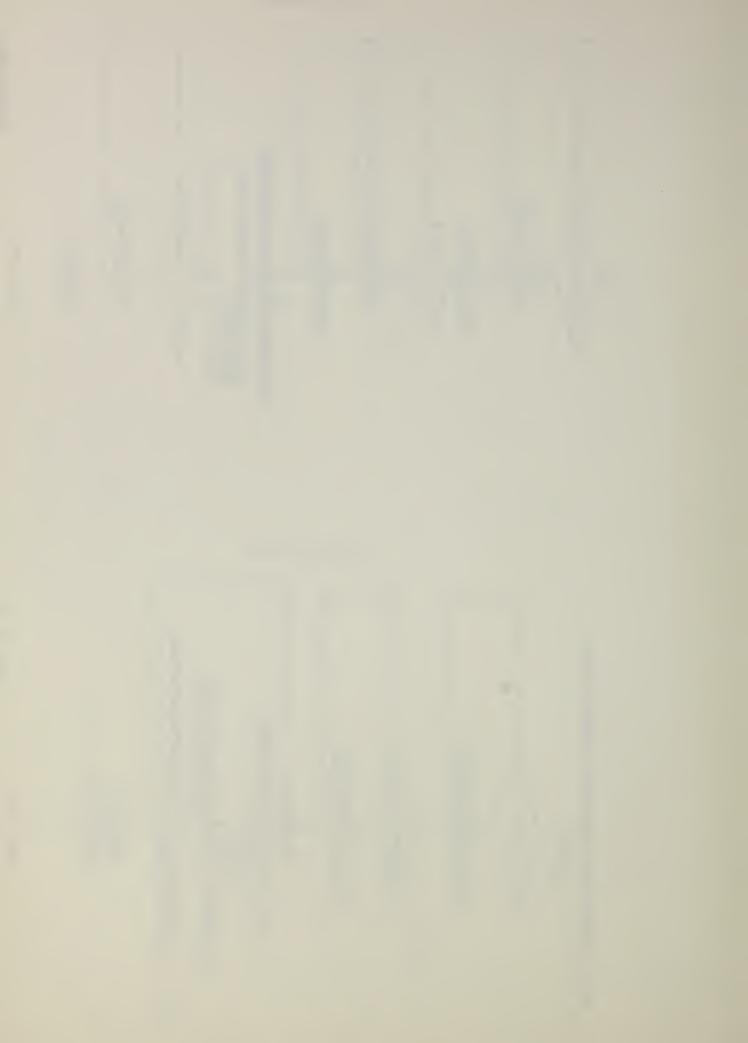


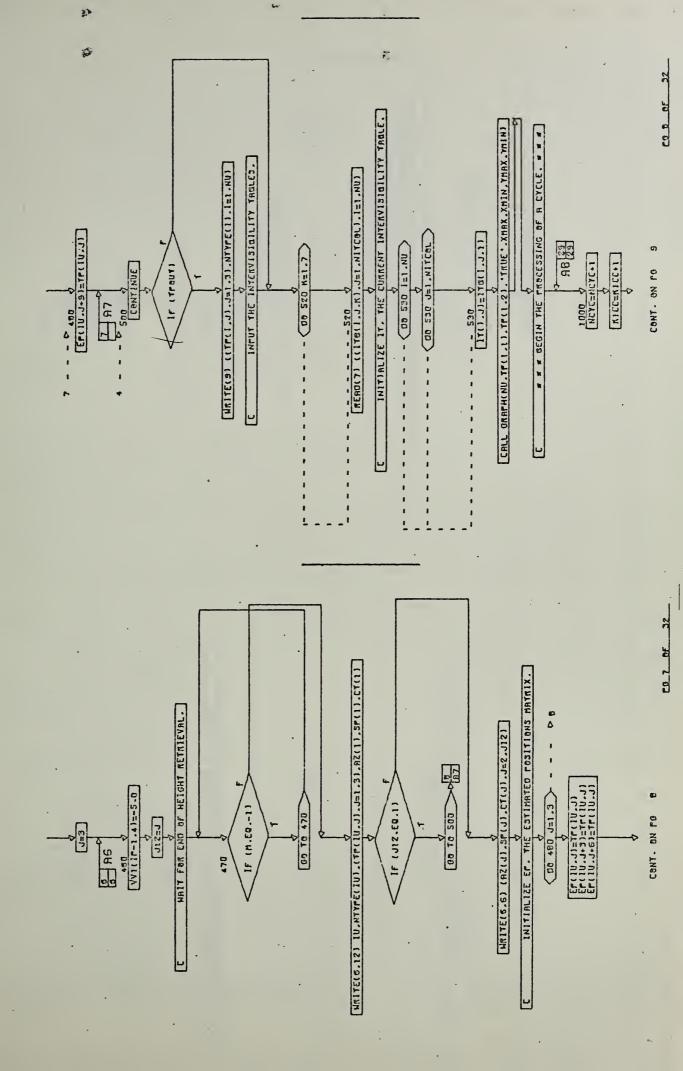




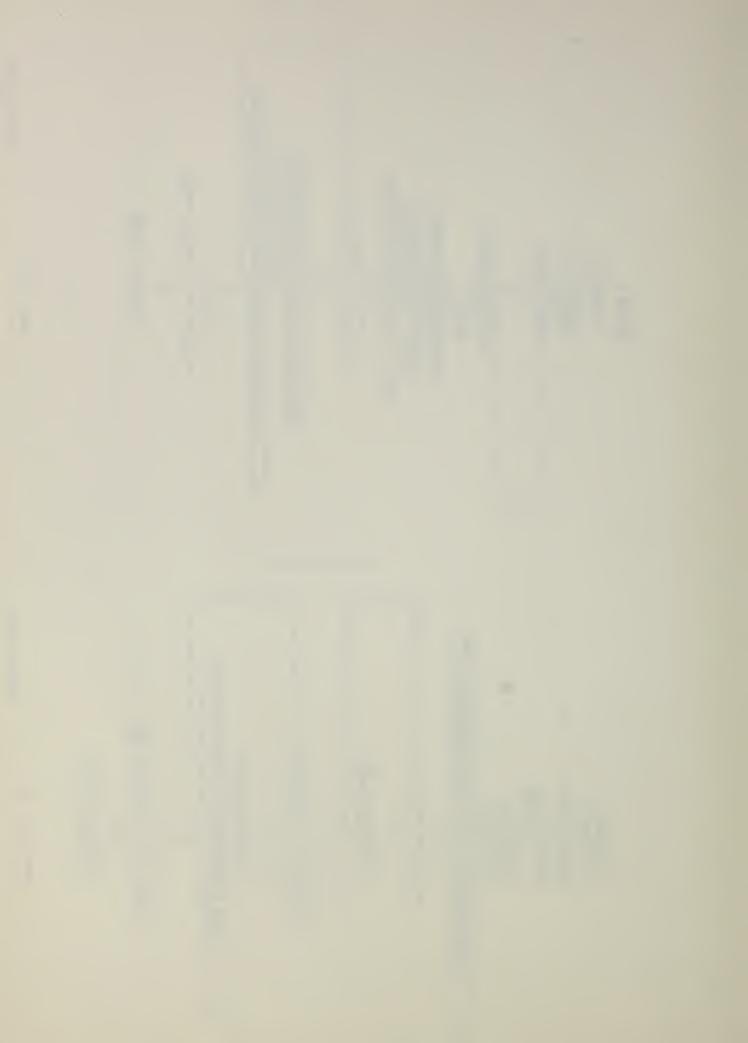








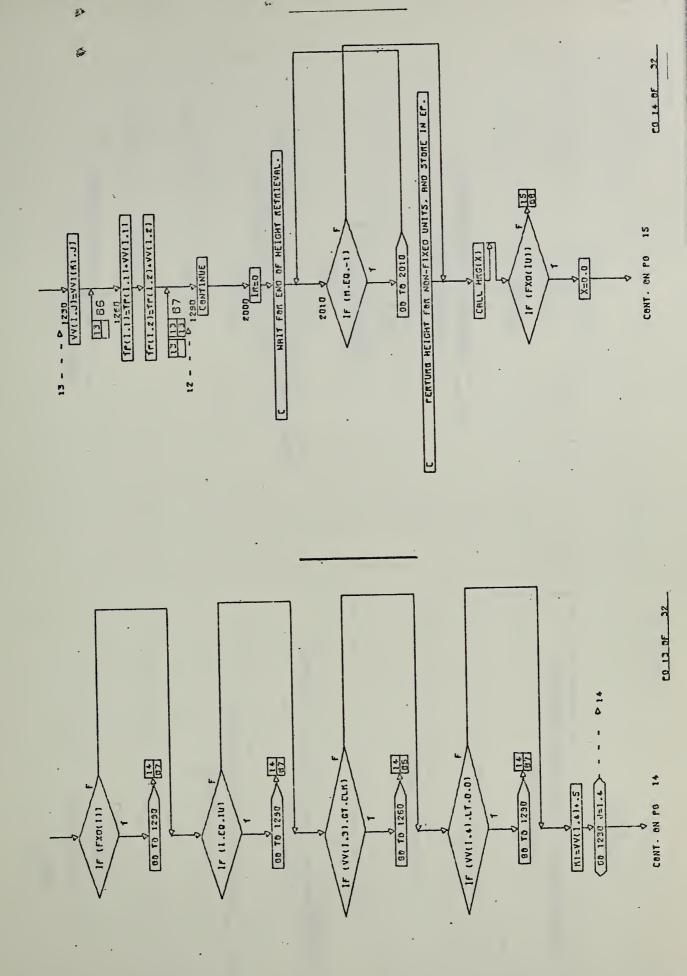




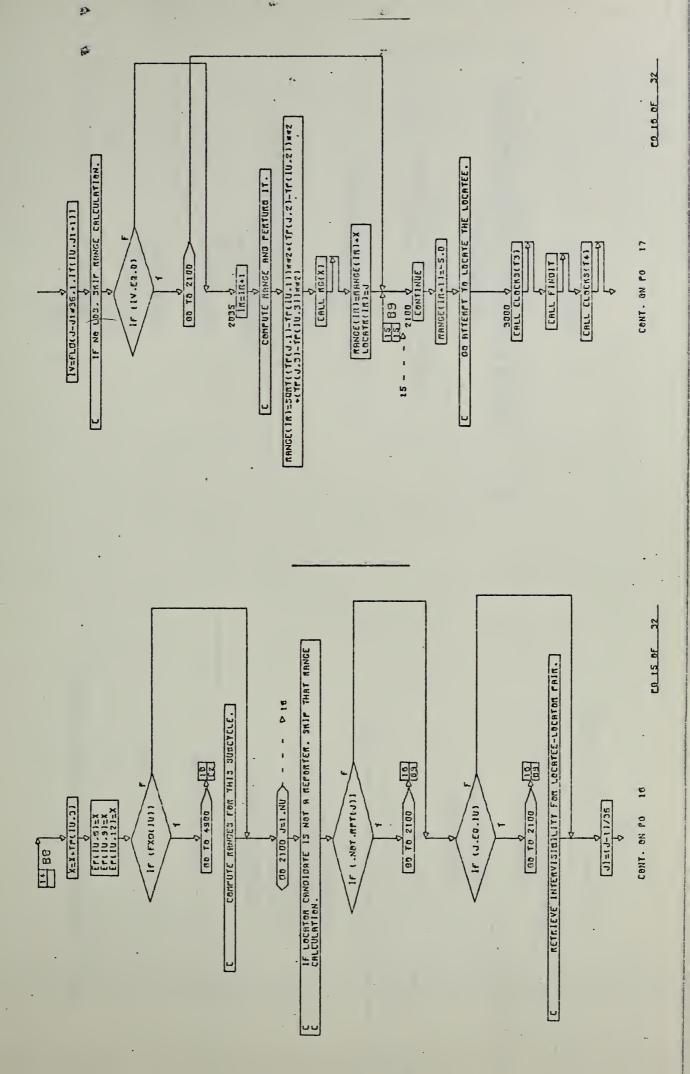
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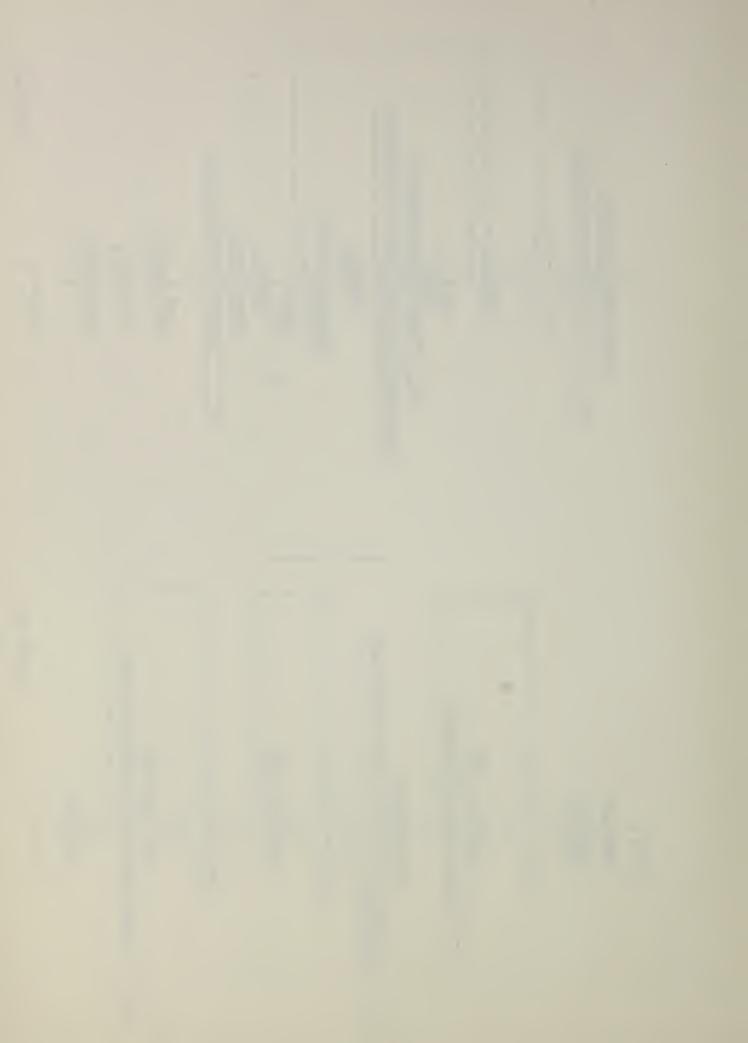
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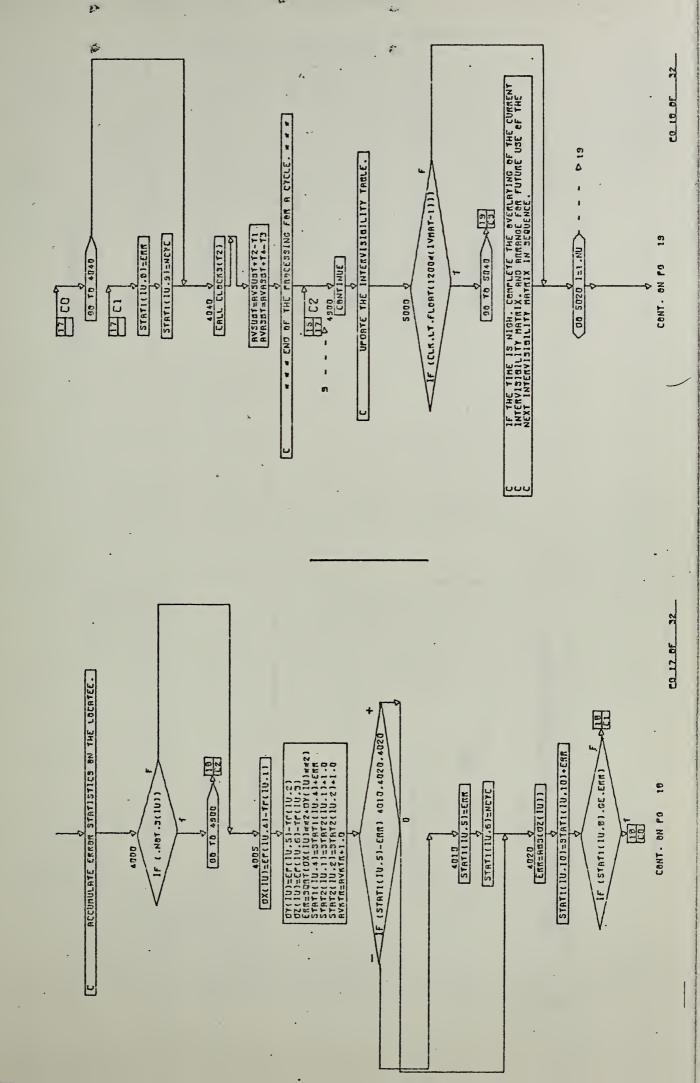


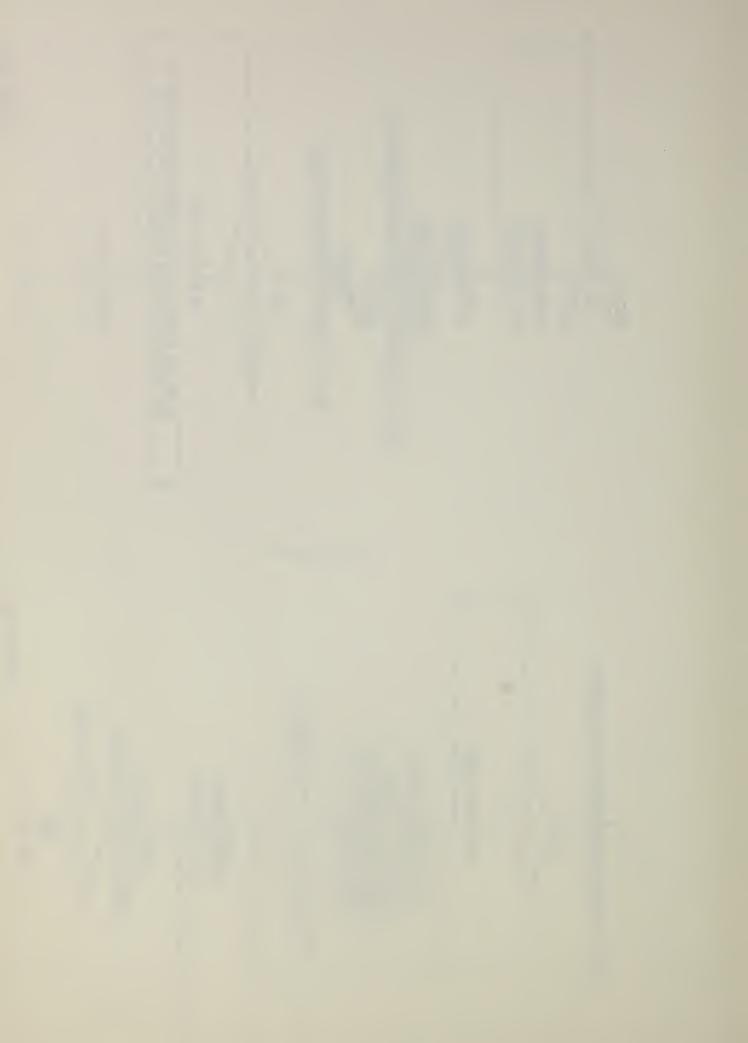


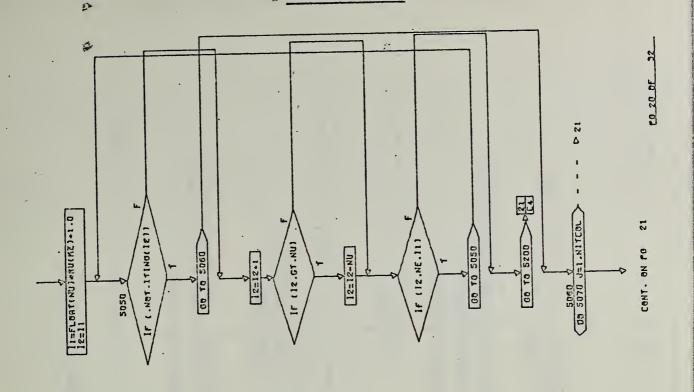


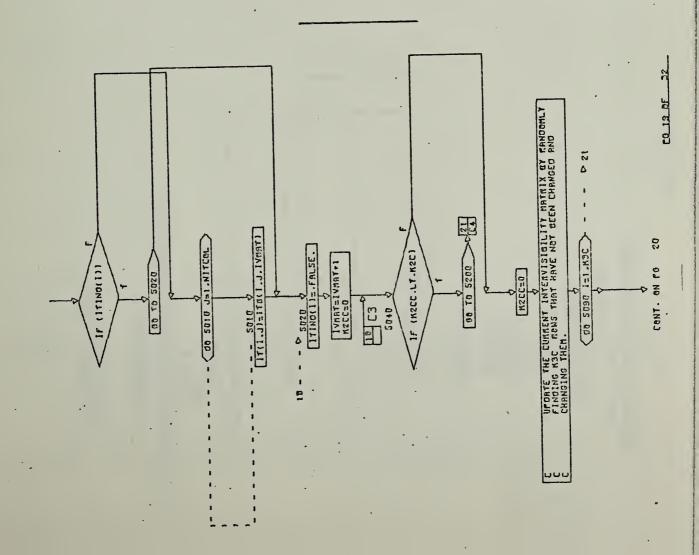




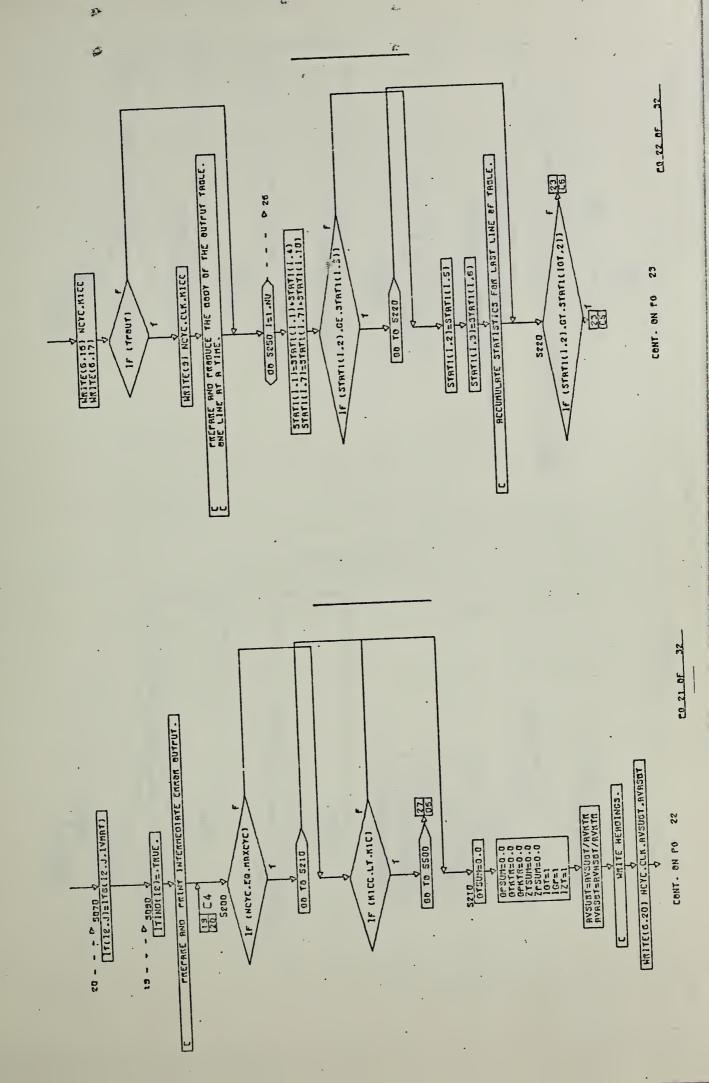




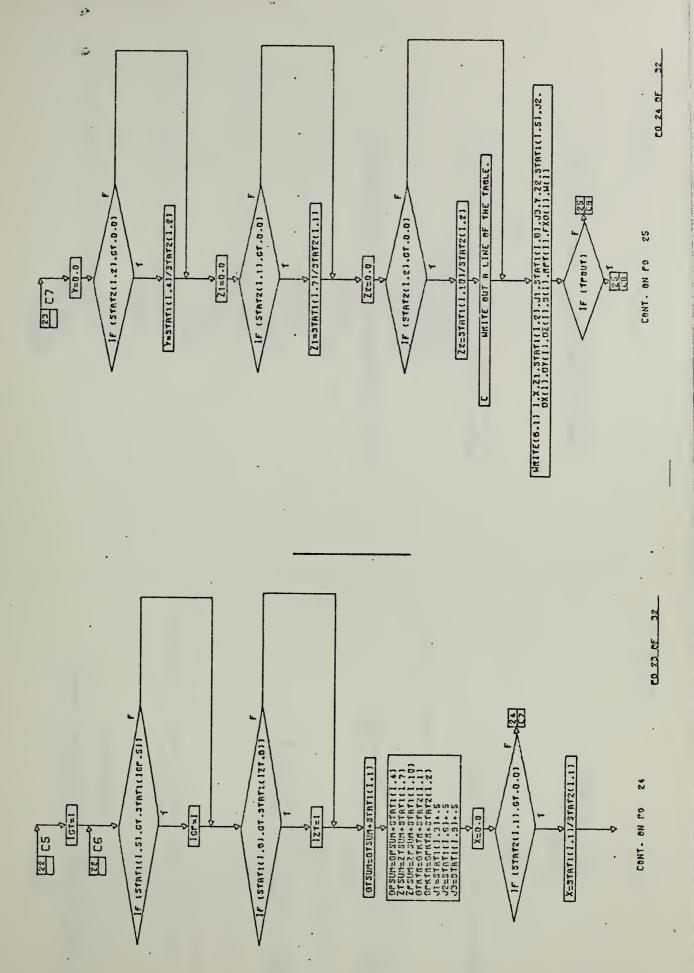


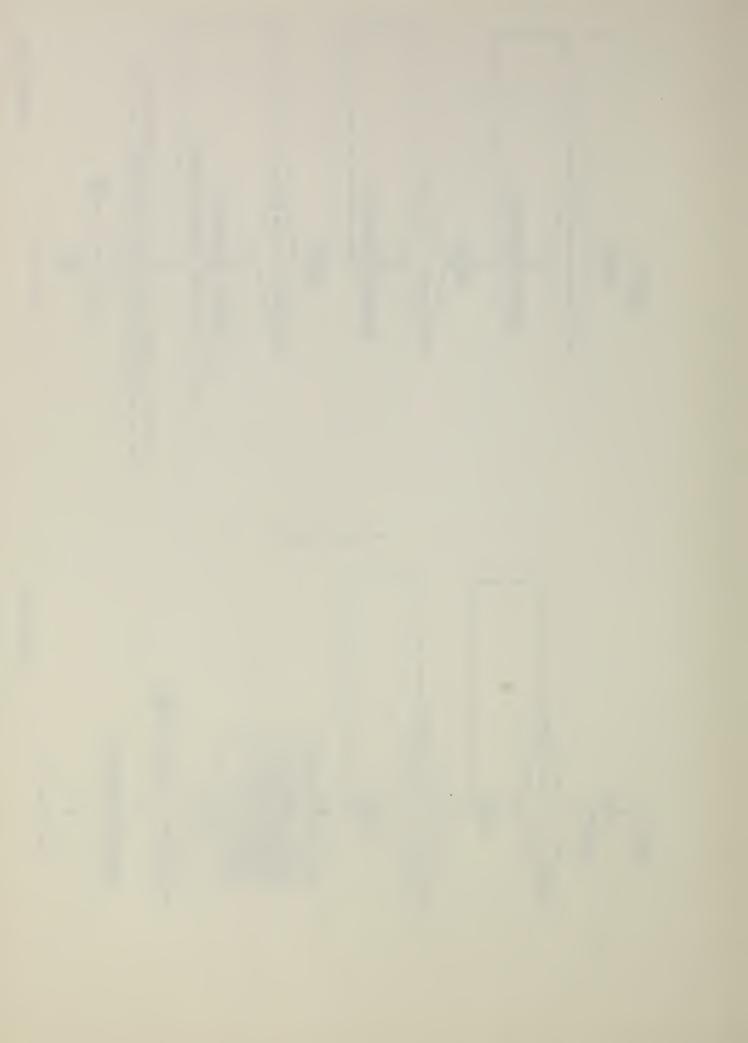


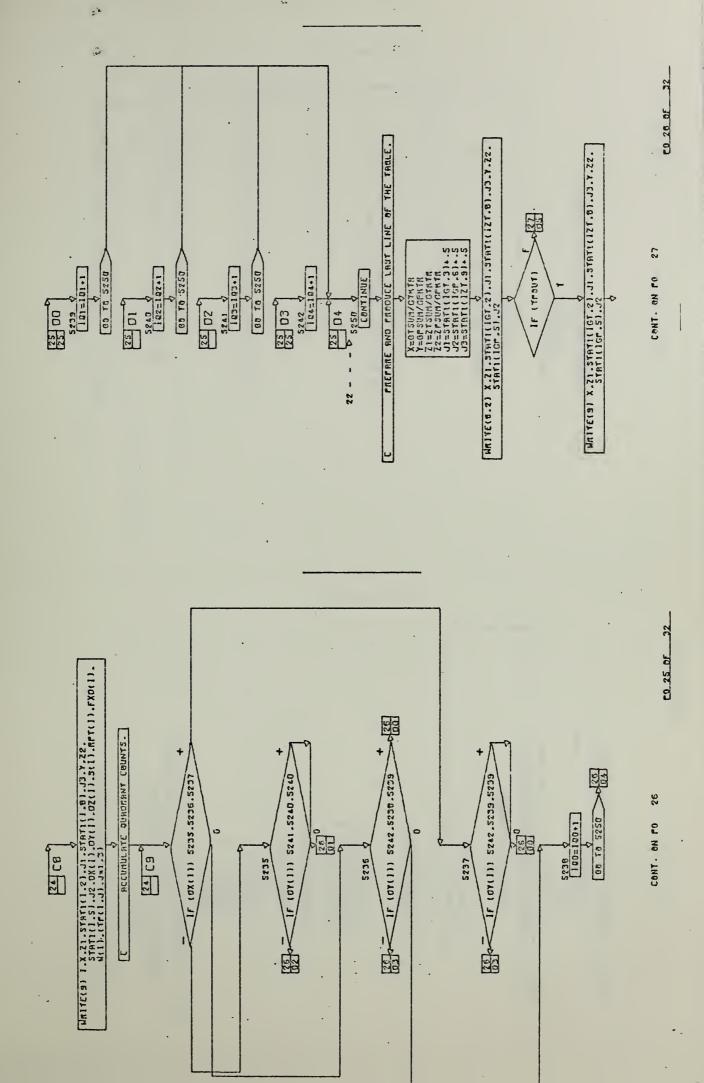


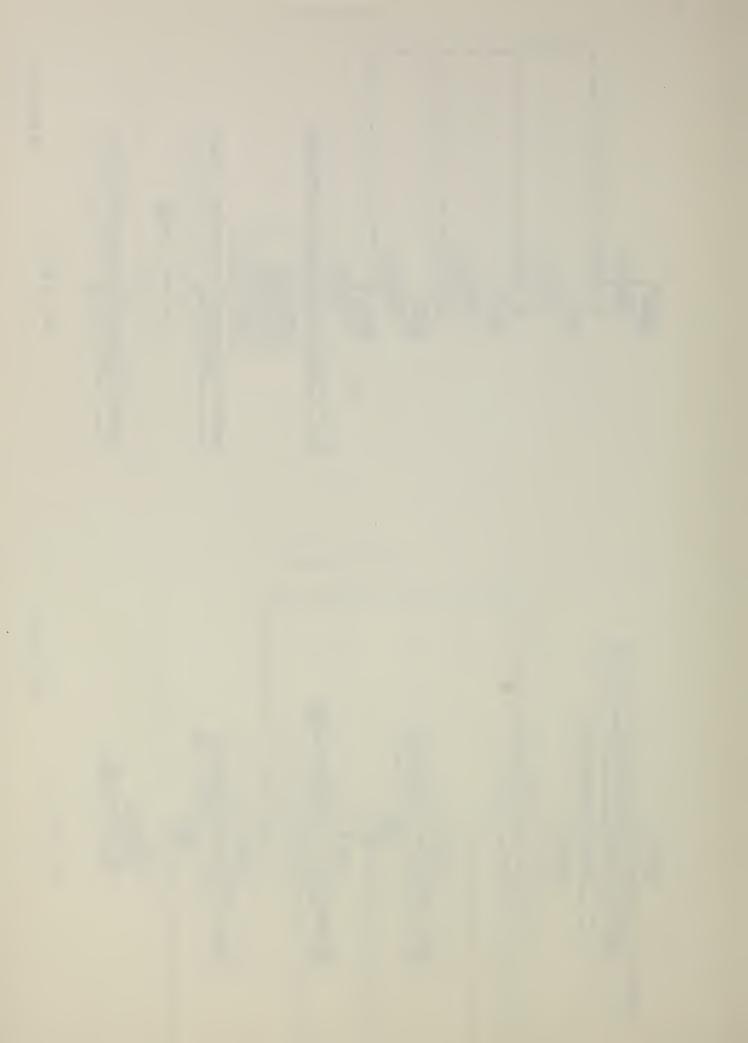


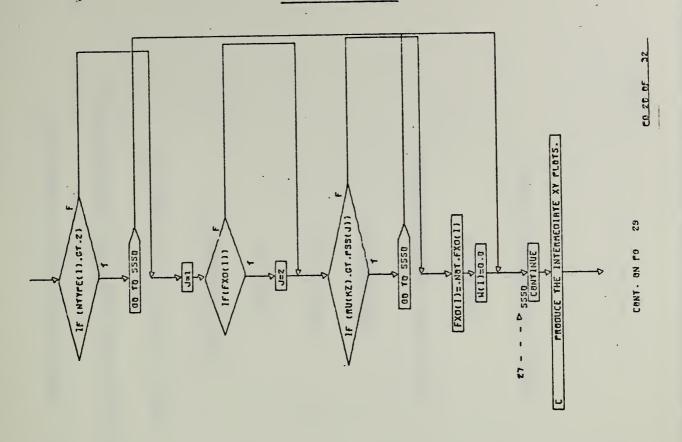


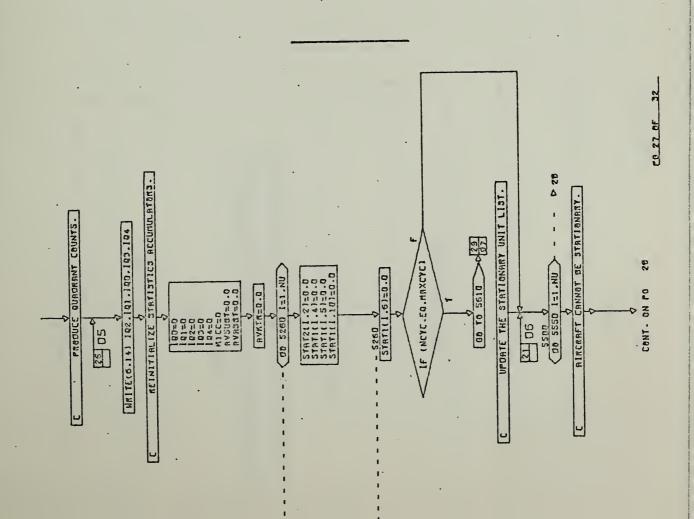




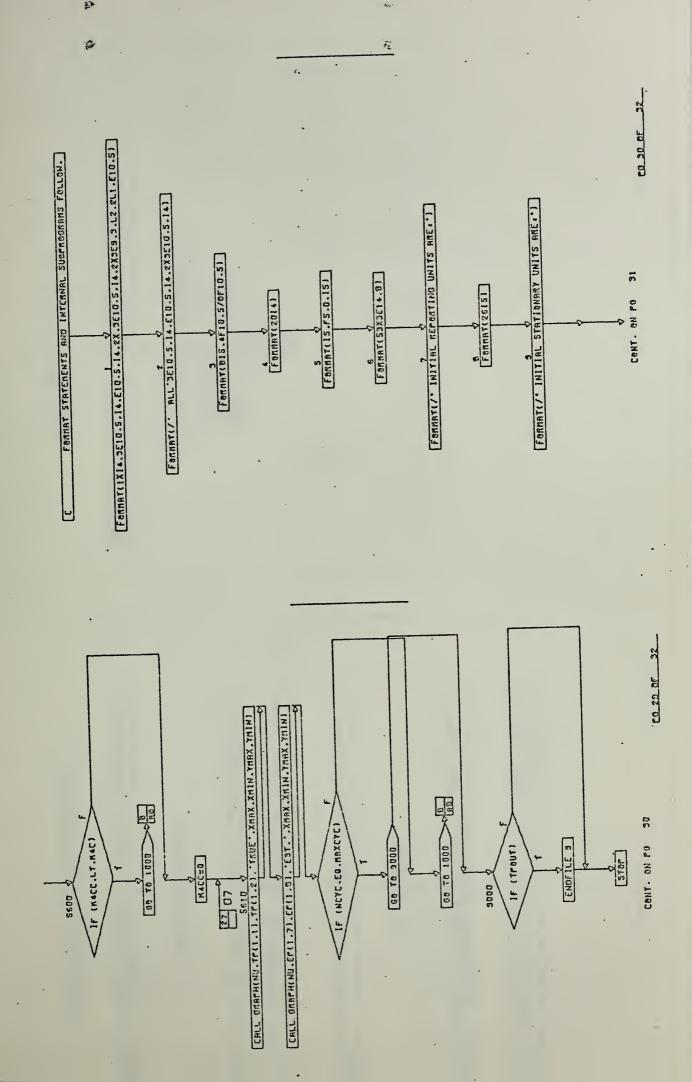




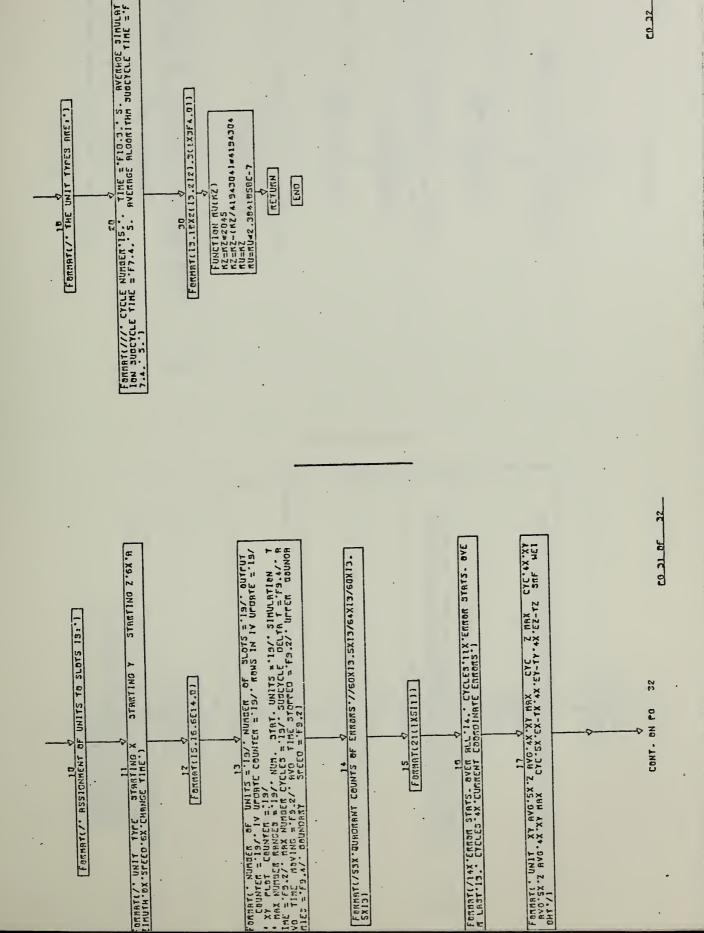




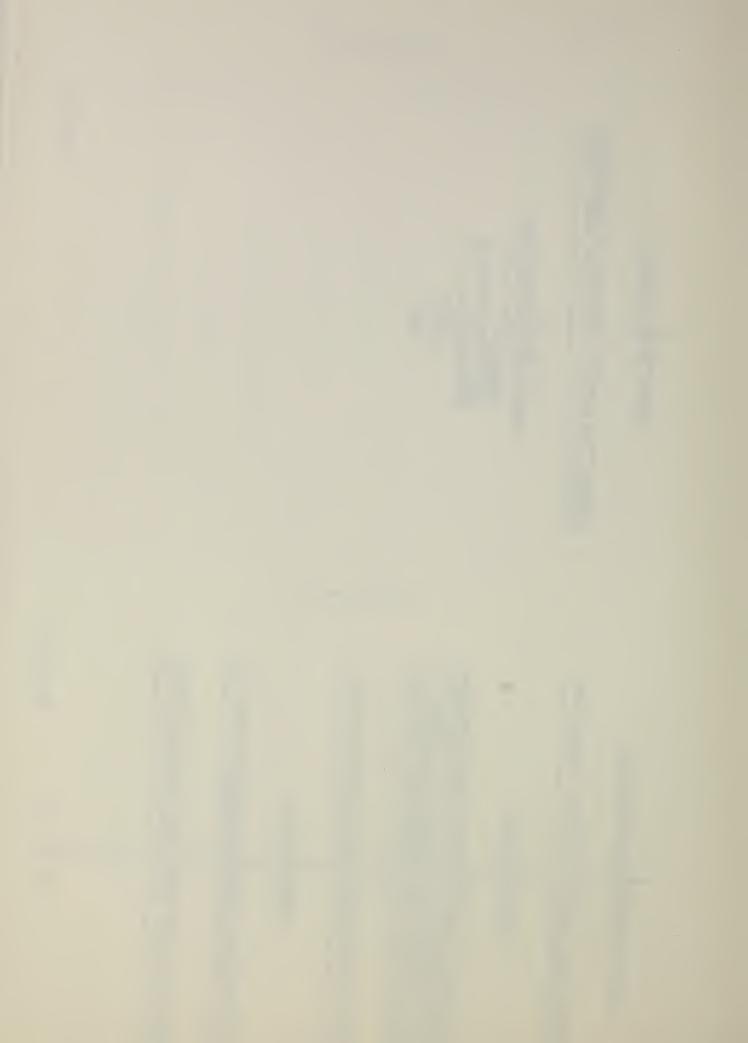


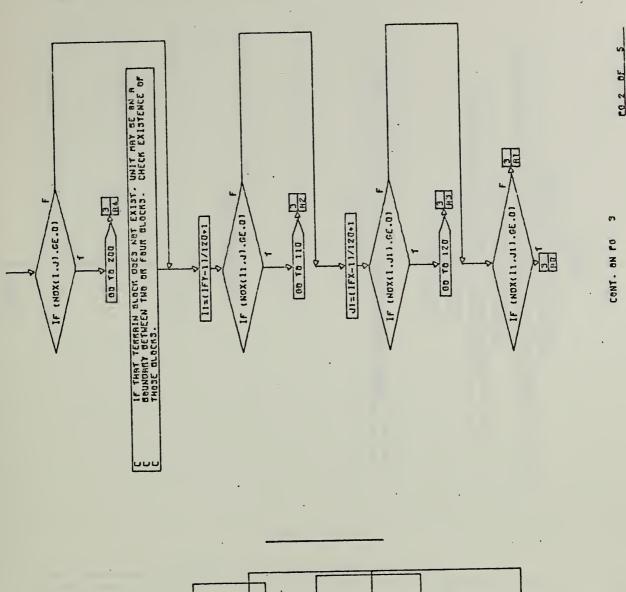


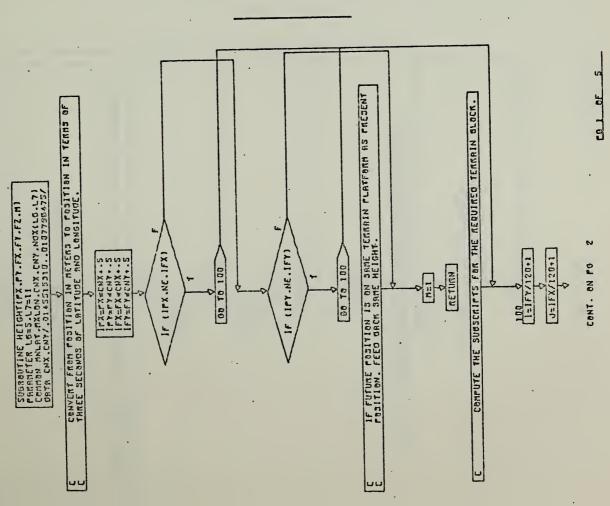




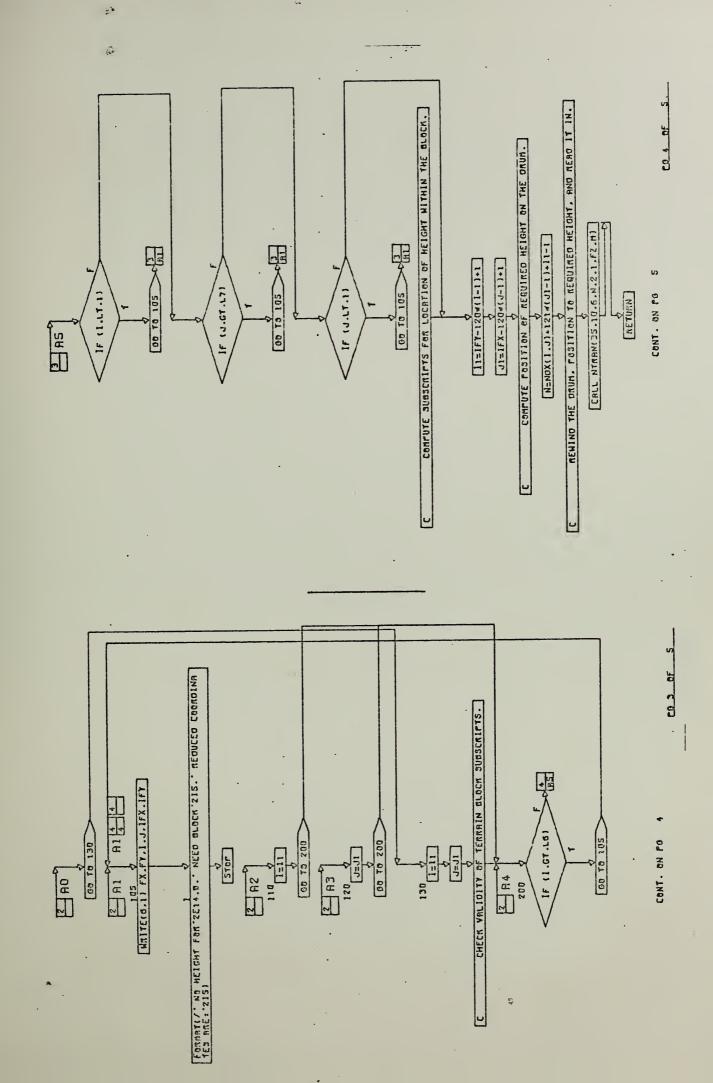
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